

Residential Demand Module of the National Energy Modeling System: Model Documentation

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Update Information

This edition of the *Residential Demand Module of the National Energy Modeling System: Model Documentation* reflects changes made to the module since the previous iteration of this report. These changes include the following:

- Incorporating new equipment efficiency standards, including standards for furnace fans and external power supplies, as well as a voluntary agreement for set-top boxes (AEO2015)
- Updating cost and performance assumptions for major end-use equipment (AEO2015)
- Revising and refining market niches for distributed generation to more accurately reflect solar insolation and marginal prices at the sub-Census division level (AEO2015)
- Modeling the impacts of energy efficiency expected with the implementation of the Environmental Protection Agency's Clean Power Plan (AEO2016)
- Adding energy efficiency rebate modeling capability for major end-use equipment (AEO2015)
- Adding energy efficiency rebate modeling capability for distributed generation equipment (AEO2016)
- Updating solar photovoltaic generation calibration using latest version of PVWatts software (AEO2016)
- Extending modeling projection horizon through 2050 (AEO2017)
- Incorporating the option to use ZIP code-level hurdle models of solar photovoltaic systems (AEO2016), calibrated to historical capacity levels by U.S. Census division (AEO2017)
- Using a 5-year average of historical consumption benchmarking factors to transition into projected consumption (AEO2017)
- Modeling wine coolers consumption as a miscellaneous electric load to represent recent DOE equipment efficiency standard (AEO2017)
- Improving representation of distributed energy generation impacts on end-use load shapes (AEO2017)
- Adjusting shares of PV generation deducted from specific end uses (AEO2017)
- Including historical and projected energy efficiency program impact estimates (AEO2017)

Additional information regarding annual changes to modeling and assumptions can be found online with AEO Buildings Working Group materials.

Introduction

Purpose of this report

This report documents the objectives, analytical approach, and structure of the National Energy Modeling System (NEMS) Residential Demand Module (RDM). The report catalogues and describes the model assumptions, computational methodology, parameter estimation techniques, and Fortran source code.

This document serves three purposes. First, this report meets the legal requirement of the U.S. Energy Information Administration (EIA) to provide adequate documentation in support of its reports according to Public Law 93-275, section 57(b)(1). Second, it is a reference document that provides a detailed description for energy analysts, other users, and the public. Finally, it facilitates continuity in model development by providing documentation from which energy analysts can undertake model enhancements, data updates, model performance evaluations, and parameter refinements.

Model summary

The NEMS Residential Demand Module is used in developing long-term projections and energy policy analysis over the time horizon beginning with EIA's most recent <u>Residential Energy Consumption Survey (RECS)</u> (the module's base year) through 2050 (the current projection horizon). The model generates projections of energy demand (or energy consumption; the terms are used interchangeably throughout the document) for the residential sector by end-use service, fuel type, and U.S. Census division.

The RDM uses inputs from NEMS such as energy prices and macroeconomic indicators to generate outputs needed in the NEMS integration process. These inputs are used by the module to generate energy consumption by fuel type and Census division in the residential sector. NEMS uses these projections to compute equilibrium energy prices and quantities.

The RDM is an analytic tool that is used to address current and proposed legislation, private sector initiatives, and technological developments that affect the residential sector. Examples of policy analyses include assessing the potential impacts of the following:

- New end-use technologies
- Changes in fuel prices due to tax policies
- Changes in equipment energy-efficiency standards and building energy codes
- Financial incentives for energy efficiency and renewable energy investments

Archival media

The Residential Demand Module has been archived as part of the NEMS production runs that generate the *Annual Energy Outlook 2017* (AEO2017).

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Report organization

The first chapter of this report discusses the purpose of the RDM, with specific details on the objectives, primary inputs and outputs, and relationship of the module to other modules in NEMS.

Chapter 2 describes the rationale behind the design, fundamental assumptions regarding consumer behavior, and alternative modeling approaches.

Chapter 3 describes the NEMS RDM structure, including flowcharts and major sub-routines.

Appendices to this report document the variables and equations contained in the Fortran source code. Appendix A catalogues the input data used to generate projections in list and cross-tabular formats. Appendix B provides mathematical equations that support the program source code in the module. Appendix C is a bibliography of reference materials used in the development process. Appendix D discusses the data quality of the primary data source that informs the module.

Chapter 1: Model Purpose

Module objectives

The NEMS Residential Demand Module has three fundamental objectives:

- 1. The module generates disaggregated projections of energy demand in the residential sector from the base year through the projection horizon by housing type, fuel type, Census division, and end-use service.
- 2. It is an analysis tool that can assess the impacts of changes in energy markets, building and equipment technologies, and regulatory initiatives that affect the residential sector.
- The module is an integral component of NEMS; it provides projected energy demand to the supply and conversion modules of NEMS, and contributes to the calculation of the overall energy supply and demand balance.

The Residential Demand Module projects residential sector energy demand in six sequential steps. These steps produce information on housing stocks, technology choices, appliance stocks, building shell integrity, distributed generation, and energy consumption. The module uses a stock-vintaging approach that monitors equipment stock and equipment efficiency over time.

The module design allows the user to conduct a variety of analyses to assess proposed changes in policy or explore other uncertainties about future residential energy markets. Technological advancement in equipment design and efficiency, as well as incentive programs (such as rebates or tax credits), can be modified for specific types of equipment. Housing stock attrition and equipment retirement assumptions can be modified to reflect varying equipment performance over time. Building shell characteristics can be modified to reflect varying policy options, such as building codes or the impact of mortgage incentives for energy efficiency.

Projected residential fuel demand generated by the RDM is used by NEMS in the calculation of the demand and supply equilibrium. In addition, the NEMS supply modules use the residential sector outputs to determine the patterns of consumption and the resulting prices for energy delivered to the residential sector.

Module input and output

Inputs

The primary module inputs include fuel prices, housing stock characteristics, housing starts, population, and technology characteristics. The technology characteristics used in the module include installed capital costs (in real dollars), equipment efficiency, and expected equipment lifetimes. The major inputs by module component are as follows:

Housing Stock Component

Housing starts
Existing housing stock in the base year
Housing stock attrition rates

Housing floor area trends (new and existing)

Technology Choice Component

Equipment retail or replacement cost

Equipment subsidies

Equipment energy efficiency

Equipment penetration level (i.e., percent of households with that equipment)

Water usage factors

Fuel and equipment switching costs

Fuel costs

Appliance Stock Component

Expected equipment minimum and maximum lifetimes

Base-year equipment stocks

Equipment saturation level (i.e., the number of units per household)

Building Shell Component

Level of shell integrity (insulation and air tightness)

Price elasticity of shell integrity

Rate of improvement in existing housing shell integrity

Cost and efficiency of various building shell measures for new construction

Distributed Generation Component

Equipment cost

Equipment subsidies

Equipment conversion efficiency

Solar insolation values

Cross-sector capacity levels

System penetration parameters

Wind speeds

Grid interconnection limitations

Energy Consumption Component

Base-year unit energy consumption (UEC)

Population-weighted heating and cooling degree days

Population

Household size

Personal disposable income

Outputs

The primary module output is projected residential sector energy consumption by fuel type, end-use service, and Census division. The module also projects housing stock and energy consumption per housing unit. In addition, the module can produce a disaggregated projection of appliance stock and efficiency for the types of equipment included in the model:

Furnaces (electric, natural gas, liquefied petroleum gas (LPG), and distillate fuel oil) Hydronic heating systems/ boilers (natural gas, distillate fuel oil, and kerosene) Heat pumps (electric air-source, ground-source, and natural gas) Wood stoves Air conditioners (central and room)

Dishwashers

Water heaters (electric, natural gas, distillate fuel oil, LPG, and solar)

Cookstoves (electric, natural gas, and LPG)

Clothes washers

Clothes dryers (electric and natural gas)

Refrigerators (with top-, side-, and bottom-mounted freezers)

Freezers (upright and chest)

Lighting (general service, linear fluorescent, reflector, and exterior)

Solar photovoltaic systems

Fuel cells

Wind turbines

Geographic classification

The NEMS modules are designed to provide and use system data at the Census division level of aggregation, forming nine model regions within the United States. There are two primary reasons for using the Census division level of model specificity: the input data available from EIA's RECS and several other key input sources such as the Census Bureau are generally specified for the nine Census divisions; and the technical constraints of the computing system required in order to run the NEMS model within a reasonable turnaround time. The need to balance data availability, model runtime, and model output detail is best met at the Census division level.

Building type classification

While RECS and several Census Bureau products use residential building types (single-family detached, single-family attached, multifamily with 2-4 units, multifamily with 5 or more units, and mobile homes), NEMS uses just three building types: single-family, multifamily, and mobile homes. Manufactured housing is considered single-family housing.

The key geographic, building type, and major end use classifications within the module are often numbered as seen in Table 1. Fuels are indexed differently depending on where they are referenced within the RDM (Table 2).

Table 1. Categorization of key variables

Dimension	Census Division	Housing Type	End-Use Service	
Subscript:	D	В	S	
Index Value				Category
1	New England	Single-Family	Space Heating	Major
2	Middle Atlantic	Multifamily	Space Cooling	
3	East North Central	Mobile Home	Clothes Washing	
4	West North Central		Dishwashing	
5	South Atlantic		Water Heating	
6	East South Central		Cooking	
7	West South Central		Clothes Drying	
8	Mountain		Refrigeration	
9	Pacific		Freezing	
10			Lighting	
11	U.S. Total		Televisions & Related Equipment	Minor
12			Computers & Related Equipment	
13			Furnace Fans & Boiler Circulation Pumps	
14			Misc. End-Use Loads (MELs)	

Table 2. Mapping of fuel variables

Dimension			
FCON	RTFUEL		
Consumption	Technology	Fuel Name	Category
Fuel Index	Fuel Index		
1	3	Natural Gas	Major
2	4	Electricity	
3	1	Distillate Fuel Oil	
4	2	Liquefied Petroleum Gas (LPG)	
5	5	Kerosene	
6	1	Wood	Minor/ Renewable
7	4	Geothermal	
8	4	Solar	

Note: Wood is priced to distillate fuel oil when comparing across fuels; geothermal and solar are priced to electricity.

Relationship to other models

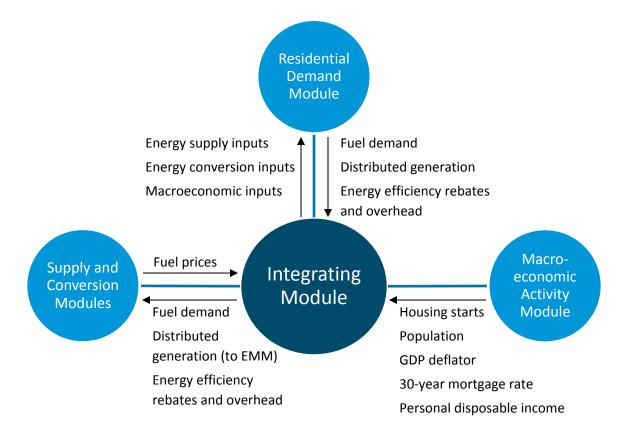
The RDM uses data from the Macroeconomic Activity Module (MAM) of NEMS. The MAM provides projected population, personal disposable income, housing starts by Census division and housing type, a gross domestic product price deflator, and a 30-year residential mortgage rate.

The RDM uses fuel price projections generated by the NEMS supply and conversion modules to calculate operating costs for technology selections, existing building shell integrity improvements, and short-term behavioral responses.

The NEMS supply and conversion modules in turn use the residential sector outputs to determine the fuel mix and the resulting prices for energy delivered to the residential sector. The Electricity Market Module (EMM) also receives aggregated utility rebate incentives and efficiency program overhead costs calculated in the RDM in order to further represent utilities passing such program costs to consumers.

Distributed generation by some technologies (such as on-site residential systems instead of utility-scale systems) is provided to the EMM for the calculation of renewable energy credits. Utility subsidies and overhead costs are also provided. Cumulative capacity levels for distributed generation technologies are shared across the residential, commercial, and electricity market modules in order to facilitate technology-learning algorithms that anticipate cost reductions based on cumulative installations.

Figure 1. Relationship to other NEMS Modules



Chapter 2: Model Rationale

Theoretical approach

The NEMS RDM is an integrated dynamic modeling system based on accounting principles and a representation of residential consumer economic behavior that generates projections of residential sector energy demand, appliance stocks, and market shares.

The RDM is a housing and equipment stock/flow model. The stock of housing units and the corresponding energy-consuming equipment are tracked for each year of the projection. The housing stock changes over time as houses are removed from the stock (demolished, retired, or converted) and new construction is added or converted to residential use. Similarly, the equipment stock changes each projection year as appliances fail and are replaced, through increases in the saturation of existing appliances, and as new technologies enter the market. Detailed subroutines provide the structure for computation of specific elements of the residential sector within the RDM.

Base-year information developed from the RECS microdata forms the foundation of equipment and housing stock. Market share information from RECS is used to estimate the number and type of replacements and additions to the equipment stock. The choice between the capital cost and the first year's operating cost determines the market share within a given service. Market shares are also modeled as functions of the corresponding fuel prices, expected level of equipment usage, and equipment efficiency characteristics.

Logistic or *logit* functions are used to estimate the market shares of competing technologies within each end-use service. Market shares are determined for both new construction equipment decisions and replacement equipment decisions. The Technology Choice Subroutine of the module considers the relative installed capital and operating costs of each equipment type within the logit function to calculate the market shares of the technology within the service, region, and housing type.

Only major end-use services with technology characterizations (i.e., space heating, space cooling, clothes washing, dishwashing, water heating, cooking, clothes drying, refrigeration, freezing, and lighting) use this approach. Because air-source and ground-source (also known as geothermal) heat pumps are used for both space heating and space cooling, heat pump market shares for space cooling are assigned from the heating choice calculations.

Unlike the major technology services, several miscellaneous electric loads (MELs) such as televisions and related equipment (set-top boxes, home theater systems, and DVD/VCR players), computers and related equipment (monitors, desktops, laptops, networking equipment), rechargeable electronics, ceiling fans, coffee makers, dehumidifiers, microwave ovens, pool heaters and pumps, home security systems, portable electric spas, and wine coolers are modeled with a different approach that does not consider investment parameters such as cost or efficiency.

Building shell integrity is also considered in the projection of end-use consumption. Building shell integrity in existing homes is sensitive to real price increases over base-year price levels for space conditioning fuels. Final residential sector energy consumption is determined as a function of the

equipment and housing stock, average unit energy consumption, weighted equipment characteristics, and building shell integrity improvements.

For new construction, market shares of building shell options are also determined using a similar logistic calculation. The shell options are linked to heating and cooling equipment, as building codes can be met with a combination of more-efficient equipment and structural options (like windows and insulation levels). These linked, minimum efficiencies for heating and cooling equipment in new construction can be increased, but not decreased.

General model assumptions

The RDM assumes that the residential sector has the following characteristics:

- The sector is bifurcated into two housing vintages: housing that existed in the base year and new construction built in years after the base year.
- Housing units are removed from the housing stock at a constant rate over time, based on an analysis of each building type's historical growth and housing starts.
- Some energy-consuming equipment is chosen based on its upfront cost compared to its
 operating costs (like water heaters and refrigerators) while some appliances are chosen based
 on factors not related to their energy consumption (such as security systems or coffee makers).
- Equipment lifetime is defined by Weibull shape parameters. These parameters are based on estimated lifetime ranges and are used to refine a linear decay function (similar to the linear decay function included in previous versions of the model).
- The equipment contained in a retiring housing structure is assumed to retire when the structure is removed from the housing stock. Zero salvage value for equipment is assumed.
- Projected new home heating fuel shares are based on the Census Bureau's new construction data and vary over time due to changes in life-cycle cost for each of the heating system types.
- The choice of fuel for water heating and cooking is largely dependent on the choice of heating fuel.
- The type of fuel used for cooking and water heating when replacing retiring equipment in singlefamily homes is based on an input percentage of those who may switch and a technology choice-switching algorithm. Replacements are with the same technology in multifamily and mobile homes.
- Space heaters, air conditioners, water heaters, cookstoves, and clothes dryers may be replaced (up to a user-specified percentage) with competing technologies in single-family homes.
 Switching is based on retail cost of new equipment and the cost of switching technologies.
- Building shell efficiency and heating, ventilation, and air conditioning (HVAC) systems for new housing stock are a function of the life-cycle cost of competing building shell and HVAC packages.
- A constant 1.2% share of existing housing is renovated each year, increasing the square footage of the conditioned (heated and cooled) living area by about one-third.
- The volumetric size of new construction is larger than existing homes, which increases the heating and cooling loads in new construction, all else equal. This assumption is based on a time-series analysis of RECS which shows increased floorspace per household over time, as well as increased prevalence of slightly higher ceilings.

Legislation-specific model assumptions

American Recovery and Reinvestment Act of 2009 (ARRA)

The ARRA legislation passed in February 2009 provides energy-efficiency funding for federal agencies, state energy programs, and block grants, as well as a sizable increase in funding for weatherization. To account for the impact of this funding, it is assumed that the total funding is aimed at increasing the efficiency of the existing housing stock. The assumptions regarding the energy savings for heating and cooling are based on evaluations of the impact of weatherization programs over time. Further, it is assumed that each house requires a \$2,600 investment to achieve the heating and cooling energy savings estimated in the evaluations, with a 20-year life expectancy of the measures.

Section 410 of ARRA provided states with funding under the condition that they adopt building codes that meet or exceed the 2009 International Energy Conservation Code (IECC), achieving 90% compliance by 2017. To represent this, new construction after 2017 is generally assumed to be built to at least IECC 2009 levels, although some Census divisions reach that level much earlier.

The ARRA provisions remove the cap on the 30% tax credit for ground-source heat pumps through 2016. Additionally, the cap for the tax credits for other energy-efficiency improvements, such as windows and efficient furnaces, was increased to \$1,500 through the end of 2010.

Successful deployment of smart grid projects based on ARRA funding could stimulate more rapid investment in smart grid technologies, especially smart meters on buildings and homes, which might make consumers more responsive to electricity price changes. To represent this, the price elasticity of demand for residential electricity was increased for the services that have the ability to alter energy intensity (e.g., lighting). The Tax Relief, Unemployment Insurance Reauthorization, and Job Creation Act of 2010 extended several ARRA tax credit provisions through 2011, often at reduced amounts.

Energy Independence and Security Act of 2007 (EISA)

The passage of the EISA in December 2007 provides additional minimum efficiency standards for various types of residential equipment. The standards contained in EISA include the following: a nearly-30% reduction in the wattage of general service lighting in 2012-2014 and about 65% reduction by 2020; boiler standards in 2012; wattage reductions for external power supplies after 2008; and standards for clothes washers, dishwashers, and dehumidifiers to be implemented between 2010 and 2012.

Energy Policy Act of 2005 (EPACT05) and Energy Improvement and Extension Act of 2008 (EIEA)

EPACT05 provided for additional minimum efficiency standards for residential equipment and provided tax credits to producers and purchasers of energy-efficient equipment and builders of energy-efficient homes. The standards contained in EPACT05 include the following: 190-watt maximum for torchiere lamps starting in 2006; dehumidifier standards starting in 2007 and 2012; and ceiling fan light kit standards starting in 2007. Producers of manufactured homes that were 30% more efficient than the latest code could claim a \$1,000 tax credit. Likewise, builders of homes that were 50% more efficient

¹ Oak Ridge National Laboratory, Estimating the National Effects of the U.S. Department of Energy's Weatherization Assistance Program with State-Level Data: A Metaevaluation Using Studies from 1993 to 2005, September 2005.

than the latest code could claim a \$2,000 credit. Production tax credits were assumed to be passed through to the consumer in the form of lower purchase cost. EPACT05 included production tax credits for energy-efficient refrigerators, dishwashers, and clothes washers, with dollar amounts varying by type of appliance and level of efficiency met, subject to annual caps. Consumers could claim a 10% tax credit for several types of appliances specified by EPACT05, including energy-efficient gas, propane, or distillate fuel oil furnaces or boilers, energy-efficient central air conditioners, air- and ground-source heat pumps, water heaters, and windows. Lastly, consumers could claim a 30% tax credit in 2006, 2007, and 2008 for purchases of solar photovoltaic (PV), solar water heaters, and fuel cells (subject to a \$2,000 cap).

EIEA extended the tax credits specified in EPACT05 through 2010. In addition, the \$2,000 cap for solar PV, solar water heaters, and fuel cells was removed, and the credit for ground-source heat pumps was increased to \$2,000.

Technology-specific modeling assumptions

The efficiency choices made for residential equipment are based on a log-linear function. The function assigns market shares for competing technologies based on the relative weights of capital/installed (first cost) and discounted operating (annual fuel) costs. A time-dependent log-linear function calculates the installed capital cost of equipment in new construction. Although not activated in most model runs, there is an option for price-induced technological change. Essentially, with this option, if fuel prices increase markedly and remain high over a multi-year period, more-efficient appliances will be available earlier in the projection period than they would have been otherwise.

Weather and climate adjustment

Space heating and air conditioning usage is adjusted across Census divisions by heating and cooling degree day factors to account for potential deviations relative to the temperatures (and their corresponding degree days) during the RECS survey period. Thirty years of historical heating and cooling degree days for each state are used to establish a linear trend of heating and cooling degree days at the state level. This 30-year trend informs the projection of state-level degree days, which are exogenously aggregated to the Census division level using state-level populations. Projected changes in degree days are thus intended to reflect projected shifts in population among states as well as continuing changes in historical degree day data.

Technology and fuel switching

Space heaters, air conditioners (heat pumps and central air conditioners), water heaters, cookstoves, and clothes dryers may be replaced with competing technologies in single-family homes. It is assumed that 20% of the replacement market in single-family homes is eligible to switch fuels in any projection year. The log-linear functional form is flexible to allow the user to specify parameters, such as weighted bias, retail equipment cost, and technology switching cost. Equipment in multifamily and mobile homes are replaced with the same technology.

Space cooling: room and central air conditioning units

Room and central air conditioning units are disaggregated based on existing housing data. The market penetration of room and central air systems by Census division and housing type, along with new

housing construction data, are used to determine the number of new units of each type. The penetration rate for central air conditioning is estimated by means of time series analysis of RECS data. Where room air conditioners are used, RECS also informs the number of room air conditioners per household in new construction.

Water heating: solar water heaters

Market shares for solar water heaters are tabulated from the RECS public use microdata. The module currently assumes that, in solar water heating systems, solar energy provides 50% of the energy needed to satisfy hot water demand, and an electric back-up unit satisfies the remaining 50%.

Refrigerators and freezers

The module assumes fixed overall shares for three types of refrigerator based on freezer orientation (top-mounted, side-mounted, or bottom-mounted freezer) and two types of freezer (upright and chest). Market shares were established based on RECS public use microdata.

Clothes dryers

The module currently assumes that clothes dryer market penetration increases over the projection period, with a terminal saturation level that is consistent with the market penetration of clothes washers. This assumption is based on analysis of RECS public use microdata.

Clothes washers

The module links clothes washer choice to the water heating service because many efficiency features for clothes washers act to reduce the demand for hot water.

Lighting

The module partitions lighting into four main categories of bulb type: general service, reflector, linear fluorescent, and exterior. Within the general service category, several *hours of use* bins further partition this category, allowing bulb choice to vary with the amount of time each fixture is used on an annual basis. The reflector, exterior, and linear fluorescent categories assume an average hours of use value for lamp choice purposes per DOE's 2010 U.S. Lighting Market Characterization report. Within an application such as general service lighting, a fixed light output level (measured in lumens) is used so that choices are among bulbs with similar light output.

Miscellaneous electric loads

The module uses exogenous expectations of saturation and per-unit consumption to form projections of the miscellaneous electric loads (MELs). Consumption projections for some of these MELs are also affected by projected changes in square footage and disposable income.

Furnace fans

The number of housing units that have fossil-fuel-fired central forced-air heating determines furnace fan energy consumption. The relative level of heating and cooling degree days also affects the amount of energy used for this service.

Secondary heating

The consumption of secondary heating fuels is determined based on the share of total housing that uses a secondary heating fuel multiplied by the UEC, adjusted for the shell integrity.

