

Bayesian Inference for Radio Observations - Going beyond deconvolution

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Abstract. Radio interferometers suffer from the problem of missing information in their data, due to the gaps between the antennae. This results in artifacts, such as bright rings around sources, in the images obtained. Multiple deconvolution algorithms have been proposed to solve this problem and produce cleaner radio images. However, these algorithms are unable to correctly estimate uncertainties in derived scientific parameters or to always include the effects of instrumental errors. We propose an alternative technique called Bayesian Inference for Radio Observations (BIRO) which uses a Bayesian statistical framework to determine the scientific parameters and instrumental errors simultaneously directly from the raw data, without making an image. We use a simple simulation of Westerbork Synthesis Radio Telescope data including pointing errors and beam parameters as instrumental effects, to demonstrate the use of BIRO.

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1. Introduction

The problem of extracting scientific parameters from dirty (dominated by artifacts) interferometric radio images has resulted in many deconvolution algorithms being developed. However, none of these solve the problem of incorporating instrumental errors as a source of uncertainty when making measurements from radio data. Deconvolution algorithms can only produce one image, which the scientist must then assume is correct before extracting any science (for example, a catalogue of source fluxes) from it. Algorithms such as CLEAN (Högbom 1974), the most popular algorithm in use, cannot reliably produce any uncertainties (Junklewitz *et al.* 2013), making it impossible to propagate the uncertainties from instrumental errors to the scientific parameters. Further, if these parameters are correlated, as they likely are, even correcting the data for instrumental errors may lead to biased scientific results, as the measurement of the

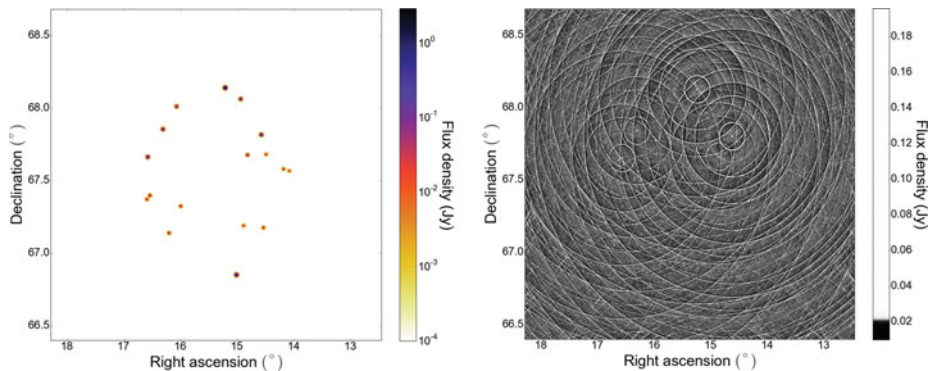


Figure 1. Mock dataset. *Left panel:* The simulated sky model. *Right panel:* The “dirty image”, which is how this field appears when convolved with the telescope beam.

instrumental error may be wrong. These instrumental effects will become more important as more sensitive telescopes such as the Square Kilometre Array† come online.

2. BIRO

We propose, in Lochner *et al.* 2015, a completely different approach, whereby we model the sky and all known sources of instrumental error simultaneously using the radio interferometry measurement equation (RIME) (Hamaker 1996). The RIME can be written as (Smirnov 2011):

$$\mathbf{V}_{pq} = \mathbf{J}_{pn} (\dots (\mathbf{J}_{p2} (\mathbf{J}_{p1} \mathbf{B} \mathbf{J}_{q1}^H) \mathbf{J}_{q2}^H) \dots) \mathbf{J}_{qm}^H, \quad (2.1)$$

where \mathbf{V}_{pq} is the visibility matrix (the radio data), \mathbf{J}_{pi} is the i 'th Jones matrix for antenna p (containing instrumental effects) and \mathbf{B} is the brightness matrix (containing the sky model, and hence all scientific parameters). We use the software package MeqTrees (Noordam & Smirnov 2010), which implements the RIME, to model our radio field and any known instrumental effects. We can then estimate the parameters of this model, both scientific and instrumental, in a Bayesian context using a sampling method such as MCMC (Metropolis *et al.* 1953, Hastings 1970). We assume uncorrelated Gaussian noise on the visibilities which leads to a simple Gaussian likelihood for \mathbf{V}_{pq} . With this approach, we are able to determine the full posterior for the problem, obtaining not only the best fits for all parameters, but also their uncertainties and correlations.

3. Applying BIRO

Fig. 1 shows the mock WSRT (Westerbork Synthesis Radio Telescope)‡ field which we tested BIRO on. This field, simulated using MeqTrees and based on a real field, consists of 17 point sources. We also applied pointing errors to each antenna as an example of a source of instrumental error, which WSRT (and many other radio telescopes) have had to deal with in the past (Smirnov & de Bruyn 2011). A mispointed antenna will observe a point source through the edge rather than the centre of its beam. Thus, in general, we would expect pointing errors and fluxes to be correlated and we apply our method to determine these correlations, as well as the parameters themselves.

