

# The Debiased Kuiper Belt: Our Solar System as a Debris Disk

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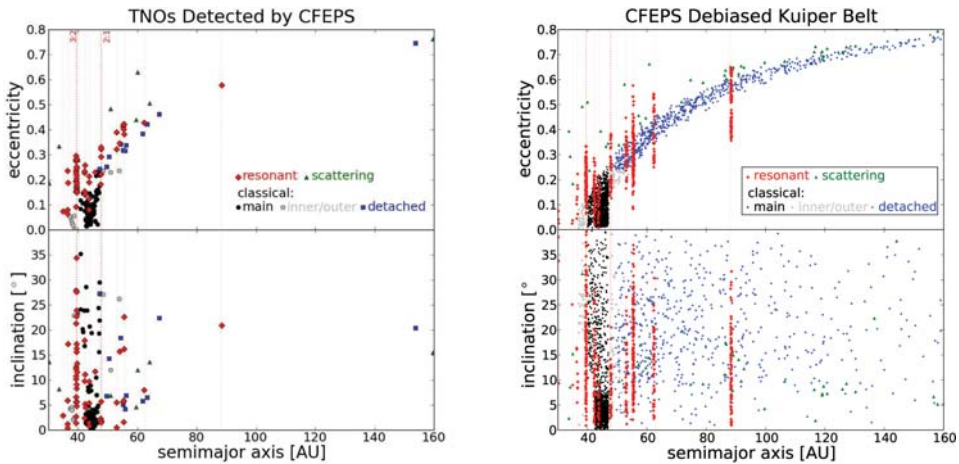
**Abstract.** The dust measured in debris disks traces the position of planetesimal belts. In our Solar System, we are also able to measure the largest planetesimals directly and can extrapolate down to make an estimate of the dust. The zodiacal dust from the asteroid belt is better constrained than the only rudimentary measurements of Kuiper belt dust. Dust models will thus be based on the current orbital distribution of the larger bodies which provide the collisional source. The orbital distribution of many Kuiper belt objects is strongly affected by dynamical interactions with Neptune, and the structure cannot be understood without taking this into account. We present the debiased Kuiper belt as measured by the Canada-France Ecliptic Plane Survey (CFEPS). This model includes the absolute populations for objects with diameters  $>100$  km, measured orbital distributions, and size distributions of the components of the Kuiper belt: the classical belt (hot, stirred, and kernel components), the scattering disk, the detached objects, and the resonant objects (1:1, 5:4, 4:3, 3:2 including Kozai subcomponent, 5:3, 7:4, 2:1, 7:3, 5:2, 3:1, and 5:1). Because a large fraction of known debris disks are consistent with dust at Kuiper belt distances from the host stars, the CFEPS Kuiper belt model provides an excellent starting point for a debris disk model, as the dynamical interactions with planets interior to the disk are well-understood and can be precisely modelled using orbital integrations.

**Keywords.** Kuiper Belt, solar system: formation, (stars:) planetary systems

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## 1. Introduction

There is much discussion in the literature about using resonant structure in debris disks as an indirect way to find planets (e.g. Wyatt 2006; Stark & Kuchner 2008). In debris disks, the observable components are the dust grains, which are used to infer the presence of a collisionally-grinding planetesimal belt (Wyatt 2008). In our own Solar System, the opposite is true: we can directly observe orbits of the planets and planetesimals to great precision, while no direct observations exist of dust in the Kuiper belt. We also know that the Kuiper belt has significant resonant structure (Gladman *et al.* 2012), which requires that Neptune's orbit has migrated outwards. This migration may have happened smoothly as Neptune scattered planetesimals inwards onto Jupiter-crossing orbits, "snowplowing" objects into mean-motion resonances along the way (Chiang & Jordan 2002; Hahn & Malhotra 2005), or Neptune may have been scattered outward by a close encounter with one of the other giant planets, and trapped planetesimals in mean-motion resonances as its eccentric orbit damped to near-circular (the "Nice model"; Levison *et al.* 2008).



**Figure 1.** Left panel shows orbital elements ( $a, e, i$ ) of TNOs discovered by CFEPS, and right panel shows debiased TNO orbital element distributions, where the relative numbers in each population and in each resonance are correct. Objects have symbols according to dynamical class (see key), and mean-motion resonance positions are indicated by dotted lines.