Other / Unspecified consumption

Even with the consumption information collected in RECS, there is consumption attributed to unspecified uses. Often these are aggregated as *other* uses.

Distributed generation

In single-family housing, adoption of solar photovoltaic systems, fuel cells, and small wind turbines for on-site electricity generation competes with purchased electricity to satisfy the home's electricity needs. Penetration is limited by factors outlined in the detailed description of the Distributed Generation Subroutine. The electricity generated from these systems is either used on-site or sold back to the grid.

Model Structure

Structural overview

The NEMS Residential Demand Module characterizes energy consumption using a series of algorithms that account for the stocks of housing and appliances, equipment market shares, and energy intensity. The module assesses the shifts of market shares between competing technologies based on fuel prices, equipment costs, and assumptions about the behavior of residential consumers.

The RDM is a sequential structured system of algorithms, with succeeding computations using the results from previously executed components as inputs. The module is composed of six components: housing stock projection, equipment technology choice, appliance stock projection, building shell integrity, distributed generation, and energy consumption.

Housing stock projection

The location and type of housing stock are the primary model drivers. The first component uses data from the NEMS Macroeconomic Activity Module to project new and existing housing for three dwelling types at the Census division level.

Equipment technology choice

The Technology Choice Component simulates the behavior of consumers by projecting market shares for each available equipment type. New and replacement equipment decisions are modeled for each technology type. For new construction, the home heating fuel is determined by the relative life-cycle costs of all competing heating systems.

Relative weights are determined for each equipment type based on the existing market share, the installed capital cost, and the operating cost. These relative weights are then used to compute the market shares and composite average efficiencies for each service listed in Table 3. The technologies are distinguished by the service demand that they satisfy, by the fuel that they consume, and by their energy efficiency.

Energy efficiency can be defined as the ratio of service demand to energy input. For relatively simple devices such as space heaters or light bulbs, service demand is a unit of heat or light, respectively, and thus efficiency is described in terms of heat per unit energy (such as coefficient of performance (COP) or annual fuel utilization efficiency (AFUE)) or light per unit energy (lumens per Watt).

For other equipment, service demand can be more difficult to quantify, or other factors beyond the primary service demand may contribute to a unit's energy consumption. In the case of refrigerators, the primary service demand is the volume of interior space refrigerated, but features such as an icemaker or through-the-door water dispenser can add to the unit's energy consumption (UEC). Another example is televisions, where service demand may be described as the area of the visual display, but other factors such as power draw in standby and off modes affect their consumption. For this reason, some equipment is described by a UEC (typically in units of kilowatt-hours per year) rather than an energy-efficiency metric.

Table 3. Services and equipment in NEMS Residential Demand Module

End-Use Equipment	Efficiency Metric
Space Heating	
Air-Source Heat Pump	Heating Seasonal Performance Factor (HSPF)
Electric Furnace	COP
Distillate Fuel Oil Boiler	Annual Fuel Utilization Efficiency (AFUE)
Distillate Fuel Oil Furnace	AFUE
Ground-Source Heat Pump	COP
Kerosene Furnace	AFUE
Liquefied Petroleum Gas (LPG) Furnace	AFUE
Natural Gas Boiler	AFUE
Natural Gas Furnace	AFUE
Natural Gas Heat Pump	COP
Wood Stove	COP
Air Conditioning	
Air-Source Heat Pump	Seasonal Energy Efficiency Ratio (SEER)
Central Air Conditioner	SEER
Ground-Source Heat Pump	Energy Efficiency Ratio (EER)
Natural Gas Heat Pump	COP
Room Air Conditioner	EER
Water Heating	
Electricity Water Heater	Energy Factor (EF)
Distillate Fuel Oil Water Heater	EF
LPG Water Heater	EF
Natural Gas Water Heater	EF
Solar Water Heater	EF
Cooking	
Electric Cookstove	kilowatt-hours per year (kWh/yr)
LPG Cookstove	Thermal Efficiency (Btu Out / Btu In)
Natural Gas Cookstove	Thermal Efficiency (Btu Out / Btu In)

Table 3. Services and equipment in NEMS Residential Demand Module (continued)

End-Use Equipment	Efficiency Metric
Clothes Drying	
Electric Clothes Dryer	EF
Natural Gas Clothes Dryer	EF
Clothes Washing	
Clothes Washer	kWh / cycle (motor), Modified Energy Factor (MEF), Water Factor (WF)
Dishwashing	
Dishwasher	EF, WF
Refrigeration	
Refrigerator w/ top freezer (21 cubic foot capacity)	kWh / yr
Refrigerator w/ side freezer (26 cubic foot capacity)	kWh / yr
Refrigerator w/ bottom freezer (25 cubic foot capacity)	kWh / yr
Freezing	
Chest Freezer (15 cubic foot capacity)	kWh / yr
Upright Freezer (automatic defrost, 20 cubic foot capacity)	kWh / yr
Lighting	
General Service – Compact Fluorescent Lamp (CFL)	Watts (for an assumed lumen level)
General Service – Incandescent and Halogen	Watts (for an assumed lumen level)
General Service – Light-Emitting Diode (LED)	Watts (for an assumed lumen level)
Linear Fluorescent (T12)	Watts (for an assumed lumen level)
Linear Fluorescent (T8)	Watts (for an assumed lumen level)
Linear Fluorescent (LED)	Watts (for an assumed lumen level)
Reflector (Incandescent)	Watts (for an assumed lumen level)
Reflector (Halogen)	Watts (for an assumed lumen level)
Reflector (CFL)	Watts (for an assumed lumen level)
Reflector (LED)	Watts (for an assumed lumen level)
Exterior (Incandescent)	Watts (for an assumed lumen level)
Exterior (Halogen)	Watts (for an assumed lumen level)
Exterior (LED)	Watts (for an assumed lumen level)
Exterior (High Pressure Sodium)	Watts (for an assumed lumen level)

Table 3. Services and equipment in NEMS Residential Demand Module (continued)

End-Use Equipment	Efficiency Metric
Televisions and Related Equipment	
Televisions	kWh / yr
Set-top Boxes	kWh / yr
Video Game Consoles	kWh / yr
Home Theater Systems	kWh / yr
DVD / VCR players	kWh / yr
Personal Computers and Related Equipment	
Desktops	kWh / yr
Laptops	kWh / yr
Monitors	kWh / yr
Networking Equipment (modems and routers)	kWh / yr
Secondary Heat	
Coal	MMBtu / yr
Distillate Fuel Oil	MMBtu / yr
Electric	MMBtu / yr
Gas	MMBtu / yr
Kerosene	MMBtu / yr
LPG	MMBtu / yr
Wood	MMBtu / yr
Furnace Fans and Boiler Circulation Pumps	
Furnace fans	kWh / yr
Other Uses	
Ceiling Fans	kWh / yr
Coffee Makers	kWh / yr
Dehumidifiers	kWh / yr
Microwaves	kWh / yr
Pool Heaters & Pumps	kWh / yr
Portable Electric Spas	kWh / yr
Rechargeable Electronics	kWh / yr
Security System	kWh / yr
Wine Coolers	kWh/ yr
Unspecified: Distillate Fuel Oil	MMBtu / yr
Unspecified: Electric	MMBtu / yr
Unspecified: Natural Gas	MMBtu / yr
Unspecified: LPG	MMBtu / yr
Distributed Generation	
Solar Photovoltaic	Electrical Efficiency
Fuel Cell	Electrical Efficiency
Small Wind Turbine	Electrical Efficiency

Appliance stock projection

The appliance stock component of the module projects the number of end-use appliances within all occupied housing units. This component tracks equipment additions and replacements.

Building shell integrity

Building shell integrity is modeled for existing and new housing. The existing housing stock responds to rising prices of space conditioning fuels by improving shell integrity. Shell integrity improvements might range from relatively inexpensive measures (such as caulking and weather-stripping) to projects with substantial costs (such as window replacement). These improvements exhibit a one-way price response: more measures are installed as prices increase, but those measures are not undone when prices fall.

New housing stock also incorporates shell integrity improvements. The shell integrity of new housing is a function of capital and operating costs for several levels of total system efficiency. New housing stock includes homes that meet the 2009 International Energy Conservation Code (IECC), those that meet ENERGY STAR criteria, those that qualify for federal tax credits for efficient shells, and those that include the most efficient commercially available building shell components, as well as some non-codecompliant homes.

Distributed generation component

The distributed generation component allows adoption of solar photovoltaic, fuel cells, and small wind turbine systems for on-site generation to compete with purchased electricity for satisfying electricity needs. Through the use of a ZIP code-level hurdle model² (solar photovoltaics) and a cash-flow formulation (fuel cells and wind), the penetration rates of these systems are projected. Electricity generated from these systems is deducted from total housing unit use, or sold back to the grid, if feasible.

Energy consumption

The energy consumption component calculates end-use consumption for each service and fuel type. The consumption projections are constructed as products of the number of units in the equipment stock and the average technology unit energy consumption (UEC). The average UEC changes as the composition of the equipment stock changes over time. For each year of the projection, the following steps are performed to develop the projection of energy consumption:

- 1. A projection of housing stock is generated based on the retirement of existing housing stock and the addition of new construction as determined in the Macroeconomic Activity Module.
- 2. Base-year equipment stock is estimated, accounting for housing demolitions and additions.
- 3. Market shares are determined for equipment types and efficiencies by service.
- 4. The previous year's equipment additions and replacements for both existing homes and new construction vintages are determined based on the current-year market share.
- 5. Efficiencies weighted by market share are calculated.
- 6. Fuel consumption is calculated using UEC and the weighted efficiencies. Consumption can also vary based on projected heating and cooling shell integrities, fuel prices, personal disposable income, housing unit sizes, and weather as applicable to specific equipment and end-use services.

² The solar photovoltaic ZIP code-level hurdle model was included in NEMS for AEO2016 but not turned on until AEO2017. The cash flow model was used for solar penetration in AEO2016 and is still an option for AEO2017 onward.

Fortran subroutine descriptions

The NEMS Residential Demand Module Fortran source code consists of more than 50 subroutines sequentially called during the execution of the module. Table 4 lists the major subroutines and their corresponding descriptions. The subroutines can be grouped into the following 13 categories according to their functions:

Fuel Price Subroutine (1 subroutine)

RDPR reads in fuel prices from NEMS

Initialization Subroutine (1 subroutine)

INTEQT initializes heating equipment market shares and applies the decay rate to the

existing equipment

Housing Subroutine (1 subroutine)

NEWHSE reads housing starts from NEMS Macroeconomic Activity Module and computes

new housing stock

Existing Equipment Subroutine (1 subroutine)

RDHTRTEC projects existing vintage equipment by service. In this subroutine,

the following operations are performed:

- 1. Read equipment market share from an input file by equipment type, housing type, and Census division.
- 2. Calculate the base-year equipment stock or the existing vintage stock as the product of the share and the number of existing housing units.
- 3. Project surviving equipment of the existing vintage using the equipment survival rate and the housing decay rate for every year in the projection.

Other Input Subroutines (11 subroutines)

These subroutines read other information from files:

RDSTEFF reads efficiencies of base-year stock equipment

RDEFF reads efficiencies of retiring equipment **RDRET** reads equipment retirement rates

RDESTARHOMES reads historical ENERGY STAR home percentages
RTEKREAD reads the detailed technology data for equipment
RTEKREAD1 reads the detailed technology data for building shells

RDSQFT reads home square footage data

RDUECS reads unit energy consumption data for equipment

BLDBASEREAD reads baseline electricity consumption for energy efficiency program calculations

RSUECSHLREAD reads unit energy consumption data for building envelopes

RSMELSREAD reads miscellaneous electric load data **RSSWITCHREAD** reads fuel and equipment switching data

RSMLGTREAD reads lighting technology data

DEGDAYREAD reads degree day data

RSMISCREAD reads miscellaneous variables

Calculation Subroutines (2 subroutines)

The model includes a subroutine SQFTCALC to calculate average home floor areas for new and existing houses and compute size and volume effects for new construction. The subroutine PITC calculates the amount of price-induced technology change based on fuel prices.

Technology Choice - TEC Subroutines (10 subroutines)

The code includes 10 technology choice subroutines that follow these general steps:

- 1. Initialize capital costs and equipment efficiencies.
- 2. Set discount rate, adjustment factors, and present value horizon.
- 3. Compute operating costs of each equipment type.
- 4. Compute life-cycle costs of each equipment type.
- 5. Compute technology share for new housing.
- 6. Calculate new and replacement equipment weights based on the bias, capital cost, and operating costs using a log-linear function.
- 7. Compute new market shares, ratio between equipment weights and total equipment weight.
- 8. Calculate efficiencies for new and replacement equipment types weighted by their respective market shares.

These subroutines are as follows:

RSHVAC	RHTRTEC	RCLTEC	RWHTEC	RSTVTEC
RDRYTEC	RREFTEC	RFRZTEC	RCWTEC	RDWTEC

Replacements and Additions - ADD Subroutines (8 subroutines)

The code contains eight equipment replacement and additions subroutines (water heaters and cookstoves use the same ADD subroutine). TEC subroutines for each service are followed by ADD subroutines that calculate new and replacement equipment for the previous year based on the current year's market share. The following steps are implemented in these subroutines:

- 1. Determine new construction vintage equipment additions based on the estimated share (from the MAM) of new houses that demand that service.
- 2. Compute the surviving new vintage equipment in existing vintage houses.
- 3. Compute total equipment required for existing vintage houses.
- 4. Compute the equipment replacements in existing vintage houses by subtracting the sum of surviving existing-vintage equipment and surviving new-vintage equipment in existing-vintage houses from the total equipment demanded for existing-vintage houses. Technology switching is allowed at

- replacement for space heaters, heat pumps and central air conditioners, water heaters, cookstoves, and clothes dryers in single-family homes.
- 5. Compute the surviving new-vintage equipment that was purchased as either additions or replacements for new houses.
- 6. Calculate the current year's replacements of new-vintage equipment in new houses by subtracting the surviving replacements and equipment additions in new houses from the stock of surviving new houses. Technology switching is allowed at replacement for space heaters, heat pumps and central air conditioners, water heaters, cookstoves, and clothes dryers in single-family homes.

These subroutines are as follows:

RHTRADD	RCLADD	REUADD	RDRYADD	RREFADD
RFRZADD	RCWADD	RDWADD		

End-Use Consumption - CON/CNS Subroutines (15 subroutines)

The 15 end-use consumption subroutines are defined by service. The ADD subroutines are followed by consumption subroutines. Within each of these subroutines the new, replacement and average unit energy consumption values are calculated. These UECs are then multiplied by the equipment stock (and climate adjustment factor and shell integrity for space conditioning) to yield final fuel consumption. These subroutines, which follow, also include a price-sensitivity expression that adjusts short-term demand for fuels:

RHTRCON	RCLCON	RWHCON	RSTVCON	RDRYCON
RREFCON	RFRZCON	LTCNS	APCNS	SHTCNS
APPCNS	RCWCON	RDWCON	TVCNS	PCCNS

Distributed Generation (1 subroutine)

RDISTGEN projects the number of housing units with distributed generation technologies;

calculates amount of distributed capacity; and estimates electricity generated

both for own use and for sale to the grid (reported to NEMS EMM).

Overall Consumption - CN Subroutines (2 subroutines)

The model includes the following two subroutines that calculate overall fuel consumption and list output NEMS consumption:

FUELCN calculates fuel consumption

NEMSCN writes out NEMS consumption

Historical Consumption/Calibration Subroutines (2 subroutines)

EXCONS calculates base-year consumption

RSBENCH calibrates consumption to historical and near-term forecast consumption

Energy Efficiency Program Impacts (1 subroutine)

CALC111D

calculates incremental electricity consumption between an integrated NEMS model run that includes energy efficiency rebates and one in which no rebates are included; aggregates regional subsidies for major end-use and distributed generation equipment; and estimates energy efficiency program overhead costs; all outputs are sent to EMM of NEMS

Report Subroutines (4 subroutines)

RESDRP aggregates consumption by end use for NEMS reports

RESDRP2 provides diagnostic reports for internal use

RESDBOUT provides diagnostic reports for internal use

NHTSHR prepares new heating system shares report

Table 4. Primary NEMS Residential Demand Module Subroutines

Subroutine Name	Description of the Subroutine
RTEKREAD	Read technological characterizations for all equipment
RTEKREAD1	Read technological characterizations for building shells
RDSQFT	Read annual average housing floor areas
RSMISCREAD	Read miscellaneous data for the module
RDPR	Read prices
PITCINIT	Initialize values for price-induced technology change
RSPITC	Compute price-induced technology change
INTEQT	Initialize heating equipment market share
RDHTRTEC	Project base-year vintage for all services
RDUECS	Initialize equipment UECs (service aggregates)
RCONSFL	Rationalize fuel numbering among equipment types
EXCONS	Calculate base-year consumption
RDISTGEN	Project distributed generation penetration
NEWHSE	Calculate new housing
SQFTCALC	Calculate average floor area of housing
RDSTEFF	Read in efficiency of equipment from base-year stock
RDEFF	Read in efficiency of retiring equipment from base-year stock
RDRET	Read in proportion of retiring equipment from base-year stock
RDESTARHOMES	Read in historical ENERGY STAR home shares
RSUECSHLREAD	Read in unit energy consumption data for building envelopes
RSMELSREAD	Read in miscellaneous electric load data
RSSWITCHREAD	Read in fuel-switching and equipment-switching parameters
RSMLGTREAD	Read in lighting technology data
DEGDAYREAD	Read in degree day data
BLDBASEREAD	Read in baseline electricity consumption for energy efficiency program impact calculations
REPLACE	Share out replacement equipment switching among competing
	technologies for single-family homes up to an input limit
RCWTEC	Choose clothes washing equipment
RCWADD	Calculate new and replacement clothes washing
RCWCON	Calculate consumption for clothes washing
RDWTEC	Choose dishwashing equipment
RDWADD	Calculate new and replacement dishwashers
RDWCON	Calculate consumption for dishwashing
PCCNS	Calculate personal computer and related equipment consumption
TVCNS	Calculate television, set-top box, and video game console consumption
RWHTEC	Choose water heating equipment
REUADD	Calculate new and replacement water heaters and cookstoves
RWHCON	Calculate consumption for water heating

Table 4. Primary NEMS Residential Demand Module Subroutines (continued)

Subroutine Name	Description of the Subroutine
RSTVTEC	Choose cooking equipment
RSTVCON	Calculate consumption for cooking
RDRYTEC	Choose clothes dryer equipment
RDRYADD	Calculate new and replacement clothes dryers
RDRYCON	Calculate consumption for clothes dryers
RSHVAC	Choose HVAC equipment and shell characteristics for new homes
RHTRTEC	Choose heating equipment and compute average efficiencies
RHTRADD	Calculate new and replacement heating equipment
RHTRCON	Calculate heating consumption
RCLTEC	Choose cooling equipment
RCLADD	Calculate new and replacement cooling equipment
RCLCON	Calculate cooling consumption
RREFTEC	Choose refrigeration equipment
RREFADD	Calculate new and replacement refrigerators
RREFCON	Calculate energy consumption for refrigeration
RFRZTEC	Choose freezing equipment
RFRZADD	Calculate new and replacement freezing equipment
RFRZCON	Calculate consumption by freezers
LTCNS	Calculate lighting stock, efficiency, and consumption
APCNS	Calculate consumption for electric appliances
SHTCNS	Calculate consumption for secondary heating
APPCNS	Calculate appliance consumption
NHTSHR	Prepare new home heating system shares report
FUELCN	Calculate fuel consumption
RSBENCH	Calibrate consumption to benchmark values
NEMSCN	Calculate and report NEMS output variables
RESDBOUT	Prepare residential output database file
CALC111D	Calculates energy efficiency program costs and energy savings
RESDRP	Prepare data for reporting
RESDRP2	Report module results

Appendix A: Input Parameters

Residential Demand Module input data files

For AEO2013, several input files were renamed for consistency and/or reorganized based on their function. With this convention, all residential input files begin with the letters *rs*, with the exception of KDEGDAY, which is shared with the commercial module.

AEO2012 and prior	AEO2013 and subsequent
Unchanged files	
RSSTEO	RSSTEO
RSEFF01	RSEFF01
RSRET01	RSRET01
RSSTKEFF	RSSTKEFF
Renamed files	
RGENTK ³	RSGENTK
RSEQP93	RSSTK
RSSQRFT	RSSQFT
RSUEC10	RSUEC
RSUEC11	RSESTAR
RTEKCL	RSCLASS
RTEKTY	RSMEQP
RTEKTYC	RSMSHL
Combined files	
RSHTSHR	RSHTSHR
RSHTSH95	
Separated files	
RMISC	RSMLGT
	RSSWITCH
	RSMELS
	RSUECSHL
	RSMISC
Files in common with other mod	dules
RMISC (degree day arrays)	KDEGDAY

³ The unused RGENTK was repurposed starting with AEO2016 to contain ZIP code-level solar photovoltaic penetration input data.

Residential Technology Class Description

File: RSCLASS.TXT (formerly RTEKCL.TXT)

Source: RECS

Units: See discussion of individual variables below.

Comments: This file provides various pointers used throughout the module to coordinate and

allocate the number of equipment types within an end use, as well as overarching

parameters such as equipment life functions and choice parameters.

Variables:

RTCLENDUea End use number. Matches RTTYENDUes in the RSMEQP.TXT input file. Equipment classes

having the same end use compete with one another. The RDM allocates equipment

among them in the technology choice process.

1=Space Heating

2=Space Cooling

3=Clothes Washing

4=Dishwashing

5=Water Heating

6=Cooking

7=Clothes Drying

8=Refrigeration

9=Freezing

RTCLEQCL_{eq} Equipment class number. Appears on all records. Matches RTTYEQCL_{es} in

the RSMEQP.TXT file for one or more equipment types; there are one or

more equipment types in RSMEQP.TXT for each class in RSCLASS.

RTCLTYPT_{eg} Required pointer from equipment class to a representative equipment

type. This is the only pointer from RSCLASS to RSMEQP.TXT. This pointer selects the equipment type used in determining the equipment class for newly constructed housing units and replacement equipment class in single-family houses. Its value is the $RTEQTYPE_{es}$ in RSMEQP.TXT of

the representative equipment.

 $RTCLPNTR_{eq}$ Class pointer. Required for end uses 1, 2, and 5; otherwise, equals 0.

If end use = 1: Required pointer from space heater class to associated water heater class linking water heater fuel choice to space heater fuel choice for newly constructed

housing units.

If end use = 2: Required pointer from cooling heat pump class to same class of heating

heat pump.

0 = Not a heat pump

Integer = Heater heat pump class number

If end use = 5: Required pointer from water heater class to matching cooking class linking cooking fuel choice to water heater fuel choice for newly constructed housing units. Also see $RTCLREPL_{eg}$ end use 5 (water heating) below; only natural gas water heaters may point to two types of cookstoves.

 $RTCLREPL_{eq}$ Replacement class. Required for end uses 1 and 5; zero otherwise.

If end use = 1: Flag for replacing the existing space heater class with a natural gas forced air space heater at retirement.

If end use = 5: Second pointer from natural gas water heater class to matching cooking class. The model assumes that 44% of new single-family homes, 15% of new multifamily homes, and 100% of new mobile homes with natural gas water heaters have natural gas cookstoves and the remainder have electric cookstoves.

RTFUEL_{eg} Fuel used by this equipment (Table 2)

 $RTMAJORF_{eg}$ Major fuel flag. Used only for end use (RTCLENDU) 1, space heating; zero otherwise. Space heater shares for systems using major fuels are calculated differently from space heater shares for systems using minor fuels. Set to 1 to indicate a major fuel, which applies to all modeled space heating equipment. Set to 0 to indicate a minor fuel. Not

currently used in RDM.

RTFFAN_{eg} Furnace fan flag. Value of 1 assigns use of a furnace fan with respective central

heating/cooling technology; zero otherwise.

RTBASEFF_{eq} Base efficiency for this equipment class. Defined differently for different end uses:

End uses 1, 2, 4, 5, 7: base efficiency for this equipment class.