The instrumental parameters for this simulated data consist of the pointing errors (one for each direction for each antenna), the width of the primary beam and the noise on the visibilities, which we assume to be Gaussian, as is widely considered a good approximation. We allow the pointing errors to vary in time as second order polynomial functions,

† Square Kilometre Array, <http://www.skatelescope.org>

‡ WSRT, <https://www.astron.nl/radio-observatory/astronomers/wsrt-astronomers>

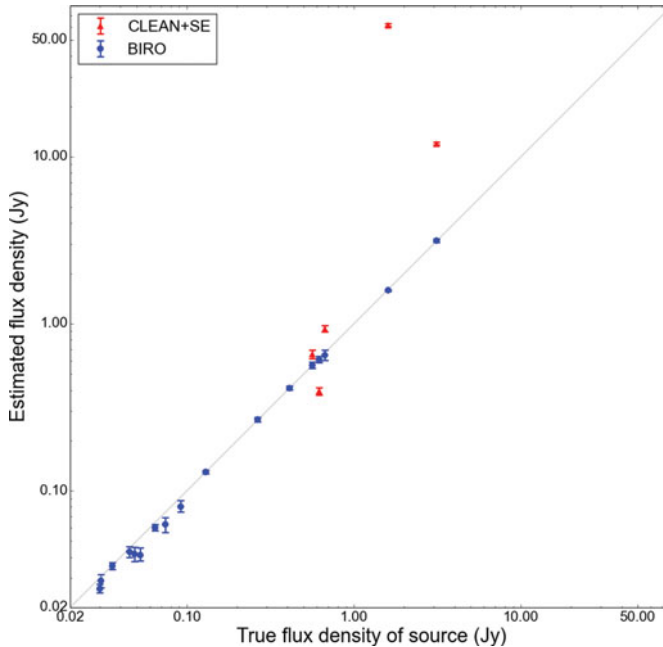


Figure 2. Comparison between BIRO and the fluxes obtained from CLEAN, combined with a source extraction algorithm (CLEAN+SE). While the BIRO results are unbiased, CLEAN+SE misestimates the fluxes by up to 44σ , due to the strong correlations between pointing error and flux.

resulting in 84 pointing error parameters (3 for each direction for each antenna). Our scientific parameters are the flux for each source.

We compared BIRO with the standard, commonly used CLEAN algorithm combined with a source extraction algorithm on the CLEANed image (we call this CLEAN+SE) for this dataset. Fig. 2 illustrates this comparison for the estimated fluxes from BIRO and CLEAN+SE. With no knowledge of the time-varying pointing errors, it is no surprise that CLEAN+SE returns biased fluxes. The danger is that the error bars, estimated using only the surrounding flux of the point source in this source extraction algorithm, do not and cannot take into account the additional source of uncertainty from the instrumental errors. In contrast, the BIRO estimates are unbiased and the error bars are larger, correctly propagating the instrumental errors. We also found that while CLEAN+SE identified many of the point sources as extended (and the only extended source as a point source), BIRO is properly able to determine the type of each source simply by fitting shape parameters to the sources. BIRO is also able to determine the covariance matrix between all the parameters (Fig. 3).

4. Conclusions

We have introduced BIRO, a Bayesian approach to the deconvolution problem of radio interferometry observations. Fig. 3 highlights the importance of fully propagating the uncertainty on instrumental errors, as they can be highly correlated with the scientific parameters and hence bias scientific results. Due to the fully Bayesian nature of BIRO, it allows for very elegant extensions to this simple scenario. For example, the choice of model for the field can be selected for using the Bayesian evidence (see Lochner et al. 2015). BIRO can be useful in any scenario where reliable statistics are required for the science extracted and may be essential to fully exploit the sensitivity of the SKA.

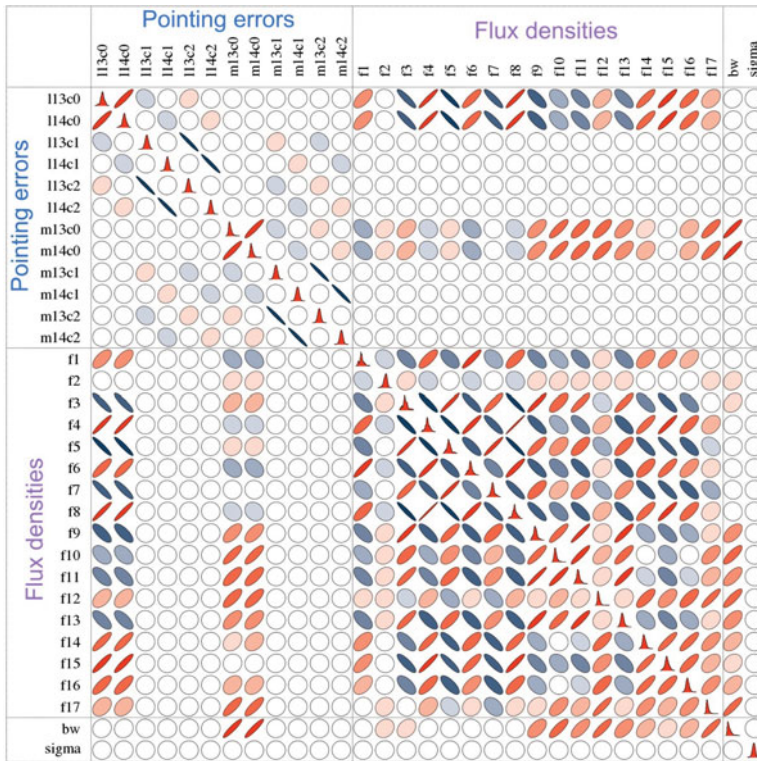


Figure 3. Covariance matrix between a subset of parameters. The parameters are listed on each axis with the correlations between them represented by a coloured ellipse. Highly correlated parameters are red with a thin ellipse angled to the right, whereas anti-correlated parameters have a dark blue ellipse, angled to the left. The diagonal shows the 1D marginalised posterior for each parameter. The correlations in the fluxes arise due to uncertainty in the flux distribution from gaps in the uv -plane, while the pointing errors are correlated simply because every pointing error affects every source. Of particular interest is the complex way in which pointing errors correlate with the fluxes, which would be very difficult to determine from first principles.

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