## 2. Survey Strategy

The Canada-France Ecliptic Plane Survey (CFEPS) was a large survey carried out with the Megacam instrument on the Canada-France-Hawaii Telescope (CFHT) between 2003–2007, with the goal of discovering many trans-Neptunian objects (TNOs) and using the known sky coverage, observation depths, and tracking fractions in different observing blocks at many points along the ecliptic plane to debias the observations and regain the true orbital distribution of the Kuiper belt.

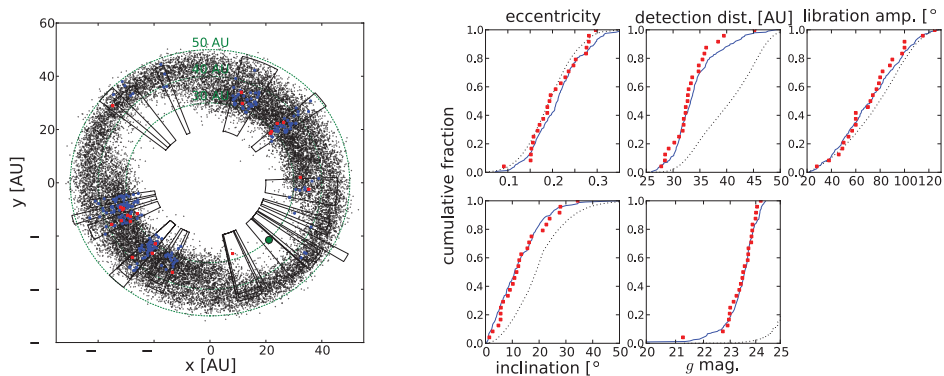
The observing strategy for CFEPS is described in detail in Jones *et al.* (2006), Kavelaars *et al.* (2009) and Petit *et al.* (2011). To summarize, a patch of sky is observed three times in a night, with each observation separated by about one hour. These triplets of images are searched for moving objects, and preliminary orbits are calculated. One month later, followup images are taken of the same field, and the same objects are recovered. This is repeated each month for 4–5 months. This 4–5 month baseline is used to predict object positions one year later, and the objects are recovered again, further improving the calculated orbits.

A 10 Myr-long orbital integration is performed using the orbital elements and position of each TNO, and including the gravitational effects of the four giant planets. The TNOs are then placed into dynamical classes following the procedure outlined by Gladman *et al.* (2008). The classes are resonant (TNOs in mean-motion resonances with Neptune), scattering (TNOs that closely encounter Neptune within 10 Myr), detached (TNOs that currently do not dynamically interact with Neptune), and classical (TNOs on low- $e$ , low- $i$  orbits with  $a$  within a few AU of Neptune).

## 3. Discoveries and Debiasing

CFEPS detected 176 TNOs. Their orbital element distributions are shown in the left panel of Figure 1.

Because the survey is well-characterized, it can be debiased to reproduce not only the orbital elements of each different dynamical class, but also the absolute populations. We



**Figure 2.** Left panel shows a distribution of plutinos viewed from above the Solar System, and right panel shows cumulative distributions in five different observable parameters: eccentricity, distance at detection, libration amplitude, inclination, and visible  $g$  magnitude. Black (in both panels) shows synthetic non-detections, blue circles/solid lines show synthetic detections by the survey simulator, and red squares shows real detections. Also shown in the left panel are the CFEPS observing blocks, with the relative magnitude limits indicated by the outer edge of each wedge (showing the distance limit where a  $\sim 100$  km diameter object would still be detected).

will use the plutinos (objects in the 3:2 mean-motion resonance) as an example to explain the debiasing process (Figure 2).