End uses 3, 6, 8, 9: intensity for this equipment class.

RTALPHA_{eq} Equipment life parameter alpha (α) for exponential decay.

RTMINLIF_{eq} Minimum life of this equipment class (years). Not used by the model, but retained here

for informational purposes.

RTMAXLIF_{eq} Maximum life of this equipment class (years). Not used by the model, but retained here

for informational purposes.

 RTK_{eq} Equipment life Weibull distribution shape parameter k.

RTLAMBDA_{ea} Equipment life Weibull distribution scale parameter lambda (λ).

RTFCBETA_{eq} New home heating technology choice model log-linear parameter beta (β). Used only

for end use 1; zero otherwise.

RTSWFACT_{eq} Maximum fraction of single-family homes which may switch away from specified

equipment class on replacement.

RTSWBETA_{eq} Replacement technology choice model log-linear parameter beta (β). Used only for

single-family homes.

RTSWBIAS_{eq} Replacement technology choice model bias parameter. Used only for single-family

homes.

RTCLNAME_{eq} Unique name for each equipment class.

Base-year Equipment Stock

File: RSSTK.TXT (formerly RSEQP93.TXT)

Sources: RECS; Analysis and Representation of Miscellaneous Electric Loads in NEMS, Navigant

Consulting, Inc. and SAIC

Units: Number of units (e.g. number of refrigerators, number of televisions, etc).

Comments: Each value represents values from RECS public use microdata, aggregated to the Census

division and building type level.

Variables: *EQCESE*_{baseyr,eq,b,r}

Equipment Classes Included:

Space Heaters: Electric Furnace	Furnace Fans
Space Heaters: Air-Source Heat Pump	Televisions
Space Heaters: Natural Gas Furnace	Set-Top Boxes
Space Heaters: Natural Gas Boiler/Radiator	Home Theater Systems
Space Heaters: Kerosene Furnace	DVD Players
Space Heaters: LPG Furnace	Video Game Consoles
Space Heaters: Distillate Fuel Oil Furnace	PC Desktops
Space Heaters: Distillate Fuel Oil Other	PC Laptops
Space Heaters: Wood Stoves	PC Monitors
Space Heaters: Ground-Source Heat Pump	Network Equipment
Space Heaters: Natural Gas Heat Pump	Rechargeable Devices
Space Coolers: Room Air Conditioner	Ceiling Fans
Space Coolers: Central Air Conditioner	Coffee Machines
Space Coolers: Air-Source Heat Pump	Dehumidifiers
Space Coolers: Ground-Source Heat Pump	Microwaves
Space Coolers: Natural Gas Heat Pump	Pool Heaters and Pumps
Clothes Washers	Security Systems
Dishwashers	Spas
Water Heaters: Natural Gas	Wine Coolers
Water Heaters: Electric	Secondary Heaters: Natural Gas
Water Heaters: Distillate Fuel Oil	Secondary Heaters: Electric

Water Heaters: LPG	Secondary Heaters: Distillate Fuel Oil
Water Heaters: Solar	Secondary Heaters: LPG
Cookstoves: Natural Gas	Secondary Heaters: Kerosene
Cookstoves: LPG	Secondary Heaters: Wood
Cookstoves: Electric	Appliances: Electric
Clothes Dryers: Natural Gas	Appliances: Natural Gas
Clothes Dryers: Electric	Appliances: LPG
Refrigerators	Appliances: Distillate Fuel Oil
Freezers	

Base-year Unit Energy Consumption

File: RSUEC.TXT (formerly RSUEC10.TXT)

Sources: RECS; Updated Buildings Sector Appliance and Equipment Costs and Efficiency, Navigant

Consulting, Inc. and SAIC; Analysis and Representation of Miscellaneous Electric Loads in

NEMS, Navigant Consulting, Inc. and SAIC

Units: Per-unit energy consumption (MMBtu/unit/year or MMBtu/household/year)

Definition: Unit Energy Consumption (UEC) for all residential equipment classes and building types

in each Census division. The equipment classes are the same as those listed in the

previous section for the stock of existing equipment (RSSTK.TXT).

Comments: For space heating, space cooling, and water heating, each value represents per-unit

consumption data from RECS public use microdata, aggregated to the Census division and building type level. Other end uses are informed by several sources. The inputs are

structured the same as the Base-year Equipment Stock file described above.

Variables: EQCUEC baseyr,eg,b,r

Equipment classes included: Same as those in the *Base-year Equipment Stock* described above.

Square Footage

File: RSSQFT.TXT (formerly RSSQRFT.TXT)

Source: Multiple RECS; U.S. Census Bureau, Survey of Construction (SOC) (formerly

Characteristics of New Housing/C25).

Units: Square feet per housing unit

Comments: Average of floor space in residential buildings in each housing type, for each division,

from the base year to the projection horizon. Values after the last data year are based

on an exogenous projection derived from Census data.

Variables: *SQRFOOT*_{y,b,d}

Stock Equipment Efficiencies

File: RSSTKEFF.TXT

Source: Exogenous vintaging models developed based on shipment data.

Units: Dimensionless (energy out/energy in) except refrigerators, freezers, and cookstoves.

Comments: Values in this file give the average efficiencies of equipment remaining from the base-

year stock expected to be retired in each year. They are calculated in an external

spreadsheet that vintages efficiencies from the shipment data.

Variables: BASEFF_{y,eq}

Equipment classes included:

Electric Furnaces

Air-Source Heat Pumps (heating)

Natural Gas Furnaces Natural Gas Other Kerosene Furnaces

LPG Furnaces

Distillate Fuel Oil Furnaces Distillate Fuel Oil Other

Wood Stoves

Ground-Source Heat Pumps (heating) Natural Gas Heat Pumps (heating)

Room Air Conditioners
Central Air Conditioners

Air-Source Heat Pumps (cooling)
Ground-Source Heat Pumps (cooling)
Natural Gas Heat Pumps (cooling)

Clothes Washers Dishwashers

Natural Gas Water Heaters

Electric Water Heaters

Distillate Fuel Oil Water Heaters

LPG Water Heaters Solar Water Heaters Natural Gas Stoves

LPG Stoves Electric Stoves Natural Gas Dryers Electric Dryers Refrigerators Freezers

Stock Equipment Retired Fraction

File: RSRET01.TXT

Source: Exogenous vintaging models developed based on shipment data.

Units: Dimensionless (units retired to date/units extant in the base year).

Comments: Values in this file give the fraction of base-year equipment stocks expected to be retired

as of each year. They are calculated in an external spreadsheet that vintages efficiencies from the shipment data. Equipment classes included are the same as those described in

the Stock Equipment Efficiencies file described above.

Variables: $EQCRET_{y,eg}$

Stock Equipment Retired Efficiencies

File: RSEFF01.TXT

Source: Exogenous vintaging models developed based on shipment data.

Units: Dimensionless (energy out/energy in) except refrigerators, freezers, and cookstoves.

Comments: Values in this file give the average efficiencies of base-year equipment stock expected to

be retired as of each year. They are calculated in an external spreadsheet that vintages efficiencies from the shipment data. Equipment classes included are the same as those

described in the Stock Equipment Efficiencies file described above.

Variables: *EQCEFF*_{y,eg}

Heating Shares in New Construction

File: RSHTSHR.TXT (also incorporates the former file RSHTSH95.TXT)

Source: U.S. Census Bureau, Survey of Construction (SOC) (formerly Characteristics of New

Housing/C25).

Units: Fraction of purchases

Comments: Market share of general space heating equipment for new homes in the base year and

benchmarked years. This file provides the share of each equipment class by building type and Census division. Equipment classes included are the same as those described in the *Base-year Equipment Stock* file described above, but limited to heating equipment.

Variables: HSYSSHR_{y,eg,b,r}

Major end-use technology menu (except lighting)

File: RSMEQP.TXT (formerly RTEKTY.TXT)

Source: RECS; Updated Buildings Sector Appliance and Equipment Costs and Efficiency, Navigant

Consulting, Inc. and SAIC; multiple Technical Support Documents of DOE Appliance

Standard Rulemakings.

Units: Discussed for each variable.

Comments: Each line of this data file gives the important user-modifiable parameters for one

equipment type. Used by the RDM for allocating equipment choice among the individual

equipment types.

Variables:

RTEKDOLLARYR Dollar year of equipment costs, based on source data.

RTTYENDU_{es} End use number as in RSCLASS. Matches RTCLENDU in the RSCLASS.TXT input file.

RTTYEQCLes Equipment class for this equipment type. Must match a class number, RTCLEQCLeq, in

the RSCLASS file.

RTEQTYPE_{es} Equipment type number. Each equipment class may include multiple types. Each

equipment type may have up to one record for each year of the projection period (years must not overlap). The user may add equipment types to existing classes. When adding

RTTYPNTR pointer for cooling and the RTCLTYPT pointer in the RSCLASS file for heating. If adding heat pump types, add same type to both space heating and space cooling and

new types, update the type numbers for the rest of that end use; also, adjust the

adjust pointers.

RTINITYRes Initial calendar year for this model of this equipment type. The first RTINITYRes for a

model within a type should be the NEMS residential demand module base year;

subsequent initial years for a model must be previous RTLASTYR_{es}+1.

 $RTLASTYR_{es}$ Last calendar year for this model of this equipment type. Must be greater than or equal

to RTINITYRes for this model; final RTLASTYRes should be year of the projection horizon.

RTCENDIV Census division, as numbered in the geographic description section

HVACPT Pointer to identify the unique HVAC system number.

RTTYPNTR_{es} Required pointer from cooling heat pump type to same type of heating heat pump. Also

used as a flag to mark room air conditioners and central air conditioners. Used by end

use 2 only; zero otherwise. Modify as follows only if heat pumps added:

-1 = Room air conditioner

0 = Central air conditioner (not heat pump)

Other Integer = Matching heater heat pump HVAC system number

CWMEF_{es} Modified energy factor (MEF). Used only for clothes washers.

LOADADJes Proportion of water heating load affected by efficiency gains in end uses 3 and 4

(clothes washing and dishwashing, respectively).

RTEQEFF_{es} Defined differently for different end uses, but with the same approach as RTBASEFF_{eg}:

If end use = 1, 2, 4, 5, 7: Equipment efficiency (AFUE, COP, etc.)

If end use = 3, 6, 8, 9: Energy consumption (e.g., annual kWh consumption for

refrigerators).

RTEQCOST_{es} Installed capital cost per unit.

 $RTRECOST_{es}$ Retail capital cost per unit.

SUBREPL_{es} Federal subsidy/ rebate per installed unit.

SUBNEWes Federal subsidy/ rebate per replacement unit.

S111DREPL_{es} Utility subsidy/ rebate per installed unit.

S111DNEW_{es} Utility subsidy/ rebate per replacement unit.

RTMATURE_{es} Technology maturity description.

MATURE = No further cost reductions expected; used above constants for installed

wholesale and retail capital costs.

ADOLESCENT = Main cost reductions occurred before 1993; function EQCOST reduces installed wholesale and retail capital cost with 1993 (or first year of availability) as the

inflection point.

INFANT = All cost reductions expected after first year of availability; function *EQCOST* reduces installed wholesale and retail capital cost with the inflection point in the future.

RTCOSTP1_{es} If MATURE technology, not used.

If ADOLESCENT technology, representative year cost decline began (y₁ in code).

If *INFANT* technology, year of inflection of cost trend (y₀ in code).

RTCOSTP2_{es} If MATURE technology, not used.

If ADOLESCENT or INFANT technology, logistic curve shape parameter (gamma in

code).

RTCOSTP3_{es} If MATURE technology, not used.

If ADOLESCENT technology, total possible proportional decline in equipment cost from

 y_0 onward (d in code).

If INFANT technology, total possible proportional decline in equipment cost from y₁

onward (d in code).

RTECBTA1_{es} Efficiency choice model log-linear parameter β_1 , weights capital cost.

RTECBTA2_{es} Efficiency choice model log-linear parameter β_2 , weights fuel cost.

RTECBTA3_{es} Efficiency choice model log-linear parameter β_3 , weights life-cycle cost.

RTECBIAS_{es} Efficiency choice model, consumer preference log-linear parameter.

 $RTTYNAME_{es}$ Unique name for each equipment type.

Lighting technology menu

File: RSMLGT.TXT (formerly part of RMISC.TXT)

Source: RECS; Updated Buildings Sector Appliance and Equipment Costs and Efficiency, Navigant

Consulting, Inc. and SAIC; DOE Lighting Market Characterization; multiple DOE Solid-

State Lighting Program reports.

Units: Index values; discussed for each variable.

Comments: Unlike other end uses and equipment types, characterizing lighting equipment stock and

consumption requires time intervals measured in hours rather than years. Furthermore, there are multiple applications of lighting technologies (general service, reflector, linear

fluorescent, and exterior), that have different usage profiles.

Variables:

General lighting control variables:

RLGTDOLLARYR Dollar year of bulb costs, based on source data.

NumApps Number of lighting applications modeled.

 $AppID_{app}$ A three-character variable denoting the application name:

General service lighting (GSL)

Reflector (REF)

Linear fluorescent (LFL)

Exterior (EXT)

AppIndex_{app} Numerical order of the application

*NumTypes*_{app} Number of bulb types modeled per application

*NumBins*_{app} Number of hour-of-use bins modeled per application (maximum 6)

Lighting cost and performance data includes one record for each bulb modeled, with each row containing the following variables. The number of data records is allowed to vary (terminated by FirstYear = 9999), with requirements that each application must include bulbs for all lighting types for that application covering all modeled years from the base year through the projection horizon.

First year bulb is available.

Last year bulb is available.

BulbCost Cost per bulb.

BulbSub Subsidy/ rebate per bulb. Nine columns correspond to the nine U.S. Census divisions

shown in Table 1.

LPW Lumens per Watt efficacy of bulb.

BulbWatts Number of Watts bulb consumes.

LifeHours Service life in hours-of-use for bulb.

BulbCRI The color rendering index (CRI) for bulb. 100 for full-spectrum incandescent lighting,

lower for other bulb types (e.g., an LED may have a CRI value of 80)

LightingApp A three-character variable that matches the AppID for which bulb is being characterized.

BulbType A three-character variable that defines the bulb type:

Incandescent/halogen incandescent (INC)

Compact Fluorescent Lamp (CFL)

Light-emitting diode (LED)

Characterization of base-year bulb stocks (one record for each application) with stocks for each of the residential housing types (*ht*) modeled (single-family, multifamily, and mobile homes):

BulbsPerHH_{app,ht} Number of bulbs per household

Data characterizing base-year bulb usage for each application by hours-of-use bin, grouped by application:

AppBinHours_{app,bin} Daily hours-of-use for application in each hours-of-use bin

BinShares_{app,bin} Shares of bulbs for application by bin (must add to 100%)

BulbBinShares_{app,e,bin} Within bins, bulb shares by bulb type *e* for each application.

BaseWattsBulbs_{app,e} Base-year Watts for each of the bulb types used for this application.

Choice parameters:

 β_1 The choice parameter that applies to capital cost

 β_2 The choice parameter that applies to operating cost

Building shell technology menu

File: RSMSHL.TXT (formerly RTEKTYC.TXT)

Source: Exogenous modeling of housing units using REMDesign software.

Definition: HVAC technology data for new homes.

Units: Discussed for each variable.

Comments: Each of the lines of this data file gives the important user-modifiable parameters for

HVAC equipment in new homes.

Variables:

RSHLDOLLARYR Dollar year of shell costs, based on source data.

RSCENDIV Census division number (1-9).

RSBTYPE Building type number (1-3).

HVAC heating equipment class. Same as the RTCLTYPT pointer in the RSCLASS.TXT file

for heating.

HVHTEQTY HVAC heating equipment type. Same as the RTEQTYPE variable in the RSMEQP.TXT file

for heating.

HVCLEQCL HVAC cooling equipment class. Same as the RTCLTYPT pointer in the RSCLASS.TXT file for

cooling.

HVAC cooling equipment type. Same as the RTEQTYPE variable in the RSMEQP.TXT file

for cooling.

HVFYEAR Initial calendar year for this model of this equipment type. The first HVFYEAR for a

model within a type should be the NEMS base year; subsequent initial years for a model

must be previous RTLASTYRes+1.

HVLYEAR Last calendar year for this model of this equipment type. Must be greater than or equal

to HVFYEAR for this model; final HVLYEAR should be year of the projection horizon.

HVHEATFACT Elasticity of the heating shell factor based on square footage.

HVCOOLFACT Elasticity of the cooling shell factor based on square footage.

HTSHEFF Heating shell efficiency index for HVAC system type.

CLSHEFF Cooling shell efficiency index for HVAC system type.

SHELCOST Installed capital cost for shell measures per unit for new homes.

SHELLSUBSIDY Federal subsidy/ rebate per housing unit.

SHELLSUBSIDY111D Utility subsidy/ rebate per housing unit.

HVBETA1 HVAC efficiency choice model log-linear parameter β_1 , weights capital cost.

HVAC efficiency choice model log-linear parameter β_2 , weights fuel cost.

HVPACKG HVAC shell efficiency package number.

HVPGNAME Unique name for each HVAC shell efficiency package type.

Service demand and baseload by new housing type

File: RSUECSHL.TXT (formerly part of RMISC.TXT)

Source: Various.

Units: Discussed for each variable.

Comments: Contains new-home service demand and baseload inputs by housing type, Census

division, and technology; used to calculate operating costs for builder choice in new

construction.

Variables:

NEWHEATUEC_{es,b,r} Service demand for heating equipment by equipment type (aligns with

equipment class name RTCLNAME in RSCLASS.TXT input file), housing type, and

Census division. Efficiency by equipment type found in Table 3.

NEWCOOLUEC_{b,r} Service demand for cooling equipment by equipment type (aligns with

equipment class name RTCLNAME in RSCLASS.TXT input file), housing type, and

Census division. Efficiency by equipment type found in Table 3.

BASELOAD_{es} Standard level of efficiency as seen in Table 3 for RTCLEQCL heating classes 1–11

and cooling classes 1-5 in the RSCLASS.TXT input file.

LEARNFACT_{b,r} Learning factors (no units) for ENERGY STAR qualified shells by housing type and

Census division.

Miscellaneous Electric Loads (MELs)

File: RSMELS.TXT (formerly part of RMISC.TXT)

Source: Analysis and Representation of Miscellaneous Electric Loads in NEMS, Navigant

Consulting, Inc. and SAIC; multiple Technical Support Documents of DOE Appliance

Standard Rulemakings.

Units: Index, base year = 1.0.

Comments: For each end use described in this file, there are two arrays, both indexed to the base

year. One index modifies the number of units per household (penetration, or PEN) and the other modifies the per-unit energy consumption (efficiency, or EFF). Each end use has two variables associated with it; the variable naming convention uses the first three letters to associate the end use and the last three letters to associate the index type

(PEN or EFF).

Variables:

PEN_v Indexed change in equipment stock per household by year for each end use.

___*EFF*_y Indexed change in per-unit energy consumption index by year for each end use.

Where the first three letters of each variable are associated with the following end uses:

Televisions and related equipment

TVS___ Televisions
STB Set Top Boxes

HTS___ Home Theater Systems

DVD___ DVD Players

VGC___ Video Game Consoles

Computers and related equipment

DPC___ Desktop PCs
LPC__ Laptop PCs
MON Monitors

NET___ Modems & Routers (networking equipment)

Other miscellaneous electric loads

BAT___ Non-PC Rechargeable Electronics (battery chargers)

CFN___ Ceiling Fans
COF__ Coffee machines
DEH__ Dehumidifiers
MCO Microwaves

PHP___ Pool Heaters & Pumps
SEC__ Security Systems
SPA__ Portable Electric Spas

WCL Wine Coolers

Equipment Switching

File: RSSWITCH.TXT (formerly part of RMISC.TXT)

Source: Switching costs based on RSMeans Residential Cost Data, 2008.

Units: Discussed for each variable.

Comments: The bias parameters inform the logit function for new home heating equipment choice,

while the replacement cost parameters describe costs associated with switching heating

equipment (in addition to the equipment cost itself).

Variables:

RTFCBIAS_{ea,b,r} Bias parameters for new home heating fuel choice.

RPINSCOST_{eq,eqsw} Installation cost associated with switching from equipment class (eg) to

equipment class (egsw) when equipment is replaced.

Distributed Generation Technologies

File: RSGENTK.TXT (formerly RGENTK.TXT)

Source: "Review of Distributed Generation and Combined Heat and Power Technology

Performance and Cost Estimates and Analytic Assumptions for the National Energy Modeling System," Leidos; "Tracking the Sun: The Installed Price of Residential and Non-Residential Photovoltaic Systems in the United States," Lawrence Berkeley National Laboratory; "Annual Technology Baseline," National Renewable Energy Laboratory; Interstate Renewable Energy Council; Solar Energy Industry Association; Database of

State Incentives for Renewable Energy (DSIRE); RECS.

Units: Described for each variable.

Comments: This file contains variables used in the distributed generation module calculations,

including cost, efficiency and performance variables for the three modeled technologies (photovoltaics, fuel cells and small wind turbines); niche variables for modeling within

Census region (see RDISTGEN section of documentation); and historical installations by Census division.

Variables:

igencapcostyr Dollar year of equipment costs, based on source data.

xalpha Penetration function shape parameter.

xpenparm Penetration function used to calculate maximum market share into new construction

parameter.

 $xoperhours_t$ Typical operating hours by technology.

*xbeta*_t Learning *beta* parameter by technology.

 xcO_t Learning cO parameter by technology.

iRPSStartYear Year for which renewable portfolios standard (RPS) credits are available for residential

photovoltaic generation.

iRPSPhaseOutYear Last year for which RPS credits are available for residential photovoltaic

generation.

iRPSGrandFatherYear Year after which photovoltaic installations are grandfathered in to receive RPS

credits.

xinx Initial interconnection limitation by Census division.

xinxfy First year of interconnection limitations.

xinxly Last year of interconnection limitations.

xtaxrate Marginal combined federal and state income tax rate, currently assumed to be 34% for

the typical homeowner.

xdownpaypct Down payment percentage assumed to apply to the distributed generation investment,

currently 10% of the installed cost.

xintrate Residential mortgage rate from the Macroeconomic Activity Module.

xterm Loan term (currently set at 30 years).

xinflation Inflation assumption for converting constant-dollar fuel costs and fuel cost savings into

current dollars for the cash flow model in order to make the flows correspond to the

nominal-dollar loan payments. The current assumption is 3% annually.

aequipname_{t,v} Distributed generation technology equipment name.

 $ifueltype_t$ Fuel used by technology (0 for solar and wind); must coincide with fuels in Table 1.

*ifirstyr*_{t,v} First year technology is available.

 $ilastyr_{t,v}$ Last year technology is available.

 xkW_{tv} Capacity (kW) of typical system. Note that capacity must remain constant across

vintages for a given technology.

 $xeleff_{t,v}$ Electrical conversion efficiency by technology and vintage.

xlossfac_{t,v} Conversion losses (for systems that are rated at the unit rather than per available

alternating current wattage) if appropriate.

 $xdegrad_{t,v}$ Degradation of conversion efficiency by technology and vintage.

 $xeqlife_{t,v}$ Equipment lifetime by equipment type and vintage.

xwhrecovery_{t,v} Waste heat recovery factor for technologies that burn fuel (i.e., not wind or

solar photovoltaics).

 $xinstcost_{t,v}$ Installation cost in dollars per kW.

 $xcapcost_{t,v}$ Capital cost of the investment in dollars per kW.

 $xmaintcst_{t,v}$ Annual maintenance cost in dollars per kW.

*xintervalcst*_{t,v} DC-to-AC inverter cost.

*iintervalyrs*_{t,v} DC-to-AC inverter equipment lifetime.

 $xavail_{t,v}$ Percentage of time available (1 – forced outage rate – planned outage rate)

applied to typical operating hours.

 $xtxcrpct_{tv}$ Tax credit percentage that applies to a given technology's total installed cost (if

any).

xtxcrmaxperkw_{t,v} Maximum tax credit dollar amount, if any, per kW system capacity.

xtxcrmaxpersys_{t,v} Maximum tax credit dollar amount, if any, per distributed generation system.

xtxcrpct_div_{t,v,r} Subsidy/ rebate per system as a percent of installed capital cost. Nine columns

correspond to the nine U.S. Census divisions shown in Table 1.

xtemp RPS credit availability (1 = yes, 0 = no). Annualized using xrps variable.

xtemp1 Number of years before RPS rate adjustment. Annualized using iNumYrsatRPSBaseRate

variable.

xtemp2 Total number of RPS credit years. Annualized using iNumRPSCreditYrs variable.

Descriptions for renewable resource and electricity *niche-dimensioned* rate level variables within each Census division from RECS:

xSolarInsolation_{r.n.rl} Estimated solar insolation (kWh per square meter per day) for Census division,

solar niche, and electricity rate level.

*xHHShare*_{r,n,rl} RECS share of households within each niche.

xRateScalar_{r.n,rl} RECS ratio of electricity price for niche to Census division average price.

xAvgKWH_{r,n,rl} RECS average annual electricity consumption in kWh per household within each

niche.

*xRoofAreaPerHH*_{r.n,rl} Estimated roof area per household within each niche.

 $xWindSpeed_{r,n,rl}$ Estimated wind speed within each niche in meters per second.

xRuralPctHH_{r.n,rl} RECS percentage of households that are considered rural in each niche.

Variables representing program-driven and historical distributed generation capacity:

xexogpen_{t,t,y} Exogenous distributed generation capacity by technology, Census division, and year.

Solar Photovoltaic Penetration Hurdle Model

File: RGENTK.TXT

Source: State solar PV program data from California, New Jersey, and Arizona; U.S. Census

Bureau's American Community Survey (ACS); solar insolation data from the National

Renewable Energy Laboratory; various reports and studies.

Units: Described for each variable.

Comments: This file has been repurposed from its former use as the residential distributed

generation technology menu and now contains ZIP code-level variables used to calculate

solar photovoltaic installation penetration.

Variables:

UseNewModel Boolean variable used to activate ZIP code solar PV penetration model.

EstYear First year of data estimated by ZIP code model.

Coefficients for full, urban, and rural models:

CINT Model intercepts.

CHH Number of households.

CPD Population Density.

CINC Income.

CINS Solar insolation.

CER Electricity rate.

CCDD One-year lagged cooling degree days.

CPMT Monthly payment for PV system (30-year).

CIR Interest rate.

CLAG1 Lag1 PV installs (one-year lag).

CLAG2 Lag2 PV installs (two-year lag).

CPVP PV installed price net of tax credits (if any).

NumZips Total number of ZIP code records in file.

ZIP code-level data:

ZipCodes Record ZIP code.

State State that includes the record ZIP code.

CenDiv Census division (shown in Table 1) that includes the record ZIP code.

Income Median household income in nominal *EstYear* dollars.

Households Number of households within the ZIP code.

PopDensity Population density in units of households per square mile.

Insol Annual average solar irradiation level, in kilowatthours per square meter per day

(assumed to be constant over time).

ElecRate ZIP code-level electricity rate in cents per kilowatthour, derived from state-level and ZIP

code-level rates.

LagCDD One-year lagged cooling degree days.

IntRate Annual average mortgage interest rate for EstYear.

PVPrice Installed price of solar PV system in EstYear.

Monthly Payment Monthly payment per kW of installed system capacity, based on a 30-year (360

month) mortgage.

Lag1Installs One-year lagged estimate of number of residential solar PV installations in the ZIP code.

Lag2Installs Two-year lagged estimate of number of residential solar PV installations in the ZIP code

(not currently used in the models).

PureHurdle Value (0 or 1) indicating whether or not Lag1Installs is used in projections for the ZIP

code (0 indicates it is used).

RuralZip Value (0 or 1) identifying ZIP code as rural (i.e., having a population density of 10 or

fewer households per square mile).

ModelInstalls Projected number of new residential solar PV installations for the ZIP code.

Historical ENERGY STAR Home Shares

File: RSESTAR.TXT (formerly RSUEC11.TXT).

Source: ENERGY STAR Certified New Homes Market Indices for States, Environmental Protection

Agency.

Units: Share of homes within Census division, building type, and shell integrity level.

Comments: The information in this file was not used for AEO2016.

Variables: HVEQWTN_{v,e,s,d} Percent of homes meeting ENERGY STAR Home specification or better

by heating technology type, shell level type, and Census division.

Weather (Degree Days)

File: KDEGDAY.TXT (formerly part of RMISC.TXT)

Source: Historical and near-term forecast of heating and cooling degree days from NOAA.

Projected degree days developed exogenously by EIA based on a 30-year historical trend. Population weights from detailed inputs to the Macroeconomic Activity Module,

which maintains historical and projected state-level populations.

Units: Population-weighted degree days.

Comments: This file, which is also used by the commercial demand module (CDM), supplies heating

and cooling degree day information for weather adjustments in the RDM.

Variables:

HDDADJ_{v,r} Heating degree days by Census division and year.

 $CDDADJ_{y,r}$ Cooling degree days by Census division and year.

Miscellaneous Inputs

File: RSMISC.TXT (formerly RMISC.TXT)

Units: Discussed for each variable.

Source: Discussed for each variable.

Comments: This file contains several variables and arrays that otherwise did not fit conceptually

with the other input files.

Variables:

HDR_b Housing demolition rates by building type.

Existing houses in the base year by building type and Census division (with totals).

 $RACSAT_{b,r}$ New room air conditioner saturation level by building type and Census division.

RACUNTS_{b,r} Number of room air conditioners per housing unit by building type and Census division.

 $CACSAT_{b,r}$ New central air conditioner saturation level by building type and Census division.

CACPR_r Central A/C penetration rate by Census division.

DISHPEN Dishwasher penetration rate.

FRZSAT_{b.f} New home freezer saturation level by building type and Census division.

*REFSAT*_{b,r} New home refrigerator saturation level by building type and Census division.

ELDRYPR_{b,r} Electric dryer penetration rate by building type and Census division.

SHTSHR_{r,f,b} Secondary heating share by fuel, building type, and Census division.

NSHTSHR_{r,f,b} Secondary heating share for post-base-year construction by fuel, building type, and

Census division.

ELASTIC_{s,r} Elasticity of service demand with respect to square footage by end use and Census

division.

*NEWDRYSAT*_{eg,b,r} New dryer saturation by type (natural gas, electric).

 $DISHNEW_{b,r}$ Percent of new housing units with dishwashers by building type and Census division.

 $WASHNEW_{b,r}$ Percent of new housing units with clothes washers by building type and Census division.

 $WTHRZTN_{v,f,r}$ Changes to existing shell index due to weatherization measures.

ELAST Elasticity parameters for calculating model price elasticities.

Historical Data and Short-Term Energy Outlook Benchmarking

File: RSSTEO.TXT

Units: Trillion Btu

Source: Three EIA products: State Energy Data System, Monthly Energy Review, and Short-Term

Energy Outlook

Comments: Regional consumption by fuel and year for historical years comes from the State Energy

Data System for the model's base year and as many subsequent years as available. Beyond those years, national total energy consumption by fuel and year comes from the *Monthly Energy Review*, and beyond that, the *Short-Term Energy Outlook* for near-term

forecasts.

Variables: STEOCN_{y,f,r}

Baseline Electricity Consumption for Energy Efficiency Calculations

File: BLDBASE.TXT (also used by the Commercial Demand Module of NEMS)

Source: Integrated NEMS model run in which no energy efficiency rebates or subsidies are

included (with the exception of federal tax credits).

Units: Billion kilowatthours.

Comments: Used to calculate incremental electricity consumption between an integrated NEMS

model run that includes energy efficiency rebates (i.e., the AEO Reference case including the Environmental Protection Agency's Clean Power Plan) and one in which no rebates

are included.

Variable:

baselinebkwh_{v,r} Baseline electricity consumption, by Census division, model index year (starting

in 1990), and sector (residential and commercial).

Appendix B: Detailed Mathematical Description

This appendix presents the detailed calculations used in each of the module components. Table B-1 shows the correspondence between each of the subscripts in the documentation and the subscripts in the Fortran source code. The table of subscripts includes all of the major usages. In some minor instances, additional subscripts are defined as needed.

The equations and variable assignment statements follow the logic of the Fortran code very closely to facilitate an understanding of the code and its structure. In several instances, a variable appears on both sides of an equal sign. These statements must not be interpreted as equations. They are computer programming assignment statements that allow a previous calculation to be updated (for example, multiplied by a factor) and re-stored under the same variable name (i.e., in the same memory location). The equal signs in these statements do not denote equality; rather, they indicate that the value stored in a location in the computer's memory is being overwritten by a new value.

The subscript *y* in the documentation refers to the year represented as 1990 through the projection horizon. In the Fortran code, the subscript CURIYR represents array dimensions starting with an index of 1 to represent 1990, and CURCALYR represents the calendar years 1990 through the projection horizon.

Some variables are documented having a *y* dimension when, in the Fortran code, they do not. The most common instances are for the variables, LFCY, OPCOST, SA, SHARESN, and SHARESR. These variables are calculated on an annual basis but are retained only for the current year. Although previous values are overwritten, the variables do have a *y* dimension. The *y* dimension is shown explicitly in the documentation to highlight 1) that the calculations do vary by year, and 2) to indicate the current year in formulas to avoid confusion.

Summations over all relevant variables are usually written without upper and lower range limits on the summation signs.

Table B-1. Definition of Subscripts

Subscript in	Subscript in Fortran	
Documentation	code	Description
R	r or d	Census division
T	y or t	Calendar year index
F	F	Fuel types
В	В	Housing (building) type
Baseyr	RECSyear	Base year (latest RECS available)
Υ	curiyr or curcalyr	Annual index or calendar year
y-1	curiyr-1 or curcalyr-1	Previous year
Eg	eqc, reccl	General equipment class within an end use (e.g., 1 to 11 for space heating)
Egsw	Eqcsw	Equipment class within an end use available to switch to another equipment class
Es	Eqt	Specific equipment type within an end use
V	V	Vintage of equipment

Classification

The RDM regards the residential sector as a consumer of energy. It classifies this consumption into a series of end uses that represent the various ways in which energy is used by housing units. The end uses listed in Table 1 are defined within the logic of the RDM and determine the organization of the data found in the input data files and discussed in this document.

Further, the RDM assumes that a series of broad equipment classes are available to satisfy the demands within the end uses. Using input data files, the user can modify the definitions of equipment classes available for each of the major end uses, as well as penetration and per-unit consumption assumptions for several miscellaneous electric loads. In general, the equipment classes are each used to satisfy a particular end use; however, there are a few cases where one class of equipment (e.g., heat pumps) satisfies more than one end use, or where the availability of one class of equipment makes another class more likely (a natural gas furnace is frequently accompanied by a natural gas water heater and cooking equipment).

Each equipment class comprises a variety of specific equipment types that each have their own technological characteristics, such as efficiency, cost, and year when the technology is expected to become available or made obsolete. Examples of equipment types include the array of available natural gas furnaces, the more expensive of which tend to have higher efficiencies. The RDM does not attempt to represent all manufacturers' products, but rather defines broad types that are similar to one another in their technological characteristics. The user has the ability to define and modify the definitions of these equipment types by modifying the equipment menu files.

Each equipment type can be assigned different characteristics during different ranges of years or vintages. Each of these time-related sets of characteristics is sometimes referred to as an equipment model of the given equipment type.

The concept of equipment classes comprising a number of different equipment types that each contain several models underlies the entire discussion of this manual. In earlier editions of the documentation, these two classifications were referred to as general equipment type (equipment class), and specific equipment type (equipment type). These names survive in the subscripts assigned to the two concepts throughout the document, eg and es, respectively. Over time, cost and performance can vary even within a specific equipment type, especially as appliance standards are introduced.

Other RDM files define the characteristics of the mix of appliances that are in use in the base year, including relative numbers installed (i.e., existing stock), efficiencies, and the rates at which they are expected to be replaced.

Within the present structure of the Residential Demand Module, there are 30 defined technology classes. The list is not exhaustive of all equipment used in the residential sector in the main end uses, in that there is, for example, a small percentage of homes in which wood is burned to heat domestic water; the vast majority of equipment used to satisfy the major end uses falls into at least one class.

Within each of the equipment classes defined in the RSCLASS.TXT file, the Residential Demand Module accepts one or more types of equipment. The module chooses among the equipment types according to

energy costs, equipment costs, and the relative efficiencies of the available types. The RSMEQP.TXT file contains the data used by the model for selecting which of the types are used. In general, the module does not exclusively select one of the alternatives available within a class, but rather changes the proportions of each type according to its evaluation of the equipment characteristics (i.e., a distribution of selections rather than a single selection).

The characteristics of each equipment type can change over time, so the RSMEQP.TXT file allows more than one set of characteristics for each equipment type.

Housing and equipment stock formation

To calculate the number of existing dwellings, the Housing Stock Component adds newly built homes to the inventory and subtracts demolitions. Housing construction starts are obtained from regional outputs of the Macroeconomic Activity Module (MAM). Existing base-year housing stock is designated as the *existing* vintage, and new additions to the housing stock are referred to as the *post-base-year* vintage. Additions and replacements for both housing vintages are tracked through the projection period.

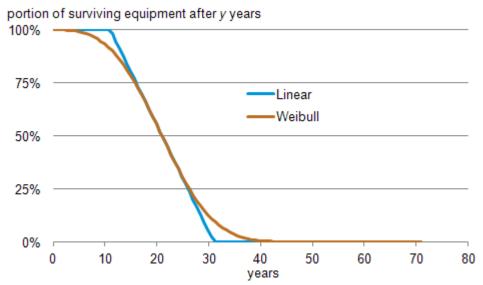
SVRTE is a function that can be called with arguments and returns a single value as its result. The survival rate function is a Weibull-shaped decline, as shown in Figure 2 below. Its mathematical description is as follows:

$$SVRTE_{y,k,\lambda} = e^{-(y/\lambda)^k}$$
 (B-1)

where

 $SVRTE_{y,k,\lambda}$ is the proportion of surviving equipment after y years, y is the number of years after purchase, λ is the scale parameter, and k is the shape parameter.

Figure 2. Weibull and linear equipment survival rate functions



The Weibull k and λ shape parameters were estimated to approximate the median and slopes of the existing linear decay functions that had been used in AEO2012 and prior *Outlooks*.

Note that function calls to SVRTE in the Fortran code include a placeholder as the first argument; however, the first argument is currently not used in the calculations. Because it is not used in the definition of the function in (B-1), it is not noted explicitly in the remainder of this documentation.

Existing housing evolution rate

The model assumes housing units are removed from the stock at a constant rate over time. This rate is intended to reflect all changes to the count of residential units other than additions from new construction. This includes demolition, decay, vacancy, etc., as well as additions such as conversion from commercial buildings. Thus, they are best thought of as evolution rates rather than demolition or decay factors. The evolution rates for the housing unit types (HDR_b) are as follows:

Single-Family Homes: $HDR_1 = 0.997$ Multifamily Homes: $HDR_2 = 0.995$ Mobile Homes: $HDR_3 = 0.966$

These values were determined based on analysis of housing starts and housing stock arrays provided by the Macroeconomic Activity Module. By analyzing these two concepts at the building type level, the long-term average implicit evolution rate can be calculated.

The surviving base-year housing stock is defined by

$$EH_{y,b,r} = RECS \ data \ , if \ y = baseyr$$

$$EH_{y,b,r} = EH_{y-1,b,r} * HDR_b \ , if \ y > baseyr$$
 (B-2)

where

 $EH_{y,b,r}$ is the base-year housing stock surviving in year y, HDR_b is the housing evolution rate

New construction

New houses are added to the stock each year, as provided by the NEMS Macroeconomic Activity Module. The total number of new additions in a given year is computed as:

$$NH_{y,r} = MC_HUSPS1_{y,r} + MC_HUSPS2A_{y,r}$$

$$+ MC_HUSMFG_{y,r}$$
 (B-3)

where

 $NH_{y,r}$ is total new housing added by year and Census division, $MC_HUSPS1_{y,r}$ is single-family housing added by year and Census division, $MC_HUSPS2A_{y,r}$ is multifamily housing added by year and Census division, and $MC_HUSMFG_{y,r}$ is mobile home shipments added by year and Census division.

Square footage

In the calculation of square footage, the model first aggregates the housing stock to the national level:

$$OLDHSES_{y} = \sum_{b,r} EH_{y,b,r}$$
(B-4)

$$NEWHSES_{y} = \sum_{b,r} NH_{y,b,r}$$
(B-5)

where

 $OLDHSES_y$ is the national total of remaining housing that existed in the base year, and $NEWHSES_y$ is the national total of remaining post-base-year new construction additions.

$$SQFTAVG_{baseyr} = \frac{\sum_{b,r} \left(SQRFOOT_{baseyr,b,r} * EH_{baseyr,b,r} \right)}{OLDHSES_{baseyr}}$$
(B-6)

$$SQFTAVG_{y \neq baseyr} = \frac{\sum_{b,r} \left(SQRFOOT_{baseyr,b,r} * EH_{baseyr,b,r} + SQRFOOT_{y,b,r} * NH_{y,b,r} \right)}{OLDHSES_{baseyr} + NWHSES_{y}}$$
(B-7)

where

 $SQFTAVG_y$ is the average floor area of houses of all types, and

 $SQRFOOT_{v,b,r}$ is a table of historical and projected housing floor areas by year, housing type,

and Census division.

Projecting base-year vintage equipment for all end-use services

Much of the equipment that exists in the base year survives into subsequent years. For years beyond the base year:

$$EQCESE_{y,eg,b,r} = EQCESE_{baseyr,eg,b,r} * HDR_b^{y-baseyr} * EQCRET_{y,eg}$$
(B-8)

where

EQCESE_{y,eg,b,r} is the amount of surviving base-year vintage equipment in base-year housing by

housing type and Census division,

 HDR_b is the housing evolution rate by housing type, and

 $EQCRET_{y,eq}$ are the annual equipment retirement fractions for the equipment classes.

Technology Choice Component

The Technology Choice Component uses a log-linear function to estimate technology market shares for the 10 major end uses. The module is able to calculate market shares based on consumer behavior as a function of bias, capital costs, and operating costs or as a function of life-cycle costs.

All other uses are modeled differently and in less detail than the 10 major end-use services.

Space Heating

Space heating is modeled in two stages. For new construction, the first-stage choice is the *HVAC/shell* package which is a combination of heating equipment, air conditioning equipment, and building shell levels. There are up to five HVAC/shell packages available, generally named relative to the code level that is met: no code, the IECC code, and three more advanced ENERGY STAR qualified shells performing 30%, 40%, and 50% better than IECC. Not all equipment combinations are modeled for advanced shells.

The HVAC/shell packages are fuel-specific, so once chosen, the fuel choice is also determined. The second-stage choice models increases in efficiency for the heating and air conditioning equipment if available (for some of the advanced packages, the equipment may already be the most-efficient available). For existing construction, the first stage considers fuel-choice and the second stage equipment efficiency for the selected equipment class.

New equipment operating costs are computed by the expression:

$$OPCOST_{y,es,b,r,v} = PRICES_{f,r,y} * EQCUEC_{y,eg,b} * HDDFACT_{r,y}$$

$$*RTEFFAC_{eg,v} * HSHELL_{v-l,r,v}$$
 (B-9)

where

 $OPCOST_{y,es,b,r,v}$ is the operating cost for the specific equipment type by year, housing type, Census division, and vintage, $PRICES_{f,r,v}$ is the fuel price for the equipment by fuel, region, and projection year, $EQCUEC_{r,eg,b}$ is the unit energy consumption by Census division, equipment class and housing type, is an adjustment factor for weather differences between the base year and the HDDFACT_{r,v} current year; it is computed as the ratio of the numbers of heating degree days in the current (numerator) and base (denominator) years; is the efficiency adjustment for the general equipment class and vintage, and $RTEFFAC_{eq,v}$ is the shell efficiency adjustment to account for building shell improvements HSHELL_{v-1,r,v} over time (which reduce heating loads).

For newly constructed homes, heating and cooling choices are linked and therefore operating cost is a function of both the heating and cooling operating costs, with the shell efficiency also accounted for as:

$$\begin{aligned} OPCOST_{y,es,b,r,hvac} &= PRICES_{f,r,y} * EQCUEC_{y,heatingb} * HDDFACT_{r,y} \\ * RTEFFAC_{heatingv} * HTSHELL_{eg,r,b} + PRICES_{f,r,y} * EQCUEC_{y,coolingb} \\ * CDDFACT_{r,y} * RTEFFAC_{coolingv} * CLSHELL_{eg,r,b} \end{aligned} \tag{B-10}$$

where

 $HTSHELL_{eg,r,b}$ is the heating shell efficiency factor for the HVAC system, $CDDFACT_{r,y}$ is the cooling degree day adjustment factor, and $CLSHELL_{eg,r,b}$ is the cooling shell efficiency factor for the HVAC system.

The consumer is allowed to choose among the various levels of cost and efficiency for a given class of equipment. Electric heat pumps are an example of an equipment class (denoted by eg). Equipment type (denoted by es) refers to the same class of equipment with different efficiency ratings (e.g., high- vs. low-efficiency electric heat pumps).

EQCOST is a time-dependent function for computing the installed capital cost of equipment in new construction and the retail replacement cost of equipment in existing housing. It is called if the cost trend switch COSTTRSW = 1 in COMMON file RTEK (which is the default). The formulation allows for three general classifications of equipment: mature equipment – no further time-dependent cost declines occur; adolescent and infant equipment – costs declines occur, but at different rates as set by the parameters and described below. For each of the three general classifications, the following equations describe the calculations for mature, adolescent, and infant technologies, respectively:

$$EQCOST_{es,y,CAP} = RTEQCOST_{es} \text{ , if } RTMATURE_{es} = MATURE$$

$$EQCOST_{es,y,RET} = RTRECOST_{es} \text{ , if } RTMATURE_{es} = MATURE$$
 (B-11)
$$EQCOST_{es,y,CAP} = \frac{RTEQCOST_{es} * 2 * d}{1 + \left(\frac{y - y_1}{y_0 - y_1}\right)^{\gamma}} + (1 - d) * RTEQCOST_{es},$$
 (B-12)
$$EQCOST_{es,y,RET} = \frac{RTRECOST_{es} * 2 * d}{1 + \left(\frac{y - y_1}{y_0 - y_1}\right)^{\gamma}} + (1 - d) * RTRECOST_{es},$$
 if $RTMATURE_{es} = ADOLESCENT$

$$EQCOST_{es,y,CAP} = \frac{RTEQCOST_{es} * d}{1 + \left(\frac{y - y_1}{y_0 - y_1}\right)^{\gamma}} + (1 - d) * RTEQCOST_{es},$$

$$if \ RTMATURE_{es} = INFANT$$

$$EQCOST_{es,y,RET} = \frac{RTRECOST_{es} * d}{1 + \left(\frac{y - y_1}{y_0 - y_1}\right)^{\gamma}} + (1 - d) * RTRECOST_{es},$$

$$if \ RTMATURE_{es} = INFANT$$
(B-13)

where

EQCOST_{es,y,ctype} is time-dependent installed capital cost of equipment in new construction or the retail replacement cost of equipment in existing housing,

ctype tells function type of equipment cost to return,

CAP = Return installed capital cost in new construction, RET = Return retail replacement cost in existing housing,

RTMATURE_{es} is a technology maturity description,

MATURE = no further equipment cost reductions expected,

ADOLESCENT = major cost reductions occurred before base year, INFANT = all cost reductions expected after first year available,

RTEQCOST_{es} is installed wholesale capital cost in RTEKDOLLARYR dollars per unit for new

homes, which remains constant for MATURE technologies only (used when

ctype = CAP),

RTRECOST_{es} is retail capital cost in RTEKDOLLARYR dollars per unit for replacements, and

remains constant for MATURE technologies only (used when ctype = RET),

y is the current projection calendar year,

 y_0 is the year of inflection of cost trend,

RTINITYR_{es} if ADOLESCENT, RTCOSTP1_{es} if INFANT,

 y_1 is the year cost decline began,

RTCOSTP1_{es} if ADOLESCENT, RTINITYR_{es} if INFANT,

d is the total possible proportional decline in equipment cost, RTCOSTP3_{es},

from y₀ onward if ADOLESCENT and from y₁ onward if INFANT,

y is the assumed logistic curve shape parameter, RTCOSTP2_{es}.