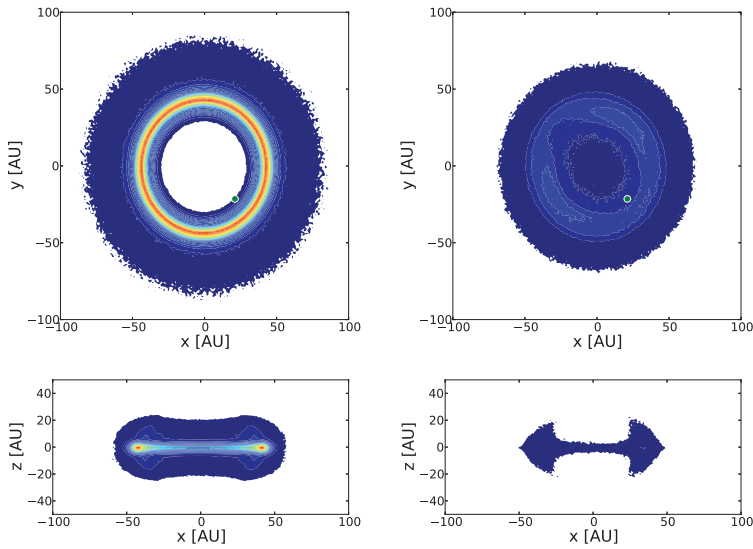
First, we choose parameters to model the distribution of synthetic plutinos in eccentricity, inclination, libration amplitude, and size distribution (shown in black in Figure 2), which is discussed in detail in Gladman *et al.* (2012) and Lawler & Gladman (2013). This synthetic distribution is run through the CFEPS survey simulator, where each object is evaluated to determine if it would have been detected by CFEPS. Synthetic detections are shown in blue in Figure 2. The cumulative distributions of five parameters of the synthetic detections are compared statistically to the cumulative distributions of the real CFEPS detections. Any modeled distribution where the bootstrapped comparison statistic for any of the five distributions occurs  $<5\%$  of the time is considered rejected. In this way, we get very powerful constraints on the orbital element distributions and the size distribution, and we can use this to calculate absolute population.

This modelling process is repeated for each resonance (Gladman *et al.* 2012) and other Kuiper belt components individually (Petit *et al.* 2011).

#### 4. A Simple Kuiper Belt Dust Model

Many very detailed models of the dust produced by the Kuiper belt exist in the literature (e.g. Vitense *et al.* 2010; Kuchner & Stark 2010). The model presented here is only meant to serve as a demonstration of how the CFEPS debiased Kuiper belt distribution (available for download at [www.cfeps.net](http://www.cfeps.net)) can be used as a starting point for a Kuiper belt dust simulation.

Figure 3 shows contour plots of the number density of the debiased resonant (right panels) and non-resonant TNOs (left panels). Applying a simple dust flux model, where each TNO is replaced by a modified-blackbody dust grain, the resonant structure is completely drowned out by the much higher number density of classical objects.



**Figure 3.** Number density contour plots of the classical (left panels) and resonant (right panels) debiased Kuiper belt looking down on the Solar System from above (top panels) and from edge-on (bottom panels). The position of Neptune is shown by a green circle in the top panels. The two top panels have the same contour levels, and the two bottom panels have the same contour levels, making it obvious that the classical objects dominate the number density.

## 5. Conclusions

The Kuiper belt has been sculpted by giant planet migration, and contains many populated resonances (20% of  $>100$  km objects are resonant), but this is difficult, if not impossible, to see in the overall disk structure as seen from afar. Currently, no theoretical giant planet migration models can reproduce all the structure that is observed in the Kuiper belt (Gladman *et al.* 2012). Because of the completely unknown biases that are present in the Minor Planet Center Database, the CFEPS debiased Kuiper belt distribution is currently the most accurate model for TNOs  $>100$  km in diameter, and makes an excellent starting point for collisional dynamical Kuiper belt dust models.

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**Discussion**

TRIAUD: Would you find a retrograde component?

LAWLER: Yes. The 5 month initial observation baseline is enough to diagnose a retrograde orbit and not lose it before follow-up observations 1 year later. Because CFEPS was in the ecliptic plane only, we didn't find any of these. A related survey using the same strategy as CFEPS and observing at higher ecliptic latitudes *did* find a retrograde object.

RAFIKOV: Do you have colour information on your objects?

LAWLER: Yes, but only g and r bands, and with large error bars. So not very good colour information.

MACINTOSH: Very nice talk! I am curious what the  $L_{IR}/L_*$  of the simple disk emission model is?

LAWLER: I didn't do my model carefully enough to calculate this. My model was really just supposed to be a demonstration of the CFEPS dataset and was supposed to encourage all of you in the audience to use our Kuiper Belt model to do a better dust model than this.

KRIVOV: What is the total mass of your debiased Kuiper Belt?

LAWLER: There are  $\approx 130,000$  objects  $> 100$  km in diameter, so a rough order-of-magnitude calculation gives about 1 Earth mass.

DVORAK: I expect that you also found Neptune Trojans.

LAWLER: CFEPS did not find any Neptune Trojans. The non-detection gives an upper limit of  $\approx 300$ -400 Neptune Trojans, which is consistent with the known Neptune Trojans. It isn't unexpected that CFEPS didn't detect any.