For newly constructed homes, the costs shown above also include the cooling system and shell efficiency measures.

The concept of price-induced technology change is also included in the formulation of equipment costs. Although not activated in most model runs, this concept allows future technologies faster diffusion into the marketplace if fuel prices increase markedly and remain high over a multi-year period. First, compare the average fuel price for a given fuel over a three-year period to the price observed in the base year:

$$PRICE\Delta_{y,f} = \frac{0.33333*(PRICE_{y,f} + PRICE_{y-l,f} + PRICE_{y-2,f})}{PRICE_{baseyr}}$$
(B-14)

Under a *persistent* doubling of energy prices (defined in the models as three consecutive years, as noted in (B-14) above), the most advanced technologies will advance forward by at most 10 years. For nearer-term technologies, shifts are limited to a lesser number of years by the algorithm to ensure that future technologies cannot become available before the persistent price change is projected to occur. The formulation only allows technologies potentially to shift toward earlier availability, and once shifted, they never shift back. This shift is represented as:

$$SHIFTYEARS_f = \frac{\left(PRICE\Delta_f - 1.0\right)}{0.10}$$
 (B-15)

subject to the constraints listed above. The initial technology year, RTINITYR, used in equations (B-11) to (B-13) is adjusted according by the year shift obtained in equation (B-15).

The module includes the option to use life cycle costing to calculate market share weights. The life-cycle cost calculation is

$$LFCY_{y,es,b,r,v} = CAPITAL_{es} + OPCOST_{y,es,b,r,v} * \left(\frac{1 - (1 + DISRT)^{-HORIZON}}{DISRT}\right)$$
(B-16)

where

 $LFCY_{y,es,b,r,v}$ is the life-cycle cost of an equipment type by projection year, housing type,

Census division, and vintage,

CAPITALes is the installed capital cost of an equipment type based on calling EQCOST with

RTEQCOST1_{es},

 $OPCOST_{y,es,b,r,v}$ is the operating cost for the specific equipment type by year, housing type,

Census division, and vintage,

HORIZON is the number of years into the future used to compute the present value of

future operating cost expenditures, presently set to seven years, and

DISRT is the discount rate applied to compute the present value of future operating

costs, presently set at 20%.

A weight for each equipment class is calculated to estimate the market share for each of the 11 heating system classes for new construction based on the cost factors computed above. The functional form is expressed as:

$$HEATSYS_{y,eg,b,r} = LAGFACTOR * HEATSYS_{y-1,eg,b,r} + (1 - LAGFACTOR) * \exp(RFTBIAS_{y,eg} + RTFCBETA_{eg} * LFCY_{y,eg,b,r,v})$$
(B-17)

where

HEATSYS_{v,eq,b,r} is the equipment weight for a heating equipment class for new housing by year,

housing type, and Census division,

LAGFACTOR is the weight given to the prior year's heating system share,

RTFCBIAS_{v,eq} is a consumer preference parameter that fits the current market share to

historical shipment data,

LFCY_{v,eq,b,r,v} is the life-cycle cost for the equipment class by year, housing type, Census

division, and vintage, and

 $RTFCBETA_{eg}$ is a parameter value of the log-linear function.

The sum over the heating equipment classes gives the total weight for all of the heating equipment:

$$SYSTOT_{y,b,r} = \sum_{a=-1}^{11} HEATSYS_{y,eg,b,r}$$
(B-18)

where

 $SYSTOT_{y,b,r}$ is the sum of equipment class weights for the all equipment classes.

The equipment class fuel share is computed as

$$HTYSSHR_{y,eg,b,r} = \frac{HEATSYS_{y,eg,b,r}}{SYSTOT_{y,b,r}}, if SYSTOT_{y,b,r} > 0$$
 (B-19)
$$HTYSSHR_{y,eg,b,r} = 0, otherwise$$

where

 $HTYSSHR_{v,eq,b,r}$ is the equipment class fuel share by year, building type, and Census division.

For each equipment type within each class, a weight is calculated based on the cost factors computed above. The functional form is expressed as:

$$EQWTN_{y,es,b,r} = \exp(RTECBTA1_{es} * CAPITAL_{es} + RTECBTA2_{es} * OPCOST_{y,es,b,r,1})$$
(B-20)

$$EQWTR_{y,es,b,r} = \exp(RTECBTA1_{es} * CAPITAL_{es} + RTECBTA2_{es} * OPCOST_{y,es,b,r,2})$$
(B-21)

where

EQWTN_{y,es,b,r} is the equipment weight for new equipment type by year, housing type, and Census division,

*EQWTR*_{y,es,b,r} is the equipment weight for replacement equipment type by year, housing type, and Census division,

 $OPCOST_{y,es,b,r,v}$ is the operating cost for the equipment type by year, housing type, Census division, and vintage (1=new, 2=existing), and

RTECBTA1es

RTECBTA2_{es} these two parameters give relative weights to the capital and operating costs in the equipment choice determination – their ratio is approximately the discount rate used valuing the operating cost savings from more-efficient equipment.

Sums over the equipment types within each class give total weights for the equipment classes:

$$TOTEWTN_{y,eg,b,r} = \sum_{es \in eg} EQWTN_{y,es,b,r}$$
(B-22)

$$TOTEWTR_{y,eg,b,r} = \sum_{es \in eg} EQWTR_{y,es,b,r}$$
(B-23)

where

 $TOTEWTN_{y,eg,b,r}$ is the sum of weights for the new equipment types within equipment classes,

 $TOTEWTR_{y,eg,b,r}$ is the sum of weights for the replacement equipment types within equipment classes.

The equipment type share within a general equipment class is computed as:

$$EQFSHRN_{y,es \in eg,b,r} = \frac{EQWTN_{y,es \in eg,b,r}}{TOTEWTN_{y,eg,b,r}}, if \ TOTEWTN_{y,eg,b,r} > 0$$

$$EQFSHRN_{y,es \in eg,b,r} = 0, otherwise$$
(B-24)

$$EQFSHRR_{y,es \in eg,b,r} = \frac{EQWTR_{y,es \in eg,b,r}}{TOTEWTR_{y,eg,b,r}}, if \ TOTEWTR_{y,eg,b,r} > 0$$
 (B-25)
$$EQFSHRR_{y,es \in eg,b,r} = 0, otherwise$$

where

 $EQFSHRN_{y,es} \in _{eg,b,r}$ is the new equipment type share by year, building type, and Census division, and

 $EQFSHRR_{y,es} \in _{eg,b,r}$ is the replacement equipment type share by year, building type, and Census division.

The weighted average equipment efficiencies for the equipment types within each equipment class are then computed as:

$$WTEQCEFFN_{y,eg,b,r} = \frac{\sum_{es \in eg} \left[\frac{EQFSHRN_{y,es,b,r}}{RTEQEFF_{y,es}} \right]}{\sum_{es \in eg} EQFSHRN_{y,es,b,r}}, if \sum_{es \in eg} EQFSHRN_{y,es,b,r} > 0$$

$$WTEQCEFFN_{y,eg,b,r} = \frac{1}{RTBASEFF_{eg}}, otherwise$$
(B-26)

$$WTEQCEFFR_{y,eg,b,r} = \frac{\sum_{es} \left[\frac{EQFSHRR_{y,es,b,r}}{RTEQEFF_{y,es}} \right]}{\sum_{es} EQFSHRR_{y,es,b,r}}, if \sum_{es} EQFSHRR_{y,es,b,r} > 0$$

$$WTEQCEFFR_{y,eg,b,r} = \frac{1}{RTBASEFF_{eg}}, otherwise$$
(B-27)

where

WTEQCEFFN_{y,es,b,r} is the weighted average efficiency of new equipment type within each

equipment class by year, housing type, and Census division,

 $RTEQEFF_{v,es}$ is the efficiency of the equipment type,

RTBASEFF_{es} is the base-year stock average efficiency of the equipment class, and

WTEQCEFFR_{v.es.b.r} is the weighted average efficiency of replacement equipment types

within each equipment class by year, housing type, and Census division.

Appliance stock component

The appliance stock component tracks the major energy-consuming equipment by housing vintage and equipment vintage for additions, replacements, and surviving equipment.

The equipment accounting system partitions equipment into two major categories, depending on the vintage of the housing unit: equipment installed in housing units existing in the base year (at the beginning of a model run) and equipment added to new housing units (those added during the model run). Equipment is further partitioned into three additional survival/replacement categories: equipment that survives, equipment purchased to replace other equipment, and equipment purchased for new construction. The categorization of equipment by housing vintage and surviving/replacement type results in seven categories of equipment that are tracked, as seen in Table B-2 below.

Table B-2. Categorization of tracked equipment by vintage and survival/replacement type

Category	Variable	Definition
Existing housing unit	EQCESE	Surviving equipment stock in base-year existing homes (i.e., equipment that was present in the base year)
	EQCSR90	Equipment stock in base-year existing homes that has been added as a replacement after the base year and that still survives
	EQCRP90	Current-year replacement equipment for base-year existing housing
	EQCRP90RP	Current-year replacements for equipment that had previously been replaced in EQCRP90 (i.e., replacements of replacements)
Modeled (new construction)	EQCSUR	Equipment that has been modeled as added and still survives
housing unit	EQCREP	Equipment that has been modeled as added and is in need of replacement in the current year
	EQCADD	Equipment for housing units added in the current year

Note: EQCND90 is the sum of EQCESE, EQCSR90, EQCRP90RP, and EQCRP90.

Table B-3. Categorization of equipment unit energy consumption (UEC) by category of housing unit

Category	Variable	Definition
Existing housing unit	EQCUEC	Average UEC for the original base-year equipment in housing units that existed in the base year
	EQCSUEC	Average UEC for surviving equipment in existing base-year housing units
	EQCAUEC	Average UEC for surviving equipment in existing base-year housing units that has been replaced in the model run
	EQCRUEC	UEC for all equipment added in the current year to replace existing base- year equipment
Modeled (new construction) housing unit	EQCHVUEC	UEC for heating and cooling equipment in new construction added in the current year
	EQCAHVUEC	Average UEC for heating and cooling equipment in surviving new construction
	EQCNUEC	UEC for all equipment added in the current year to replace equipment after the base year

Shell indices are modeled for three categories of housing units:

- EHSHELL is the shell index applicable to housing units that existed in the base year.
- AHSHELL is the shell index applicable to housing units added in all but the current year.
- NHSHELL is the shell index for housing units added in the current year.

For example, in accounting for the heating energy consumption of surviving equipment installed in housing units that existed in the base year, the equipment stock, HTESE, would be multiplied by the unit energy consumption, HTUEC, and by the shell index EHSHELL. This procedure was designed to account

for heating equipment, but the accounting principle is used throughout the residential demand module. For the example above, the appropriate space cooling variables would be CLESE, CLUEC and ECSHELL. The shell indices apply only to heating and cooling; thus, for example, for refrigeration the accounting requires only RFESE and RFUEC.

The housing decay rate is used in conjunction with the equipment survival rate to determine the number of equipment units that survive/retire each year in the projection. The Weibull-shaped function described in (B-1) is used to model the proportion of equipment surviving after y years of use.

Equipment in houses constructed in the model run is the product of the number of new houses and the market share of each equipment class. This is expressed as

$$EQCADD_{v,eg,b,r} = HSEADD_{v,b,r} * SHARESN_{v,eg,b,r}$$
(B-28)

where

EQCADD_{y,eg,b,r} is the number of post-base-year-vintage equipment units added to new houses

in year y, by housing type and Census division,

 $HSEADD_{y,b,r}$ is the number of new housing units constructed in the projection year by housing

type and Census division, and

 $SHARESN_{y,eg,b,r}$ is the current-year market share for each equipment class by housing type and

Census division.

The number of replacements for the post-base-year equipment units in post-base-year houses is calculated as

$$EQCREP_{y,eg,b,r} = \sum_{t=b,a(se)v+1}^{t=y-1} \left(EQCADD_{t,eg,b,r} * HDR_b^{y-t} * \left(1 - SVRTE_{y-t,L_{\min},L_{\max}} \right) \right)$$
(B-29)

where

EQCREP_{y,eg,b,r} is the number of equipment replacements of post-base-year equipment in post-

base-year houses,

HDR_b is the housing evolution rate by housing type, and

y-t is the age of the equipment.

Post-base-year replacement units required in the current year for houses existing in the base year are calculated as:

$$EQCRP90_{y,eg,b,r} = EQCESE_{baseyr,eg,b,r} * EQCRET_{y,eg} * HDR_b$$
(B-30)

where

EQCRP90_{y,eg,b,r} is the number of replacement units required for homes existing in the base year

in year y, by housing type and Census division,

EQCRET_{v.ea} is the equipment retirement rate for houses existing in the base year by

projection year,

 $EQCESE_{baseyr,eg,b,r}$ is the vintage stock of equipment in the base year in houses existing in the base year by housing type and Census division.

Within the projection period, some of the EQCRP90 will also need to be replaced. The number of units needing replacement is estimated as:

$$EQCRP90RP_{y,eg,b,r} = \sum_{t=2006}^{t=y-1} (EQCRP90_{t,eg,b,r} + EQCRP90RP_{t,eg,b,r}) * (1 - SVRTE_{y-t,L_{min},L_{max}})$$
(B-31)

where

 $EQCRP90RP_{y,t,eg,b,r}$ is the number of replacement units required to replace post-base-year

equipment in houses existing in the base year by projection year,

housing type, and Census division.

Next, a series of calculations is made to determine the number of replacement units that switch to a different technology type. For each type of replacement (EQCRP90, EQCRP90RP, EQCREP), first calculate the number of eligible switches (single-family houses only):

$$ELIGIBLE_{y,eg,b,r} = \sum_{eg} \left(\frac{EQCRP90_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r}}{+ EQCREP_{y,eg,b,r}} \right) * \left(SWFACT_{eg} \right)$$
(B-32)

where

ELIGIBLE_{y,eg,b,r} is the number of replacements eligible to switch technology types by housing type

and Census division, and

 $SWFACT_{eq}$ is the fraction that may switch from equipment class eq.

The fuel switching weight for each equipment type is calculated as:

$$RPWEIGHT_{y,egsw,b,r} = \exp\left(RTSWBIAS_{egsw} + \left(RTWSBETA_{egsw} + \left(LFCY_{y,egsw,b,r,v} + RPINSCOST_{eg,egsw}\right)\right)\right)$$
(B-33)

where

 $RTSWBIAS_{eq}$ is a replacement technology choice model bias parameter (used only for

single-family homes),

RTSWBETA_{ea} is a replacement technology choice model log-linear parameter β (used

only for single-family homes),

LFCY_{v.eg,b,r,v} is a life-cycle cost for the equipment class by year, housing type, Census

division, and vintage, and

RPINSCOST_{ea.easw} is the installation cost associated with switching from equipment class

eg to equipment class egsw when equipment is replaced.

Shares are summed over all equipment types:

$$TOTSH_{y,b,r} = \sum_{egsw=1}^{egsw=11} RPWEIGHT_{y,egsw,b,r}$$
(B-34)

The totals are used to normalize the shares, so that they add to 100%:

$$RPSHARE_{y,egsw,b,r} = \frac{RPWEIGHT_{y,egsw,b,r}}{TOTSH_{y,b,r}}, if \ TOTSH_{y,b,r} > 0$$
 (B-35)
$$RPSHARE_{y,egsw,b,r} = 0, otherwise$$

where

RPSHARE_{v,eqsw,b,r} is the share that will switch to equipment class egsw on replacement by year, housing type, and Census division, is the weight assigned to each equipment class egsw by year, housing RPWEIGHT_{y,eqsw,b,r} type, and Census division, is the consumer preference parameter for switching to this equipment RTSWBIAS_{easw} class, RTSWBETA_{easw} is the set of parameter values that influence purchasing decisions, is the life-cycle cost of the equipment type switching to essw by year, $LFCY_{v,essw,b,r,v}$ housing type, Census division, and vintage, $RPINSCOST_{eq,eqsw}$ is the cost of switching from equipment class eq to eqsw upon

The equipment classes are then reconciled by *from* and *to* switching categories and redistributed to the correct equipment class.

The surviving post-base-year-vintage equipment in houses existing in the base year is computed as:

$$EQCSR90_{y,eg,b,r} = \sum_{t=baseyr+1}^{t=y-1} \left(\frac{(EQCRP90_{t,y,eg,b,r} + EQCRP90RP_{t,y,eg,b,r})}{*SVRTE_{y-t,L_{\min},L_{\max}} *HDR_{b}^{y-t}} \right)$$
(B-36)

where

is the equipment stock in homes existing in the base year that has been replaced after the base year and still survives, by housing type and Census division,

is the number of replacement (post-base-year-vintage) equipment units demanded each year in houses existing in the base year, by housing type and Census division,

EQCRP90RP_{t,eg,b,r} is the number of replacements of the EQCRP90 equipment units demanded each year, by housing type and Census division,

SVRTE_{y-t,Lmin,Lmax} is the equipment survival function,

*HDR*_b is the housing evolution rate by housing type, and y-t is the age of the equipment.

Surviving post-base-year equipment, originally purchased as additions or replacements in post-base-year houses, is calculated as:

$$EQCSUR_{y,eg,b,r} = \sum_{t=baseyr+1}^{t=y-1} \left(\underbrace{EQCADD_{t,eg,b,r} + EQCREP_{t,eg,b,r}}_{*SVRTE_{y-t,L_{\min},L_{\max}} * HDR_{b}^{y-t}} \right)$$
(B-37)

where

EQCSUR_{y,eq,b,r} is the surviving post-base-year equipment purchased as additions or

replacements in post-base-year houses, by housing type and Census

division,

EQCADD_{t,ea,b,r} is the quantity of post-base-year vintage equipment added to post-

base-year houses, by projection year, housing type and Census division,

SVRTE_{eg,y-t,Lmin,Lmax} is the equipment survival function,

EQCREP_{t,eq,b,r} is the number of equipment replacements of post-base-year equipment

in post-base-year houses, and

y-t represents the age of the equipment.

Shell integrity component

The shell integrity component uses three indices to capture the increases in the energy efficiency of building shells over time. One index corresponds to the existing housing stock, and two indices correspond to the post-base-year stock: one for housing constructed in the current year and the other for the average post-base-year stock. The existing shell index is adjusted each year to account for fuel price increases (decreases have no effect on shell integrity, i.e., shell efficiency only increases in response to fuel price changes) and technology improvements. The shell index for newly constructed homes is based on the choice of HVAC system, which includes the shell characteristics represented as an index, incorporating the size of the structure into the index as well. As the physical size of structures increases, the index will increase in value, while an increase in energy efficiency decreases the value of the index.

The existing housing heating shell index is calculated as:

$$EHSHELL_{y,f,r,b} = EHSHELL_{y-1,f,r,b}, if \ EHSHELL_{y,f,r,b} > EHSHELL_{y-1,f,r,b}$$

$$EHSHELL_{y,f,r,b} = LIMIT, if \ EHSHELL_{y,f,r,b} < LIMIT$$

$$EHSHELL_{y,f,r,b} = EHSHELL_{baseyr,f,r,b} * RSELAST_{y,f,r,alphaef1,ef2,ef3,baseyr}$$

$$*TECHG_{e,r,b}, otherwise$$
 (B-38)

where

EHSHELL_{y,f,r,b} is the shell integrity index for existing housing by year, fuel, Census division, and

housing type,

LIMIT is the maximum shell index efficiency index of 0.3 (i.e., maximum shell efficiency

is limited to a 70% improvement on the base-year value),

 $TECHG_{1,d,b}$ is a parameter that represents the annual increase in existing shell integrity due

to technology improvements, and

RSELAST is the short-term price elasticity function which distributes the price effect to

the current year (EF1) and the prices in the two preceding years with weights EF1, EF2, and EF3, and α , the total short-term price elasticity. This function assumes the consumer adjusts behavior more slowly than in a single year –

current model usage assumes the factors are 0.5, 0.35 and 0.15.

$$RSELAST_{y,f,r,\alpha,ef1,ef2,ef3,baseyr} = \frac{\left(PRICES_{f,r,y} / PRICES_{f,r,baseyr}\right)^{EF1*\alpha}}{*\left(PRICES_{f,r,y-1} / PRICES_{f,r,baseyr}\right)^{EF2*\alpha}}$$

$$*\left(PRICES_{f,r,y-2} / PRICES_{f,r,baseyr}\right)^{EF3*\alpha}$$

$$*\left(PRICES_{f,r,y-2} / PRICES_{f,r,baseyr}\right)^{EF3*\alpha}$$
(B-39)

The new housing heating shell index is calculated as:

$$NHSHELL_{y,f,r,b} = \sum_{t=basevy+1}^{t=y-1} (EQFSHRN_{t,es,b,r} * SHELLEFF_{t,es,b,r})$$
(B-40)

where

NHSHELL_{y,f,r,b} is the new housing units shell integrity index by year, fuel, Census division, and

housing type, and

SHELLEFF_{y,es,b,r} is the shell integrity factor associated with each HVAC package available.

The average post-base-year housing heating shell index is calculated as:

$$AHSHELL_{y,f,r,b} = \frac{\sum_{eg \in f} \left[NHSHELL_{y,r,r,b} * EQCADD_{y,eg,b,r} + AHSHELL_{y-1,f,r,b} \right]}{\sum_{eg \in f} \left[EQCREP_{y,eg,b,r} + EQCSUR_{y,eg,b,r} \right]}$$

$$(B-41)$$

where

AHSHELL_{v,f,r,b} is the average post-base-year heating shell index by year, fuel, Census division,

and housing type, equal to NHSHELL in the first year after the base year,

NHSHELL_{y,f,r,b} is the new housing units shell integrity index by year, fuel, Census division, and

housing type,

EQCADD_{y,eq,b,r} is the number of equipment units installed in new construction by

projection year, housing type and Census division,

EQCREPy,eg,b,r is the number of equipment replacements of post-base-year equipment in post-

base-year houses, and

EQCSURy,eg,b,r is the surviving post-base-year equipment purchased as additions or

replacement in post-base-year houses by projection year, housing type and

Census division.

In addition to the calculation shown above, the module places two additional restrictions upon AHSHELLy,f,r,b: it may never increase and it must not fall below LIMIT. If AHSHELLy,r,r,b is ever calculated to increase, its value is set to the prior year's value; if it falls below LIMIT, it is set equal to LIMIT.

Consumption and UEC component

Final end-use fuel consumption is determined by the fuels demanded by the equipment to provide housing units with the demanded services. For each equipment class, the UEC for new equipment, replacement equipment, and the average of all equipment is computed. New equipment UEC values are calculated as:

$$EQCNUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} * WTEQCEFFN_{y,eg,b,r}$$

$$* RTBASEFF_{baseyr,eg} * HDDFACT_{y,r} * EXSQFTADJ_{y,b,r}$$
(B-42)

where

 $EQCNUEC_{y,eq,b,r}$ is the unit energy consumption for new equipment by projection year,

housing type, and Census division,

WTEQCEFFN_{V,eq,b,r} is the equipment class efficiency weighted by the market share of the

specific equipment as computed in the logistic function in the

technology choice component by housing type and Census division,

RTBASEFF_{baseyr,eg} is the base-year stock-average efficiency of the equipment class, $EQCUEC_{r,eg,b}$ is unit energy consumption for original base-year stock of the

equipment class by Census division and housing type,

HDDFACT_{y,r} is the heating degree day adjustment factor by Census division to

correct to normal weather relative to the RECS survey year, and

*EXSQFTADJ*_{y,b,r} is the adjustment for increasing floor area of new houses.

Replacement equipment UEC values are calculated as:

$$EQCRUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} *WTEQCEFFR_{y,eg,b,r}$$

$$*RTBASEFF_{baseyr,eg} *HDDFACT_{y,r}$$
(B-43)

where

EQCRUEC_{y,eq,b,r} is the unit energy consumption for replacement equipment by housing

type and Census division,

RTBASEFF_{basevr,ea} is the efficiency of the weighted average of retiring units from the base-

year existing stock, and

WTEQCEFFR_{v.ea.b.r} is the replacement equipment efficiency weighted by the market share

of the specific equipment as computed in the logistic function in the technology choice component by housing type and Census division.

And the UEC for the surviving stock must be adjusted, according to

$$EQCSUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} * HDDFACT_{y,r} * \frac{RTBASEFF}{RTBASEFF}_{baseyr,eg}$$
(B-44)

where

*EQCSUEC*_{y,eg,b,r} is the average unit energy consumption of the original base-year equipment stock that remains after the replacements have taken place.

The average UEC for all equipment in the existing stock is calculated as:

$$EQCAUEC_{y,eg,b,r} = EQCNUEC_{y,eg,b,r}$$
, if $y = baseyr + 1$ otherwise,

otherwise,
$$\frac{\left(EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} + EQCRDD_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r}\right) * EQCNUEC_{y,eg,b,r}}{EQCSR90_{y,eg,b,r} + EQCSUR_{y,eg,b,r}} \\
+ (EQCSR90_{y,eg,b,r} + EQCSUR_{y,eg,b,r}) \\
* EQCAUEC_{y-1,eg,b,r} \\
+ EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} \\
+ EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} \\
+ EQCRP90RP_{y,eg,b,r} + EQCSR90_{y,eg,b,r} \\
+ EQCSUR_{y,eg,b,r} + EQCRP90_{y,eg,b,r}$$
(B-45)

where

EQCAUEC_{y,eg,b,r} is the average unit energy consumption for all post-base-year equipment categories.

The final step of this algorithm is to calculate consumption for the end-use service category. The consumption during the first year of the projection is computed initially as:

$$HTRCON_{y=baseyr,f,r} = \sum_{b} \sum_{eg} \begin{bmatrix} EQCESE_{y,eg,b,r} * ECQCUEC_{eg,b,r} * EHSHELL_{y,f,r,b} \\ + EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} * NHSHELL_{y,f,r,b} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} * EHSHELL_{y,f,r,b} \\ * RSELAST(f,r,\alpha,EF1,EF2,EF3,baseyr) \end{bmatrix}$$
(B-46)

Subsequent annual consumption (for $y \ge baseyr+2$) is computed as:

$$\sum_{b} \sum_{eg} \begin{bmatrix} EQCESE_{y,eg,b,r} * ECQCUEC_{eg,b,r} * EHSHELL_{y,f,r,b} \\ + EQCADD_{y,eg,b,r} * EQCHVUEC_{y,eg,b,r} * NHSHELL_{y,f,r,b} * RBN_{y,eg,b,r} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} * EHSHELL_{y,f,r,b} * RBN_{y,eg,b,r} \\ + EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} * EHSHELL_{y,f,r,b} * RBN_{y,eg,b,r} \\ + EQCSR90_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} * EHSHELL_{y,f,r,b} * RBA_{y,eg,b,r} \\ + EQCREP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} * AHSHELL_{y,f,r,b} * RBN_{y,eg,b,r} \\ + EQCSUR_{y,eg,b,r} * EQCAHVUEC_{y,eg,b,r} * AHSHELL_{y,f,r,b} * RBA_{y,eg,b,r} \\ * RSELAST (f,r,\alpha,EF1,EF2,EF3,baseyr) \end{bmatrix}$$

where

 $HTRCON_{y,f,r}$ RSELAST

is heating energy consumption by year, fuel type, and region, is the short-term price elasticity function with distributed lag weights EF1, EF2, and EF3 and the total short-term price elasticity, α , described in (B-39), and the rebound effect associated with increasing equipment efficiency for a particular equipment class causes a corresponding change in the price elasticity for the class represented as

RBN
$$_{r,eg,b,r}$$
= WTEQCEFFN $_{y,eg,b,r}$ * RTBASEFF $_{baseyr,eg}$ $^{\alpha_1}$ (B-48)

$$RBR_{r,eg,b,r} = WTEQCEFFR_{y,eg,b,r} * RTBASEFF_{baseyr,eg}^{\alpha_1}$$
(B-49)

$$RBA_{r,eg,b,r} = WTEQCEFFA_{y,eg,b,r} * RTBASEFF_{baseyr,eg}^{\alpha_1}$$
 (B-50)

where

is the rebound effect factor for surviving equipment, $RBA_{v,eq,b,r}$ $RBR_{y,eg,b,r}$ is the rebound effect factor for replacement equipment, is the rebound effect factor for new equipment, and $RBN_{v,eq,b,r}$ is the rebound effect elasticity, presently valued at -0.15. α_1

Consumption by furnace fans and boiler pumps, FANCON, is computed in a similar fashion for those systems that require them.

RCLTEC (Air conditioning equipment choice component)

Space cooling equipment choice begins with the calculation of a factor that adjusts for biased temperatures in either the base year or in the year under consideration. For each region r,

$$CDDFACT_{y,r} = \left(\frac{CDDADJ_{y,r}}{CDDADJ_{baseyr,r}}\right)^{1.75}$$
(B-51)

where

 $CDDFACT_{y,r}$ is a set of regional factors to be used in this year to adjust for abnormal

temperatures either in this year or in the base year,

CDDADJ_{v,r} are regional population-adjusted cooling degree days by Census division and

historical year, with projection years, from the KDEGDAY.TXT file, and

is an exponent that best adjusted values to recent historical data.

Operating costs for cooling equipment are calculated like those for heating equipment, with the exception of the degree-day factor:

$$OPCOST_{y,es,b,r,v} = PRICES_{f,r,y} * EQCUEC_{y,eg,b} *$$

$$CDDFACT_{r,y} * RTEFFAC_{eg,v} * CSHELL_{y-l,r,v}$$
(B-52)

where

 $OPCOST_{y,es,b,r,v}$ is the operating cost for the air conditioner equipment type by housing type,

Census division, and vintage in the projection year,

PRICES_{f.r.v} are the fuel prices by region and projection year, from the NEMS Integrating

Module,

 $EQCUEC_{r,b}$ is the electricity unit energy consumption of base-year room air conditioning

equipment by Census division and housing type,

RTEFFAC_{eq,v} is the efficiency adjustment for the generic equipment type, and

CSHELL_{y-1,r,v} is the shell efficiency adjustment to account for building shell improvements

over time (which reduce cooling loads).

The following variables are computed as in the equations indicated:

*LFCY*_{y,es,b,r,v} is the air conditioner type's life-cycle cost by year, housing type, and Census

division. It is computed as in (B-16) above.

EQWTN_{y,es,b,r} is the equipment weight for new equipment types by housing type, Census

division and year. It is computed as in (B-20) above.

EQWTR_{y,es,b,r} is the equipment weight for replacement equipment types by housing type,

Census division and year. It is computed as in (B-21) above.

 $TOTEWTN_{y,eq,b,r}$ is the sum of equipment type weights for the new equipment class. It is

computed as in (B-22) above.

TOTEWTR_{y,eq,b,r} is the sum of equipment type weights for the replacement equipment class. It is

computed as in (B-23) above.

Market shares for equipment types within the cooling equipment classes distinguish between heat pumps, whose numbers have been determined in the heating choice component, and other cooling equipment. For heat pumps,

$$\begin{split} NEQTSHR_{y,es,b,r} &= NEQTSHR_{y,RTTYPNTR_{es},b,r} \\ REQTSHR_{y,es,b,r} &= REQTSHR_{y,RTTYPNTR_{es},b,r} \end{split} \tag{B-53}$$

and for other cooling equipment,

$$NEQTSHR_{y,es,b,r} = \frac{EQWTN_{y,es,b,r}}{TOTEWTN_{y,eg,b,r}}$$
(B-54)

$$REQTSHR_{y,es,b,r} = \frac{EQWTR_{y,es,b,r}}{TOTEWTR_{y,eg,b,r}}$$
(B-55)

where

NEQTSHR_{y,es,b,r} is the new market share for the new air conditioner equipment type by year,

housing type and Census division,

REQTSHR_{y,es,b,r} is the new market share for the replacement air conditioner equipment type by

year, housing type and Census division,

RTTYPNTR_{es} is the equipment type pointer for each equipment class,

TOTEWTN_{v.ea,b.r} is the sum of equipment type weights for the new equipment class,

TOTEWTR_{y,eq,b,r} is the sum of equipment type weights for the replacement equipment class,

 $EQWTN_{y,es,b,r}$ is the equipment weight for new equipment, and $EQWTR_{y,es,b,r}$ is the equipment weight for replacement equipment.

Weighted average inverse efficiencies of the types of cooling equipment into their classes are calculated exactly as in the heating component:

WTEQCEFFN_{y,eq,b,r} is the weighted average inverse efficiency of new equipment types

within each equipment class by year, housing type, and Census division,

computed as in (B-26).

WTEQCEFFR_{v,eq,b,r} is the weighted average inverse efficiency of replacement equipment

types within each equipment class by year, housing type, and Census

division, computed as in (B-27).

RCLADD (Additions and replacements of cooling equipment component)

Given the complex dependencies between choices of heating and cooling equipment, the cooling additions logic begins very differently from that for heating. Central air conditioner additions are calculated from housing additions and a set of saturation levels:

$$EQCADD_{y,CAC,b,r} = HSEADD_{y,b,r} * CACSAT_{b,r}$$
(B-56)

where

EQCADD_{V,CAC,b,r} is the number of central air conditioners (CAC) added to new (post-base-year)

housing units by year, housing type, and Census division,

HSEADD_{y,b,r} is the number of housing units added by year, housing type and Census division,

and

 $CACSAT_{b,r}$ is the market penetration level or saturation of the market for central air

conditioning equipment by housing type and Census division.

For room air conditioners, there are similar saturation levels:

$$EQCADD_{y,RAC,b,r} = HSEADD_{y,b,r} * RACSAT_{b,r} * RACUNTS_{b,r}$$
(B-57)

where

EQCADD_{y,RAC,b,r} is the number of room air conditioners (RAC) added to new (post-base-year)

housing units by year, housing type, and Census division,

HSEADD_{v,b,r} is the amount of housing additions by year, housing type and Census division,

 $RACSAT_{b,r}$ is the market penetration level or saturation of the market for room air

conditioning equipment by housing type and Census division, and

RACUNTS_{b.r} is the number of room air conditioners per housing unit by housing type and

Census division.

For heat pumps, however, additions are determined by the number of associated heat pumps installed in the heating additions component:

$$EQCADD_{y,HP,b,r} = EQCADD_{y,RTCLPNTR_{eg}b,r}$$
(B-58)

where

EQCADD_{y,t,HP,b,r} is the number of heat pumps used for space heating added to new housing units

by year, housing type, and Census division, and

RTCLPNTR_{eg} is the pointer to the heating equipment class associated with the cooling

equipment class.

The number of new homes with central air conditioners also includes new homes with electric heat pumps. To determine the number of central air conditioners needed, electric heat pumps are first removed. If added electric heat pumps exceed the number of added central air conditioners determined by the saturation rate, 10% of central air conditioners are left in the additions:

$$EQCADD_{y,CAC,b,r} = EQCADD_{y,CAC,b,r} - EQCADD_{y,HP,b,r}$$
(B-59)

where

 $EQCADD_{y,t,eg,b,r}$ is the number of central air conditioners in each equipment class added to new (post-base-year) housing units by year, housing type, and Census division, and

eg is the space cooling equipment class.

Surviving equipment follows the same dichotomy as the other calculations, with a different method for determining the number of surviving heat pumps from that used for calculating the surviving stock for other types of cooling equipment. For heat pumps, the stock is equated to that calculated in the space heating subroutines:

$$EQCSR90_{y,eg,b,r} = EQCSR90_{y,RTCLPNTReg,b,r}$$
(B-60)

where

EQCSR90_{v,ea,b,r} is the surviving post-base-year cooling equipment in existing housing units by

year, housing type, and Census division, equated to the stock calculated in the

space heating subroutines, and

RTCLPNTR is a Fortran pointer that maps the heat pump stock from the heating subroutine

into the correct heat pump stock in the cooling subroutine.

For single-family houses with central air conditioning, there is a penetration rate that describes new units added in existing houses:

$$EQCND90_{y,eg,b,r} = EQCND90_{y,eg,b,r} *CACPR_r *HDR_b$$
(B-61)

where

 $EQCND90_{y,eq,b,r}$ is the number of air conditioning units needed in pre-2006 housing each year,

by housing type, and Census division,

 HDR_b is the housing demolition rate by housing type, and

CACPR_r is the regional penetration rate for central air conditioners from the RSMISC.TXT

file.

The replacement equipment types, EQCREP, EQCRP90, and EQCRP90RP are computed as in (B-29), (B-30), and (B-31), respectively. The surviving new additions, EQCSUR, is computed as in (B-37) above.

Because replacements for heat pumps in the cooling end use equal replacements for heat pumps in the heating end use and switching was allowed on replacement of heat pumps used for heating, switching on replacement of heat pumps in the cooling end use occurred in RHTRADD (the subroutine for replacing heating equipment types). No switching on replacement of central or room air conditioners is allowed, because these numbers are based on historical data. Therefore, Subroutine RCLADD does not call Subroutine REPLACE.

RCLCON (Cooling energy consumption component)

Energy consumption for space cooling is calculated much like the comparable quantities for space heating. Space cooling equipment consumption begins with the calculation of a factor that adjusts for biased temperatures in either the base year or in the year under consideration, in each region, as computed in (B-51) above.

Unit energy consumption is calculated for each of the vintages of homes. For surviving equipment in existing vintage homes,

$$EQCSUEC_{y,eg,b,r} = EQCUEC_{y,eg,b} * CDDFACT_{y,r} * \frac{RTBASEFF}{RTBASEFF}_{baseyr,eg}$$
(B-62)

where

EQCSUEC_{v.eg.b.r} is the unit energy efficiency of surviving equipment in existing vintage homes, by

year, equipment class, housing type, and Census division,

EQCUEC_{r,eg,b} is the unit energy efficiency of equipment in homes that existed in the base

year, by Census division, equipment class, and housing type,

CDDFACT_r are the regional cooling degree day adjustment factors, and RTBASEFF_{y,eg} are the annual average efficiencies for the equipment classes.

For new equipment,

$$EQCNUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} *WTEQCEFFN_{y,eg,b,r}$$

$$*RTBASEFF_{baseyr,eg} *CDDFACT_{y,r} *EXSQFTADJ_{y,b,r}$$
(B-63)

where

EQCNUEC_{v.ea,b,r} is the unit energy consumption by year for new equipment by housing

type, and Census division,

WTEQCEFFN_{v.ea.b.r} is the equipment inverse efficiency by year, equipment class, housing

type, and Census division,

RTBASEFF_{y,eq} is the average efficiency of the equipment class,

EQCUEC_{r,eq,b} is unit energy consumption for equipment in existing housing by Census

division, equipment class, and housing type,

*CDDFACT*_r is the cooling degree day adjustment factor by Census division to

correct for differences in weather from the RECS survey year, and

EXSQFTADJ_{y,b,r} adjusts for the increasing average floor area of new homes, as

compared with the RECS base year.

Replacement equipment UEC values are calculated in the same way as new equipment, but without the floor area adjustment:

$$EQCRUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} *WTEQCEFFR_{y,eg,b,r}$$

$$*RTBASEFF_{baseyr,eg} *CDDFACT_{y,r}$$
(B-64)

where

EQCRUEC_{v,eq,b,r} is the unit energy consumption for replacement equipment by housing

type and Census division,

RTBASEFF_{baseyr,eg} is the efficiency of the weighted average of retiring units from the

existing stock, and

WTEQCEFFR_{v,eq,b,r} is the replacement equipment inverse efficiency weighted by the

market share of the equipment type (as computed in the technology

choice component) by housing type and Census division.

The average UEC, EQCAUEC, for all cooling equipment is calculated as in (B-45) above.

Cooling shell efficiency is calculated similarly to heating shell efficiency computed in equations (B-38) through (B-41).

The final step of this component is to calculate consumption for the service category. This is accomplished in two steps. The first year of the projection is computed as

$$COOLCN_{y=baseyr+1,f,r} =$$

$$\sum_{b}\sum_{eg}\begin{bmatrix} EQCESE_{baseyr+1,eg,b,r}*ECQCUEC_{eg,b,r}*ECSHELL_{baseyr+1,r,b} \\ + EQCADD_{baseyr_{-}+1,eg,b,r}*EQCNUEC_{baseyr+1,eg,b,r}*NCSHELL_{baseyr+1,r,b} \\ + EQCRP90_{baseyr+1,eg,b,r}*EQCRUEC_{Bsaeyr+1,eg,b,r}*ECSHELL_{baseyr+1,r,b} \\ *RSELAST(f,r,\alpha,EF1,EF2,EF3,baseyr) \end{bmatrix}$$
(B-65)

Subsequent consumption is computed as

$$COOLCN_{y,f,r} =$$

$$\sum_{b} \sum_{eg} \begin{bmatrix} EQCESE & y,eg,b,r * ECQCUEC_{eg,b,r} * ECSHELL_{y,r} \\ + EQCADD & y,eg,b,r * EQCNUEC_{y,eg,b,r} * NCSHELL_{y,r,b} * RBN & y,eg,b,r \\ + EQCRP90 & y,eg,b,r * EQCRUEC_{y,eg,b,r} * ECSHELL_{y,r,b} * RBR & y,eg,b,r \\ + EQCRP90RP & y,eg,b,r * EQCNUEC_{y,eg,b,r} * ECSHELL_{y,r,b} * RBN & y,eg,b,r \\ + EQCSR90 & y,eg,b,r * EQCAUEC_{y,eg,b,r} * ECSHELL_{y,r,b} * RBA_{y,eg,b,r} \\ + EQCREP & y,eg,b,r * EQCNUEC_{y,eg,b,r} * ACSHELL_{y,r,b} * RBN & y,eg,b,r \\ + EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} * ACSHELL_{y,r,b} * RBA_{y,eg,b,r} \\ + EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} * ACSHELL_{y,r,b} * RBA_{y,eg,b,r} \end{bmatrix}$$

$$* RSELAST (f,r,\alpha,EF1,EF2,EF3,baseyr)$$

where

RSELAST is the short-term price elasticity function with distributed lag weights EF1, EF2, and EF3, and the total short-term price elasticity, α , described in (B-39).

The *rebound effect* that was introduced in the space heating section in equations (B-48) through (B-50) is also represented in the space cooling consumption equation.

RCWTEC (Clothes washing technology choice component)
Compute current year operating costs:

$$OPCOST_{y,es,b,r,v} = PRICES_{f,r,y} * EQCUEC_{y,eg,b} * \frac{RTBASEFF_{baseyr,eg}}{RTEQEFF_{ac}}$$
(B-67)

where

*OPCOST*_{v,es,b,r,v} is the operating cost for the equipment type by year, housing type,

Census division, and vintage,

PRICES_{f,r,y} is the fuel prices for the equipment from NEMS, by fuel, by region and

projection year,

EQCUEC_{r.ea,b} is the unit energy consumption by Census division, equipment class and

housing type,

RTEQEFF_{es} is the equipment efficiency, and

RTBASEFF_{baseyr,eq} is the base-year stock-average efficiency.

The following variables are computed as in the equations indicated:

LFCY_{y,es,b,r,v} is the clothes washer's life-cycle cost by year, housing type, Census division, and vintage. It is computed as in (B-16) above.

 $EQWTN_{y,es,b,r}$ is the equipment weight for new equipment type by housing type, Census

division, and year. It is computed as in (B-20) above.

is the equipment weight for replacement equipment by housing type, Census EQWTR_{y,es,b,r}

division, and year. It is computed as in (B-21) above.

TOTEWTN_{y,eg,b,r} is the sum of equipment weights for the new equipment class. It is computed as

in (B-22) above.

TOTEWTR_{y,eg,b,r} is the sum of equipment weights for the replacement equipment class. It is

computed as in (B-23) above.

Market shares for new and replacement clothes washers are derived by:

$$NEQTSHR_{y,es,b,r} = \frac{EQWT_{y,es,b,r}}{TOTEWT_{y,eg,b,r}}$$
(B-68)

for es in eg

where

 $NEQTSHR_{y,es,b,r}$ is the new market share of clothes washer equipment types by housing type and

Census division in the current year,

is the sum of equipment weights for the new equipment class, and

 $TOTEWT_{eg}$ $EQWT_{es}$ is the equipment weight for new equipment.

Because efficiency improvements in clothes washers tend to affect the amount of hot water used in a housing unit, establishing a link between clothes washers and water heaters is essential. The impact of the load reduction with respect to installing more efficient clothes washers is calculated as follows:

$$TEMP = \sum_{es \in eg} EQWT_{y,es,b,r}$$

$$\sum_{es \in eg} \left(EQWT_{y,es,b,r} * LOADADJ_{es} \right)$$

$$NCWLOAD_{y,eg,b,r} = \frac{\sum_{es \in eg} \left(EQWT_{y,es,b,r} * LOADADJ_{es} \right)}{TEMP}, \quad if \ TEMP > 0$$

$$NCWLOAD_{y,eg,b,r} = NCWLOAD_{y-1,eg,b,r}, \quad otherwise$$
(B-69)

where

NCWLOAD_{v.ea.b.r} is the weighted average load adjustment of new clothes washers with respect to

water heating load in the current year by housing type and Census division,

is the equipment weight for each type of new equipment, and $EQWT_{y,es,b,r}$

LOADADJ_{es} is the fraction of hot water needed to provide the same level of service, relative

to the base-year average.

RCWADD (Clothes washing additions component)

New clothes washing equipment is calculated using a saturation level for newly purchased equipment:

$$EQCADD_{y,eg,b,r} = HSEADD_{y,b,r} * \frac{WASHNEW_{b,r}}{100}$$
(B-70)

where

EQCADD_{y,eq,b,r} is the amount of new (post-base-year-vintage) equipment added in new housing

units in the current year by housing type and Census division,

HSEADD_{y,b,r} is the number of new housing additions in the year by housing type and Census

division, and

WASHNEW_{b,r} is the share of clothes washers in newly constructed houses by housing type and

Census division in the current year.

The next step is to calculate the numbers of clothes washers of each vintage category. The following variables were computed as in the equations indicated:

EQCSR90_{V,eq,b,r} is the surviving post-base-year vintage equipment in existing housing

units in the current year by housing type and Census division. It is

computed as in (B-36) above.

EQCSUR_{y,eg,b,r} is the surviving new (post-base-year-vintage) equipment in the current

year by housing type and Census division. It is computed as in (B-37)

above.

EQCREP_{v.ea.b.r} is the number of replacement units (post-base-year-vintage) equipment

demanded in post-base-year-vintage housing units by housing type and

Census division. It is computed as in (B-29) above.

EQCRP90_{v,ea,b,r} is the number of replacement units demanded in existing housing units

each year by housing type and Census division. It is computed as in (B-

30) above.

EQCRP90RP_{v.ea.b,r} is the number of replacement units for the EQCRP90 units demanded

each year by housing type and Census division. It is computed as in (B-

31) above.

RCWCON (Clothes washing energy consumption component)

To calculate the energy consumption attributable to clothes washers, first calculate the unit energy consumption for each vintage of home. The calculations are similar to those presented in equations (B-42) through (B-45).

EQCNUEC_{y,eg,b,r} is the unit energy consumption by year for new equipment by housing type and

Census division.

EQCRUEC_{y,eg,b,r} is the unit energy consumption by year for replacement equipment by housing

type and Census division,

EQCSUEC_{y,eg,b,r} is the UEC for surviving base-year equipment in each equipment class, by

housing type and Census division, and

EQCAUEC_{y,eg,b,r} is the average unit energy consumption for all equipment by housing type and

Census division.

Finally, the energy consumption calculation is simpler than the calculation for most of the other end uses:

$$CSWCON_{y,r} = \sum_{b,eg} \begin{pmatrix} EQCESE_{y,eg,b,r} * EQCUEC_{eg,b,r} \\ + EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} \\ + EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \end{pmatrix}, if y = baseyr + 1$$
(B-71)

$$CSWCON_{y,r} =$$

$$\sum_{b,eg} \begin{pmatrix} EQCESE_{y,eg,b,r} * EQCUEC_{eg,b,r} \\ + EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} \\ + EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSR90_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} \\ + EQCREP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSUR_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \end{pmatrix}, \quad if \quad y > baseyr + 1$$

$$+ EQCSUR_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} \\ \end{pmatrix}$$

RDWTEC (Dishwashing technology choice component)

The following variables are computed as in the equations indicated:

$OPCOST_{y,es,b,r,v}$	is the operating cost for the equipment type by year, housing type, Census
	division, and vintage. It is computed as in (B-67) above.
$LFCY_{y,es,b,r,v}$	is the dishwasher's life-cycle cost by year, housing type, Census division, and
	vintage. It is computed as in (B-16) above.
$EQWTN_{y,es,b,r}$	is the equipment weight for new equipment type by year, housing type, and
	Census division. It is computed as in (B-20) above.
$EQWTR_{y,es,b,r}$	is the equipment weight for replacement equipment by year, housing type, and
	Census division. It is computed as in (B-21) above.
$TOTEWTN_{y,eg,b,r}$	is the sum of equipment weights for the new purchase equipment class. It is
	computed as in (B-22) above.
$TOTEWTR_{y,eg,b,r}$	is the sum of equipment weights for the replacement purchase equipment class.

It is computed as in (B-23) above.

Market shares for new and replacement dishwashers are next:

$$NEQTSHR_{y,es,b,r} = \frac{EQWT_{y,es,b,r}}{TOTEWT_{y,eg,b,r}}$$
(B-73)

where

NEQTSHR_{y,es,b,r} is the new market share of dishwasher equipment types by housing type and

Census division in the current year,

 $TOTEWT_{eq,b,r}$ is the sum of equipment weights for the new equipment class by housing type

and Census division, and

*EQWT*_{y,es,b,r} is the equipment weight for new equipment by year, housing type, and Census

region.

RDWADD (Dishwashing additions component)

New dishwashing equipment is calculated using a saturation level for newly purchased equipment:

$$EQCADD_{y,eg,b,r} = HSEADD_{y,b,r} * DISHNEW_{b,r}$$
(B-74)

where

EQCADD_{y,eg,b,r} is the amount of new (post-base-year-vintage) equipment added in new housing

units in the current year by housing type and Census division,

 $HSEADD_{v,b,r}$ is the number of new housing additions in the year by housing type and Census

division, and

DISHNEW_{b,r} is the share of dishwashers in newly constructed houses by housing type and

Census division in the current year. Note that dishwashers have a single

equipment class eliminating the need for an eq subscript.

The next step is to calculate the numbers of dishwashers of each vintage category. The following variables were computed as in the equations indicated:

EQCSR90_{y,eg,b,r} is the surviving post-base-year vintage equipment in existing housing

units in the current year by housing type and Census division. It is

computed as in (B-36) above.

EQCSUR_{y,eg,b,r} is the surviving new (post-base-year-vintage) equipment in the current

year by housing type and Census division. It is computed as in (B-37)

above.

 $EQCREP_{y,eg,b,r}$ is the number of replacement units (post-base-year-vintage) equipment

demanded in post-base-year-vintage housing units by housing type and

Census division. It is computed as in (B-29) above.

EQCRP90_{y,eg,b,r} is the number of replacement units demanded in existing housing units

each year by housing type and Census division. It is computed as in (B-

30) above.

EQCRP90RP_{v,eq,b,r}

uses:

is the number of replacement units for the EQCRP90 units demanded each year by housing type and Census division. It is computed as in (B-31) above.

RDWCON (Dishwashing energy consumption component)

To calculate the energy consumption attributable to dishwashers, first calculate the unit energy consumption for each vintage of home. The calculations are similar to those presented in equations (B-42) through (B-45).

type and Census division.

$EQCSUEC_{y,eg,b,r}$	is the UEC for surviving base-year equipment in each equipment class, by housing type and Census division,
$EQCNUEC_{y,eg,b,r}$	is the unit energy consumption by year for new equipment by housing
EQCRUEC _{y,eg,b,r}	type and Census division, is the unit energy consumption by year for replacement equipment by
$EQCAUEC_{y,eg,b,r}$	housing type and Census division, and is the average unit energy consumption for all equipment by housing

Finally, the energy consumption calculation is simpler than the calculation for most of the other end

$$DSWCON_{y=2006r} = \sum_{b,eg} \begin{pmatrix} EQCESE_{y,eg,b,r} * EQCUEC_{eg,b,r} \\ + EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} \\ + EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \end{pmatrix}, \quad if \quad y = baseyr + 1$$

$$(B-75)$$

$$DSWCON_{y,r} = \left(\begin{array}{l} EQCESE_{y,eg,b,r} * EQCUEC_{eg,b,r} \\ + EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} \\ + EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSR90_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} \\ + EQCRP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSUR_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} \end{array} \right), \quad if \quad y > baseyr + 1$$

RWHTEC (Water heating equipment choice component)

New water heaters are assumed to be distributed in proportion to associated space heating equipment, where the association between water heating equipment and space heating equipment is specified by

the user in the *RTCLPNTR_{eg}* pointer for each water heating equipment class in the RSCLASS.TXT file. Replacement water heaters are not so constrained in single-family housing. There are five equipment classes for water heaters: natural gas, electric, distillate fuel oil, LPG, and solar thermal.

The component first adds up the market shares of all space heating equipment:

$$TOTN_{b,r} = \sum_{eg} HSYSSHR_{y,eg,b,r}$$
(B-77)

where

 $TOTN_{b,r}$ is the sum of the current-year market shares for space heating equipment

classes by housing type and Census division, and

HSYSSHR_{y,eq,b,r} is the current-year market share for space heating equipment classes by housing

type and Census division.

New water heater market shares are therefore calculated by the sum of the market shares of the associated heating equipment:

$$NH2OSH_{y,b,r} = \frac{\sum_{eg} HSYSSHR_{y,RTCLEQCL_{SH} = RTCLPNTR_{WH},b,r}}{TOTN_{b,r}}$$
(B-78)

where

 $NH2OSH_{y,b,r}$ is the market share of each new water heater class by housing type and Census

division,

 $TOTN_{b,r}$ is the sum of the current-year market shares for space heating equipment

classes by housing type and Census division,

 $HSYSSHR_{y,eg,b,r}$ is the current-year market share of the space heating equipment class by

housing type and Census division,

 $RTCLEQCL_{SH}$ is the equipment class number for the space heater class, and $RTCLPNTR_{WH}$ is the pointer to a space heater class from a water heater class.

The following variables are computed as in the equations indicated:

OPCOST_{v,es,b,r,v} is the operating cost for the water heater equipment type by housing type,

Census division, vintage, and year. It is computed as in (B-67).

*LFCY*_{y,es,b,r,v} is the water heater type's life-cycle cost by year, housing type, Census division,

and vintage. It is computed as in (B-16).

EQWTN_{y,es,b,r} is the equipment weight for new equipment types by housing type, Census

division, and year. It is computed as in (B-20).

 $EQWTR_{v.es.b.r}$ is the equipment weight for replacement equipment types by housing type,

Census division, and year. It is computed as in (B-21).

 $TOTEWTN_{y,eg,b,r}$ is the sum of the equipment types' weights for the new equipment class. It is

computed as in (B-22).

TOTEWTR_{y,eg,b,r} is the sum of the equipment types' weights for the replacement equipment

class. It is computed as in (B-23).

EQFSHRN_{y,f,b,r} is the fuel share of new equipment type by year, housing type and Census

division. It is computed as in (B-24).

EQFSHRR $_{y,f,b,r}$ is the fuel share of replacement equipment type by year, housing type and Census division. It is computed as in (B-25).

The fuel shares are finally defined:

$$NEQTSHR_{v,f,b,r} = EQFSHRN_{v,es,b,r}$$
 (B-79)

$$REQTSHR_{v,f,b,r} = EQFSHRR_{v,es,b,r}$$
 (B-80)

where

NEQTSHR_{y,f,b,r} is the fuel share of new water heaters by fuel, housing type, and Census

division, and

REQTSHR_{v,f,b,r} is the fuel share of replacement water heaters by fuel, housing, type and Census

division.

Weighted average class efficiencies by fuel can then be calculated from the individual equipment types for new and replacement equipment, using exactly the same formulas as for space heating equipment, as shown in equations (B-26) and (B-27):

WTEQCEFFN_{v,ea,b,r} is the weighted average inverse efficiency for new water heating

equipment classes by year, housing type, and Census division, and

 $WTEQCEFFR_{y,eg,b,r}$ is the weighted average inverse efficiency for replacement water

heating equipment classes by year, housing type, and Census division.

REUADD (Water heating and cooking additions and replacements component)

There is only one component in the RDM for addition and replacement of water heating equipment and cooking equipment.

The first operation is to calculate the total equipment in existing housing:

$$\begin{split} EQCND90_{y,eg,b,r} &= EQCESE_{baseyr,eg,b,r}*HDR_b \quad , if \quad y = baseyr + 1 \\ &EQCND90_{y,eg,b,r} &= EQCESE_{y-1,eg,b,r}*HDR_b \quad , if \quad y > baseyr + 1 \end{split} \tag{B-81}$$

where

EQCND90_{y,eg,b,r} is the total equipment in existing housing each year by housing type and Census division,

EQCESE_{baseyr,eg,b,r} is the existing equipment stock in existing housing units in the base year by

housing type and Census division, and

 HDR_b is the housing demolition rate by housing type.

Next, purchases are calculated for new housing,

$$EQCADD_{v,eg,b,r} = HSEADD_{v,b,r} * SHARE_{v,eg,b,r}$$
(B-82)

where

EQCADD_{y,eg,b,r} is the number of new units originally purchased for new housing additions by

year, housing type, and Census division,

HSEADD_{v,b,r} is the number of housing additions by year, housing type, and Census division,

and

SHARE y,eq,b,r is the share of the particular equipment for which the component has been

called, NH2OSH_{y,eg,b,r} or NCKSH_{y,eg,b,r}.

*NH2OSH*_{y,eg,b,r} is the market penetration level or saturation of the market for water

heaters by housing type and Census division, and

 $NCKSH_{y,eg,b,r}$ is the market penetration level or saturation of the market for cookstoves by housing type and Census division.

EQCSR90_{v,eq,b,r} is the surviving post-base-year vintage equipment in existing housing

units in the current year by housing type and Census division. It is

computed as in (B-36) above.

EQCSUR_{y,eq,b,r} is the surviving new (post-base-year-vintage) equipment in the current

year by housing type and Census division. It is computed as in (B-37)

above.

The following variables are computed as in the equations indicated:

 $EQCREP_{y,eq,b,r}$ is the number of replacement units (post-base-year-vintage) equipment

demanded in post-base-year-vintage housing units by housing type and

Census division. It is computed as in (B-29) above.

EQCRP90_{v,eq,b,r} is the number of replacement units demanded in existing housing units

each year by housing type and Census division. It is computed as in (B-

30) above.

EQCRP90RP_{y,eq,b,r} is the number of replacement units for the EQCRP90 units demanded

each year by housing type and Census division. It is computed as in (B-

31) above.

RWHCON (Water heating energy consumption component)

Energy consumption for water heating is calculated much like the comparable quantities for space heating. Some of the most important determinants of the amount of hot water consumption in housing units are the number of inhabitants and the usage and efficiency of clothes washers. The component therefore calculates an average housing unit size that will be used with an elasticity to account for this determinant:

$$HHSIZE_{y,r} = \frac{MC - NP16A_{r,y}}{\sum_{b} \left(EH_{y,b,r} + NH_{y,b,r}\right)}$$
(B-83)

where

HHSIZE_{v.r} is the average number of persons over age 16 per housing unit by year and

region,

MC_NP16A_{r,v} is the number of persons over age 16 by year and region, from the NEMS

Macroeconomic Activity Module,

 $EH_{v,b,r}$ is the number of existing vintage homes existing in year y, from the RSMISC.TXT

file, and

 $NH_{y,b,r}$ is the number of post-base-year-vintage homes remaining in year y, from the

NEMS Macroeconomic Activity Module, as shown in equation (B-3).

Unit energy consumption is calculated for housing vintages. First, for the surviving base-year homes,

$$EQCSUEC_{r,eg,b,r} = \frac{EQCSUEC_{r,eg,b,r}}{HHSIZE_{baseyr,r}} * \frac{RTBASEFF_{baseyr,eg}}{RTBASEFF_{y,eg}}$$
(B-84)

where

EQCSUEC_{y,eg,b,r} is the unit energy efficiency of surviving water heating equipment in existing-

vintage homes, by year, equipment class, housing type, and Census division,

EQCUEC_{r,ea,b} is the unit energy efficiency of equipment in homes that existed in the base

year, by Census division, equipment class, and housing type,

HHSIZE_{y,r} is the average housing unit size by year and Census division,

HHSELAS is an elasticity parameter for the increase in hot water intensity due to increases

in housing unit size, and

RTBASEFF_{v,eq} are the annual average efficiencies for the equipment classes.

For new purchases,

$$EQCNUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} *WTEQCEFFN_{y,eg,b,r}$$

$$*RTBASEFF_{baseyr,eg} * \left(\frac{HHSIZE_{y,r}}{HHSIZE_{baseyr,r}}\right)^{HHSELAS}$$
(B-85)

where

EQCNUEC_{v.eq,b,r} is the unit energy consumption for new equipment by year, housing

type, and Census division,

*EQCUEC*_{r,eq,b} is the unit energy consumption for the equipment class by housing type

and Census division,

WTEQCEFFN_{y,eg,b,r} is the weighted average inverse efficiency for new water heating

equipment types by year, class, housing type, and Census division,

*HHSIZE*_{V,r} is the average housing unit size by year and Census division,

HHSELAS is an elasticity parameter for the increase in hot water intensity due to

increases in housing unit size, and

 $RTBASEFF_{v,eq}$ is the efficiency of the water heating equipment classes.

For replacements in all years,

$$EQCRUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} *WTEQCEFFR_{y,eg,b,r}$$

$$*RTBASEFF_{baseyr,eg} * \left(\frac{HHSIZE_{y,r}}{HHSIZE_{baseyr,r}}\right)^{HHSELAS}$$
(B-86)

where

EQCRUEC_{y,eg,b,r} is the unit energy consumption for replacement equipment by year,

housing type, and Census division,

WTEQCEFFR_{v,eq,b,r} is the weighted average inverse efficiency for replacement water

heating equipment classes by year, housing type, and Census division,

EQCUEC_{r,eq,b} is the unit energy consumption for the equipment class by housing type

and Census division, and

 $RTBASEFF_{y,eq}$ is the efficiency of retiring equipment from the base-year stock by year.

The average UEC for all equipment is calculated as

$$EQCAUEC_{y,eg,b,r} = EQCNUEC_{y,eg,b,r}$$
, if $y = baseyr + 1$

$$EQCAUEC_{y,eg,b,r} = \frac{\left(EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r}\right)}{*EQCNUEC_{y,eg,b,r}} \\ *EQCNUEC_{y,eg,b,r} \\ + (EQCSR90_{y,eg,b,r} + EQCSUR_{y,eg,b,r}) *EQCAUEC_{y-1,eg,b,r} \\ + EQCRP90_{y,eg,b,r} *EQCRUEC_{y,eg,b,r} \\ \frac{\left(EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r}\right)}{\left(EQCREP_{y,eg,b,r} + EQCSUR_{y,eg,b,r} + EQCRP90_{y,eg,b,r}\right)}, \\ if y > baseyr + 1$$

where

 $EQCAUEC_{y,eq,b,r}$ is the average unit energy consumption for all post-base-year equipment.

Water heater efficiency is calculated next. If y = baseyr+1,

$$WTEQCEFFA_{y=baseyr+1,eg,b,r} = WTEQCEFFN_{y=baseyr+1,eg,b}$$
(B-88)

If y > baseyr+1,

$$WTEQCEFFA_{y,eg,b,r} = \\ \frac{\left(EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r} \right)}{*WTEQCEFFN_{y,eg,b,r}} \\ *WTEQCEFFN_{y,eg,b,r} \\ + \left(EQCSR90_{y,eg,b,r} + EQCSUR_{y,eg,b,r} \right) *WTEQCEFFA_{y-1,eg,b,r} \\ + EQCRP90_{y,eg,b,r} *WTEQCEFFR_{y,eg,b,r} \\ \frac{\left(EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r} \right)}{\left(EQCREP_{y,eg,b,r} + EQCSUR_{y,eg,b,r} + EQCRP90_{y,eg,b,r} \right)}$$

$$(B-89)$$

where

WTEQCEFFA_{y,eg,b,r} is the weighted average water heater efficiency by equipment class, housing type, Census division, and year.

To account for changes in hot water demand over time, both the number and efficiency (with respect to hot water use) of clothes washers is very important. To resolve this issue, the water heating consumption subroutine relies on calculations that are generated in the clothes washer subroutine. First, the number of clothes washers must be shared to each of the competing fuel types for each vintage of equipment:

$$H2OSHRCW_{y,f,b,r,v} = H2OSHR_{y,f,b,r,v} * NUMCW_{y,b,r,v}$$
(B-90)

where

H2OSHRCW_{v,f,b,r,v} is the number of clothes washers for each type of water heating fuel

type by Census division and building type for each vintage of

equipment,

 $H2OSHR_{y,f,b,r,v}$ is the share for each type of water heating fuel type by Census division

and building type for all vintages of equipment, and

NUMCW_{v,b,r,v} is the number of clothes washers by Census division and building type

for all vintages of equipment.

Next, the consumption for water heating for homes with clothes washers is computed as follows:

$$H2OCONCW_{y,f,b,r,v} = H2OSHRCW_{y,f,b,r,v} * H2OUEC_{y,f,b,r,v} * LDADJCW_{y,b,r}$$
 (B-91)

where

H2OCONCW_{v,f,b,r,v} is the water heating consumption for homes with clothes washers for

each type of water heating fuel type by Census division and building

type for all vintages of equipment,

H2OUEC_{v,f,b,r,v}

LDADJCW_{v,b,r}

is the unit energy consumption for each type of water heating fuel type by Census division and building type for all vintages of equipment, and is the adjustment to the water heating UEC to account for the efficiency of clothes washers with respect to hot water load by Census division and building type for all vintages of equipment.

Finally, energy consumption by fuel can be summed over the different housing types. If y = baseyr+1,

$$H2OCON_{y,f,r} = \left(\left(\underbrace{EQCESE_{y,eg,b,r} * EQCSUEC_{eg,b,r}}_{+ EQCADD_{y,eg,b,r}} * EQCNUEC_{y,eg,b,r} + \underbrace{EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r}}_{+ EQCRP90RP_{y,eg,b,r}} * EQCRUEC_{y,eg,b,r} + \underbrace{EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r}}_{* RSELAST(f,r,\alpha,EF1,EF2,EF3,baseyr)} + \sum_{v} H2OCONCW_{y,f,b,r,v} \right)$$

If y > baseyr+1,

$$H2OCON_{y,r} =$$

$$\sum_{b} \left(\left(\frac{EQCESE_{y,eg,b,r} * EQCSUEC_{eg,b,r}}{+ EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r}} + \frac{EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r}}{+ EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r}} + \sum_{v} H2OCONCW_{y,f,b,r,v} + \frac{EQCSR90_{y,eg,b,r} * EQCAUEC_{y,eg,b,r}}{+ EQCREP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r}} + \frac{EQCREP_{y,eg,b,r} * EQCAUEC_{y,eg,b,r}}{+ EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r}} + \frac{EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r}}{+ EQCSUR_{y,eg,b,r}} + \frac{EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r}}{+$$

where

H2OCON_{y,f,r} RSELAST is consumption for water heating by fuel, and

is the short-term price elasticity function with distributed lag weights EF1, EF2, and EF3, and the total short-term price elasticity, α , described in (B-39).

RSTVTEC (Cooking technology choice component)

Throughout this document, cooking equipment is characterized as a cookstove (i.e., gas or electric range), a unit that contains both an oven and a cooktop/ stovetop. The existing cooking equipment distribution is associated with the choice of water heaters. Homes that heat water with natural gas are allowed to have either gas or electric cookstoves; homes that heat with LPG cook with LPG; homes that heat water with distillate fuel oil cook with electricity. Replacement cookstoves in single-family homes

are not so constrained. These constraints are embodied in the technology choice by using the water heater equipment market shares for calculating the cooking equipment market shares:

$$NCKSH_{y,eg,b,r} = NH2OSH_{y,eg,b,r} * NGNGFACT$$
, if $eg = gas range$
 $NCKSH_{y,eg,b,r} = NH2OSH_{y,eg,b,r}$, if $eg = LPG range$
 $NCKSH_{y,eg,b,r} =$

$$\sum (NH2OSH_{y,eg,b,r}) + NH2OSH_{y,eg,b,r} * (1. - NGNGFACT),$$
if $eg = other$

where

 $NCKSH_{y,eq,b,r}$ is the new market share for cooking equipment in the current year by housing

type and Census division,

*NH2OSH*_{y,eq,b,r} is the new market share for water heaters in the current year by equipment class,

housing type and Census division, and

NGNGFACT is a constant that defines the fraction of new homes having gas water heaters

that have gas cookstoves.

In the formula, the summation in the case of eg = other refers to the market shares of all water heater classes other than natural gas and LPG: homes that heat water with any other equipment class than these, depending on which are defined in the RSCLASS.TXT file, are assumed to cook with electricity.

The following variables are computed as in the equations indicated:

 $OPCOST_{y,es,b,r,v}$ is the operating cost for the cooking equipment type by housing type, Census

division, vintage, and year. It is computed as in (B-67) above.

LFCY_{v,es,b,r,v} is the cooking equipment's life-cycle cost by year, housing type, Census division,

and vintage. It is computed as in (B-16) above.

EQWTN_{y,es,b,r} is the equipment weight for new equipment types by housing type, Census

division, and year. It is computed as in (B-20) above.

EQWTR_{v,es,b,r} is the equipment weight for replacement equipment types by housing type,

Census division, and year. It is computed as in (B-21) above.

 $TOTEWTN_{y,eq,b,r}$ is the sum of the equipment types' weights for the new equipment class. It is

computed as in (B-22) above.

TOTEWTR_{y,eg,b,r} is the sum of the equipment types' weights for the replacement equipment

class. It is computed as in (B-23) above.

EQFSHRN_{y,f,b,r} is the fuel share of new equipment type by year, housing type and Census

division. It is computed as in (B-24) above.

EQFSHRR_{v,f,b,r} is the fuel share of replacement equipment type by year, housing type and

Census division. It is computed as in (B-25) above.

The final shares for the equipment types are the products of the market shares and the equipment type shares,

$$NEQTSHRD_{y,eg,b,r} = NCKSH_{y,eg,b,r} * EQFSHRN_{y,es,b,r}$$

$$REQTSHRD_{y,eg,b,r} = NCKSH_{y,eg,b,r} * EQFSHRR_{y,es,b,r}$$
(B-95)

where

 $NEQTSHRD_{y,es,b,r}$ is the new equipment type share for cookstoves by equipment type, housing type and Census division,

 $REQTSHRD_{y,es,b,r}$ is the replacement equipment type share for cookstoves by equipment type,

housing type and Census division,

 $NCKSH_{y,eg,b,r}$ is the new market share for cooking equipment in the current year by housing

type and Census division,

EQFSHRN_{y,es,b,r} is the new market share for cookstoves by equipment type, housing type and

Census division, and

EQFSHRR_{y,es,b,r} is the replacement market share for cookstoves by equipment type, housing

type and Census division.

For cooking, the weighted average inverse efficiency of each equipment class is calculated differently from the foregoing end uses, because the RSMEQP file datum for *RTBASEFF*_{es} is the usage, measured in kWh or MMBtu, of the equipment in the class:

$$WTEQCEFFA_{y,eg,b,r} = \frac{\sum_{es \in eg} \left(NEQTSHR_{y,es,b,r} * RTEQEFF_{es} \right)}{\sum_{es \in eg} NEQTSHR_{y,es,b,r}}$$
(B-96)

where

WTEQCEFFA_{y,eq,b,r} is the weighted average cooking equipment usage in the current year by

housing type and Census division, and

RTEQEFF_{es} is the equipment efficiency.

REUADD (Water heating and cooking additions and replacements component)

As mentioned earlier, the capabilities for adding and replacing cooking equipment have been merged into a single component called *REUADD*. This component was documented above in the water heating section.

RSTVCON (Cooking energy consumption component)

The unit energy consumption for the surviving equipment is calculated by,

$$EQCSUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} * \frac{RTBASEFF_{baseyr,eg}}{RTBASEFF_{v,eg}}$$
(B-97)

where

EQCSUEC_{y,eg,b,r} is the unit energy consumption for surviving cooking equipment in the current

year by housing type, and Census division,

 $EQCUEC_{r,eq,b}$ is the unit energy consumption for cooking equipment by housing type, and

Census division, and

RTBASEFF_{v,eq} are the annual average efficiencies for the equipment classes (represented as

unit energy consumption for this service).

For new equipment,

$$EQCNUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} * \frac{WTEQCEFFN_{y,eg,b,r}}{RTBASEFF_{baseyr,eg}}$$
(B-98)

where

EQCNUEC_{y,eg,b,r} is the unit energy consumption for new cooking equipment in the

current year by housing type and Census division,

*EQCUEC*_{r,eg,b} is the unit energy consumption for cooking equipment by class, housing

type, and Census division,

WTEQCEFFN_{y,eq,b,r} is the weighted average cooking usage for new equipment in the

current year by housing type and Census division, and

RTBASEFF_{basevr,eq} is the base-year efficiency of the cooking equipment class.

For replacement equipment,

$$EQCRUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} * \frac{WTEQCEFFR_{y,eg,b,r}}{RTBASEFF_{baseveg}}$$
(B-99)

where

EQCRUEC_{v,eq,b,r} is the unit energy consumption for replacement cooking equipment in

the current year by housing type and Census division,

EQCUEC_{r,ea,b} is the unit energy consumption for cooking equipment by class, housing

type, and Census division,

WTEQCEFFR_{v,eq,b,r} is the weighted average cooking usage for replacement equipment in the

current year by housing type and Census division, and

RTBASEFF_{baseyr,eg} is the base-year efficiency of the cooking equipment class.

For the average efficiency, the initial year level is set to the new equipment efficiency:

If y = baseyr+1,

$$EQCAUEC_{y,eg,b,r} = EQCNUEC_{r,eg,b}$$
 (B-100)

If y > baseyr+1,

$$EQCAUEC_{y,eg,b,r} = \\ \frac{\left(EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r} \right)}{*EQCNUEC_{y,eg,b,r}} \\ *EQCNUEC_{y,eg,b,r} \\ + \left(EQCSR90_{y,eg,b,r} + EQCSUR_{y,eg,b,r} \right) *EQCAUEC_{y-I,eg,b,r} \\ + EQCRP90_{y,eg,b,r} *EQCRUEC_{y,eg,b,r} \\ \frac{\left(EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r} \right)}{\left(EQCREP_{y,eg,b,r} + EQCSUR_{y,eg,b,r} + EQCRP90_{y,eg,b,r} \right)}$$

$$(B-101)$$

And energy consumption is defined as:

$$CKCON_{y,r} = \sum_{b,eg} \begin{pmatrix} EQCESE_{y,eg,b,r} * EQCUEC_{eg,b,r} \\ + EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} \\ + EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \end{pmatrix}, \quad if \quad y = baseyr + 1$$

$$(B-102)$$

$$CKCON_{y,r} = \sum_{b,eg} \begin{pmatrix} EQCESE_{y,eg,b,r} * EQCUEC_{eg,b,r} \\ + EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} \\ + EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSR90_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} \\ + EQCREP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} \\ + EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} \end{pmatrix}, \quad if \quad y > baseyr + 1$$

$$(B-103)$$

RDRYTEC (Clothes drying technology choice component)

The following variables are computed as in the equations indicated:

 $OPCOST_{y,es,b,r,v}$ is the operating cost for the equipment type by year, housing type, Census

division, and vintage. It is computed as in (B-67) above.

LFCY_{y,es,b,r,v} is the clothes dryer's life-cycle cost by year, housing type, Census division, and

vintage. It is computed as in (B-16) above.

EQWTN_{y,es,b,r} is the equipment weight for new equipment type by year, housing type, and

Census division. It is computed as in (B-20) above.

EQWTR_{v.es.b.r} is the equipment weight for replacement equipment by year, housing type, and

Census division. It is computed as in (B-21) above.

 $TOTEWTN_{y,eg,b,r}$ is the sum of equipment weights for the new purchase equipment class. It is computed as in (B-22) above.

 $TOTEWTR_{y,eg,b,r}$ is the sum of equipment weights for the replacement purchase equipment class. It is computed as in (B-23) above.

Market shares for new and replacement dryers are computed next

$$NEQTSHR_{y,es,b,r} = \frac{EQWT_{y,es,b,r}}{TOTEWT_{y,eg,b,r}}$$
(B-104)

where

NEQTSHR_{y,es,b,r} is the new market share of clothes dryer equipment types by housing type and

Census division in the current year,

 $TOTEWT_{eg}$ is the sum of equipment weights for the new equipment class, and

*EQWT*_{es} is the equipment weight for new equipment.

The class averages of equipment type efficiencies for clothes drying equipment are calculated as for other end uses:

$$TEMP = \sum_{es} EQWT_{y,es,b,r}$$

$$WTEQCEFFA_{y,eg,b,r} = \frac{\sum_{es} \left(\frac{EQWT_{y,es,b,r}}{RTEQEFF_{es}}\right)}{TEMP}, if TEMP > 0$$

$$WTEQCEFFA_{y,eg,b,r} = \frac{1}{RTBASEFF_{baseyreg}}, otherwise$$
(B-105)

where

WTEQCEFFA_{y,es,b,r} is the weighted average usage of clothes dryer equipment classes in the

current year by housing type and Census division, and

 $EQWT_{v,es,b,r}$ is the equipment weight for each type of new equipment.

DRYADD (Clothes drying additions component)

New clothes drying equipment is calculated using a saturation level for newly purchased equipment:

$$EQCADD_{y,eg,b,r} = \sum_{es} \left(HSEADD_{y,b,r} * NEQTSHR_{y,es,b,r} * \frac{NEWDRYSAT_{b,r}}{100} \right)$$
(B-106)

where

EQCADD_{v.ea,b,r} is the amount of new (post-base-year-vintage) equipment added in new housing

units in the current year by housing type and Census division,

HSEADD_{v,b,r} is the number of new housing additions in the year by housing type and Census

division,

NEQTSHR_{y,es,b,r} is the market share of new clothes dryer equipment types by housing type and

Census division in the current year, and

NEWDRYSAT_{b,r} is the level of market penetration of new clothes dryer equipment by housing

type and Census division, expressed as a percent, from the RSMISC.TXT file.

The next step is to calculate the numbers of dryers of each vintage category. The following variables were computed as in the equations indicated:

E0.00000	
FOR CRUIT	is the surviving nost-hase-vear vintage equinment in existing housing
$EQCSR90_{y,eq,b,r}$	is the surviving post-base-year vintage equipment in existing housing

units in the current year by housing type and Census division. It is

computed as in (B-36) above.

EQCSUR_{v,ea,b,r} is the surviving new (post-base-year-vintage) equipment in the current

year by housing type and Census division. It is computed as in (B-37)

above.

 $EQCREP_{y,eq,b,r}$ is the number of replacement units (post-base-year-vintage) equipment

demanded in post-base-year-vintage housing units by housing type and

Census division. It is computed as in (B-29) above.

EQCRP90_{y,eg,b,r} is the number of replacement units demanded in existing housing units

each year by housing type and Census division. It is computed as in (B-

30) above.

EQCRP90RP_{y,eg,b,r} is the number of replacement units for the EQCRP90 units demanded

each year by housing type and Census division. It is computed as in (B-

31) above.

RDRYCON (Clothes drying energy consumption component)

The unit energy consumption for surviving equipment is calculated as:

$$EQCSUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} * \frac{RTBASEFF_{baseyr,eg}}{RTBASEFF_{y,eg}}$$
(B-107)

where

EQCSUEC_{y,eg,b,r} is the UEC for surviving base-year equipment in each equipment class, by

housing type, and Census division,

RTBASEFF_{y,eg} is the base efficiency of the same general equipment category in each year, and

EQCUEC_{r,eq,b} is unit energy consumption for equipment in base-year housing by Census

division, equipment class, and housing type.

For new equipment,

$$EQCNUEC_{y,eg,b,r} = EQCUEC_{r,eg,b} *WTEQCEFFN_{y,eg,b,r} *RTBASEFF_{y,eg}$$
(B-108)

where

EQCNUEC_{y,eg,b,r} is the unit energy consumption by year for new equipment by housing

type and Census division,

WTEQCEFFN_{y,eg,b,r} is the new equipment efficiency by year, equipment class, housing type,

and Census division,

RTBASEFF_{y,eq} is the base-year efficiency of the equipment class, and

EQCUEC_{r,ea,b} is unit energy consumption for equipment in base-year housing by

Census division, equipment class, and housing type.

For replacement equipment,

$$EQCRUEC_{y,eg,b,r} = \\ EQCUEC_{r,eg,b} *WTEQCEFFR_{y,eg,b,r} *RTBASEFF_{y,eg}$$
(B-109)

where

EQCRUEC_{y,eq,b,r} is the unit energy consumption by year for replacement equipment by

housing type and Census division,

WTEQCEFFR_{y,eg,b,r} is the replacement efficiency by year, equipment class, housing type,

and Census division,

RTBASEFF_{y,eq} is the base-year efficiency of the equipment class, and

*EQCUEC*_{r,ea,b} is unit energy consumption for equipment in base-year housing by

Census division, equipment class, and housing type.

The average of the two unit energy consumption variables is computed as follows:

If y = baseyr+1,

$$EQCAUEC_{y,eg,b,r} = EQCNUEC_{r,eg,b}$$
(B-110)

If y > baseyr+1,

$$\frac{\left(\left(EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r}\right)\right)}{\left(EQCNUEC_{y,eg,b,r} + EQCSUR_{y,eg,b,r}\right) * EQCAUEC_{y-1,eg,b,r}} \\ + \left(EQCSR90_{y,eg,b,r} + EQCSUR_{y,eg,b,r}\right) * EQCAUEC_{y-1,eg,b,r}} \\ + \left(EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r}\right) \\ \frac{\left(EQCREP_{y,eg,b,r} + EQCADD_{y,eg,b,r} + EQCRP90RP_{y,eg,b,r}\right)}{\left(EQCREP_{y,eg,b,r} + EQCSUR_{y,eg,b,r} + EQCRP90_{y,eg,b,r}\right)}$$

And energy consumption is defined as:

$$DRYCON_{y=2006r} = \sum_{b,eg} \begin{pmatrix} EQCESE_{y,eg,b,r} * EQCUEC_{eg,b,r} \\ + EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} \\ + EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \end{pmatrix}, \quad if \quad y = baseyr + 1$$

$$DRYCON_{y,r} = \left(\begin{array}{l} EQCESE_{y,eg,b,r} * EQCUEC_{eg,b,r} \\ + EQCADD_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCRP90_{y,eg,b,r} * EQCRUEC_{y,eg,b,r} \\ + EQCRP90RP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSR90_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} \\ + EQCREP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCREP_{y,eg,b,r} * EQCNUEC_{y,eg,b,r} \\ + EQCSUR_{y,eg,b,r} * EQCAUEC_{y,eg,b,r} \end{array} \right), \quad if \quad y > baseyr + 1$$

RREFTEC (Refrigeration technology choice component)

Refrigeration is modeled somewhat differently than most other end uses. It can be thought of as having three general types depending on the freezer location: top-mounted, side-mounted, or bottom-mounted. RECS includes only a single UEC; therefore, rather than modeling these different general types as classes (e.g., electric dryers where there are multiple classes and multiple UECs), the multiple types are treated as just another refrigerator type, but with some further special treatment. So for refrigeration, the denotation for equipment class *eg* is always defined as 1, and is not needed as a subscript as for other end uses.

The special treatment of the multiple types takes the form of an assumed share of the market, whereas market shares for the other end use equipment types are determined based on model-endogenous logistic equipment choice based on the relationship between operating cost and capital cost. Refrigerators with side- and bottom-mounted freezers are generally more costly and tend to be less efficient. Thus, the assumed market share for these types is needed because if modeled *competitively* as just another refrigerator type (denoted *es*) they would not receive a significant market share, even though in practice they are popular. The assumed market share is 25% for side-mounted freezers and 25% for bottom-mounted freezers. In the equations that follow, the subscript *es* will be distinguished as to whether it refers to side- or bottom-mounted freezer refrigerators versus other types when the distinction is necessary. Equipment operating cost for top-mounted freezer refrigerators is:

$$OPCOST_{v,es,b,r,v} = PRICES_{f,r,v} * RTEQEFF_{es} * FACTOR$$
 (B-114)

where

 $OPCOST_{v,es,b,r,v}$ is the operating cost of the equipment type by housing type, Census division,

and vintage in the current year,

PRICES_{f.r.v} is the fuel price in the current year by Census division from the NEMS

Integrating Module,

RTEQEFF_{es} is the efficiency (represented as unit energy consumption for this service) of the

refrigerator type, and

FACTOR is a factor (0.003412 MMBtu/kWh) that converts the units of RTEQEFFes,

expressed in kWh for refrigerators and freezers.

The following variables are computed as in the equations indicated:

*LFCY*_{y,es,b,r,v} is the refrigerator's life-cycle cost by year, housing type, Census division, and

vintage. It is computed as in (B-16) above.

EQWTN_{y,es,b,r} is the equipment weight for new equipment type by year, housing type, and

Census division. It is computed as in (B-20) above.

EQWTR_{y,es,b,r} is the equipment weight for replacement equipment by year, housing type, and

Census division. It is computed as in (B-21) above.

 $TOTEWTN_{y,eq,b,r}$ is the sum of equipment weights for the new purchase equipment class. It is

computed as in (B-22) above.

 $TOTEWTR_{y,eg,b,r}$ is the sum of equipment weights for the replacement purchase equipment class.

It is computed as in (B-23) above.

The general types of refrigerators have market shares as follows:

$$NEQTSHR_{y,es\neq TTD,b,r} = \frac{EQWTN_{es,b,r}}{TMFSHR_{b,r}} * (TMF_SHR)$$
(B-115)

$$REQTSHR_{y,es\neq TTD,b,r} = \frac{EQWTR_{es,b,r}}{TMFSHR_{b,r}} * (TMF_SHR)$$
(B-116)

where

 $NEQTSHR_{y,es\neq TTD,b,r}$ is the market share for new refrigerators of the equipment type in the

current year by housing type and Census division,

REQTSHR_{y,es \neq TTD,b,r} is the market share for the replacements of equipment type in the

current year by housing type and Census division

TMFSHR_{b,v}, is the model-calculated market share of refrigerators with top-mounted

freezers in the current year by housing type and

TMF_SHR is the assumed overall share of refrigerators with top-mounted freezers.

Market shares are defined similarly for refrigerators with side- and bottom-mounted freezers using SMFSHR and BMFSHR, respectively, instead of TMFSHR. For the refrigerators with modeled market shares, their calculated market shares are *deflated* by the assumed share of the different types, ensuring that the market shares sum to unity.

$$WTEQCEFFN_{y,b,r} = \frac{\sum_{es} \left(NEQTSHR_{y,es,b,r} * RTEQEFF_{es} \right)}{\sum_{es} NEQTSHR_{y,es,b,r}}$$
(B-117)

$$WTEQCEFFR_{y,b,r} = \frac{\sum_{es} \left(REQTSHR_{y,es,b,r} * RTEQEFF_{es}\right)}{\sum_{es} REQTSHR_{y,es,b,r}}$$
(B-118)

where

WTEQCEFFN_{y,b,r} is the weighted average usage of new refrigerator classes by housing

type and Census division,

WTEQCEFFR_{y,b,r} is the weighted average usage of replacement refrigerator classes by

housing type and Census division,

RTEQEFF_{es} is the efficiency by refrigerator type, from the RSMEQP.TXT input file, NEQTSHR_{y,es,b,r} is the new market share for the equipment types in the current year by

housing type and Census division, and

 $REQTSHR_{y,es,b,r}$ is the market share for the replacements of equipment types in the

current year by housing type and Census division.

RREFADD (Additions to the refrigeration stock component)

Refrigerator additions allow for new single-family homes to have more than one refrigerator. The additions are calculated as:

$$EQCADD_{y,b,r} = HSEADD_{y,b,r} * RFADDFAC, if b = 1$$

$$EQCADD_{y,b,r} = HSEADD_{y,b,r}, otherwise$$
(B-119)

where

EQCADD_{y,b,r} is the amount of new (post-base-year-vintage) refrigerators added in new

housing units in the current year by housing type and Census division,

 $HSEADD_{y,b,r}$ is the number of new housing units constructed in the current year by housing

type and Census division, and

RFADDFAC is the percent of new single-family housing units with two refrigerators.

The following variables are computed as in the equations indicated:

EQCSR90_{v,eq,b,r} is the surviving post-base-year vintage equipment in existing housing

units in the current year by housing type and Census division. It is

computed as in (B-36) above.

EQCSUR_{y,eg,b,r} is the surviving new (post-base-year-vintage) equipment in the current

year by housing type and Census division. It is computed as in (B-37)

above.

EQCREP_{y,eg,b,r} is the number of replacement units (post-base-year-vintage) equipment

demanded in post-base-year-vintage housing units by housing type and

Census division. It is computed as in (B-29) above.

EQCRP90_{y,eg,b,r} is the number of replacement units demanded in existing housing units

each year by housing type and Census division. It is computed as in (B-

30) above.

EQCRP90RP_{v,eq,b,r} is the number of replacement units for the EQCRP90 units demanded

each year by housing type and Census division. It is computed as in (B-

31) above.

RREFCON (Refrigeration energy consumption component)

The unit energy consumption calculations for surviving, new, and replacement equipment, and their averages are calculated as

$$EQCSUEC_{y,b,r} = EQCUEC_{r,b} * \frac{RTBASEFF_{y}}{RTBASEFF_{baseyr}}$$
(B-120)

where

EQCSUEC_{y,b,r} is the UEC for surviving base-year equipment in each equipment class, by

housing type and Census division, and

EQCUEC_{r,b} is the UEC for the original base-year equipment in each equipment class, by

housing type and Census division, and

 $RTBASEFF_{\nu}$ is the base efficiency (represented by unit energy consumption for this service).

For new refrigerators,

$$EQCNUEC_{y,b,r} = EQCUEC_{r,b} * \frac{WTEQCEFFN_{y,b,r}}{RTBASEFF_{baseyr}}$$
(B-121)

where

EQCNUEC_{v,b,r} is the efficiency-weighted unit energy consumption for new

refrigerators in the current year by housing type and Census division,

EQCUEC_{r,b} is the unit energy consumption for base-year refrigerators by housing

type and Census division,

WTEQCEFFN_{y,b,r} is the market-share-weighted usage of new refrigerators in the current

year by housing type and Census division, and

RTBASEFF_{baseyr} is the base-year stock-average efficiency of refrigerators.

For replacement refrigerators,

$$EQCRUEC_{y,b,r} = EQCUEC_{r,b} * \frac{WTEQCEFFR_{y,b,r}}{RTBASEFF_{baseyr}}$$
(B-122)

where

 $EQCRUEC_{y,b,r}$ is the efficiency-weighted unit energy consumption for replacement

refrigerators in the current year by housing type and Census division,

WTEQCEFFR_{y,b,r} is the market-share-weighted usage of replacement refrigerators in the

current year by housing type and Census division,

RTBASEFF_{baseyr} is the base-year stock-average efficiency of refrigerators.

The weighted average of the three UEC sets is calculated here.

If y = baseyr+1,

$$EQCAUEC_{v,b,r} = EQCNUEC_{v,b,r}$$
 (B-123)

If y > baseyr+1,

$$EQCAUEC_{y,b,r} = \frac{\left(EQCREP_{y,b,r} + EQCADD_{y,b,r} + EQCRP90RP_{y,b,r}\right)}{*EQCNUEC_{y,b,r}}$$

$$+ (EQCSR90_{y,b,r} + EQCSUR_{y,b,r}) * EQCAUEC_{y-1,b,r}$$

$$+ EQCRP90_{y,b,r} * EQCRUEC_{y,b,r}$$

$$\frac{\left(EQCREP_{y,b,r} + EQCADD_{y,b,r} + EQCRP90RP_{y,b,r}\right)}{\left(EQCREP_{y,b,r} + EQCSUR_{y,b,r} + EQCRP90_{y,b,r}\right)}$$

$$(B-124)$$

where

 $EQCAUEC_{y,b,r}$ is the average unit energy consumption of refrigerators in the current year by housing type and Census division.

The weighted average usage is now calculated as:

$$WTEQCEFFA_{y,b,r} = WTREFFN_{y,b,r}$$
, if $y = baseyr + 1$

$$WTEQCEFFA_{y,b,r} = \\ \frac{\left(EQCREP_{y,b,r} + EQCADD_{y,b,r} + EQCRP90RP_{y,b,r}\right)}{*WTEQCEFFN_{y,b,r}} \\ + \left(EQCSR90_{y,b,r} + EQCSUR_{y,b,r}\right) *WTEQCEFFA_{y-1,b,r} \\ + EQCRP90_{y,b,r} *WTEQCEFFR_{y,b,r} + EQCADD_{y,b,r} * \\ RTBASEFF_{baseyr,eg} \\ \frac{\left(EQCREP_{y,b,r} + EQCADD_{y,b,r} + EQCRP90RP_{y,b,r}\right)}{\left(EQCREP_{y,b,r} + EQCSUR_{y,b,r} + EQCRP90_{y,b,r}\right)}, otherwise \\ + EQCSR90_{y,b,r} + EQCSUR_{y,b,r} + EQCRP90_{y,b,r} \\ \end{pmatrix}$$

And energy consumption is estimated as:

$$REFCON_{y=baseyr+1,r} =$$

$$\sum_{b} \begin{pmatrix} EQCESE_{y,b,r} * EQCUEC_{b,r} \\ + EQCADD_{y,b,r} * EQCNUEC_{y,b,r} \\ + EQCADD_{y,b,r} * EQCUEC_{b,r} \\ + EQCRP90_{y,b,r} * EQCRUEC_{y,b,r} \\ + EQCRP90RP_{y,b,r} * EQCNUEC_{y,b,r} \end{pmatrix}, \quad if \quad y = baseyr + 1$$

$$(B-126)$$

$$REFCON_{y,r} = \left(\begin{array}{c} EQCESE_{y,b,r} * EQCUEC_{b,r} \\ + EQCADD_{y,b,r} * EQCNUEC_{y,b,r} \\ + EQCADD_{y,b,r} * EQCUEC_{b,r} \\ + EQCRP90_{y,b,r} * EQCRUEC_{y,b,r} \\ + EQCRP90RP_{y,b,r} * EQCNUEC_{y,b,r} \\ + EQCSR90_{y,b,r} * EQCAUEC_{y,b,r} \\ + EQCREP_{y,b,r} * EQCNUEC_{y,b,r} \\ + EQCREP_{y,b,r} * EQCNUEC_{y,b,r} \\ + EQCSUR_{y,b,r} * EQCAUEC_{y,b,r} \end{array} \right), \quad if \quad y > baseyr + 1$$

where

REFCON_{y,r} is energy consumption for refrigeration, EQCESE_{y,b,r} is the surviving old (existing-vintage) equipment in old (existing vintage) housing units in the current year by housing type and Census division, is the amount of new (post-base-year-vintage) refrigerators added in new housing units in the current year by housing type and Census division, is the number of replacement (post-base-year-vintage) equipment in existing housing units in the current year by housing type and Census division,

EQCRP90RP_{y,b,r} is the number of replacements for the EQCRP90 equipment in the current year by housing type and Census division, is the efficiency-weighted unit energy consumption for replacement refrigerators in the current year by housing type and Census division, is the efficiency-weighted unit energy consumption for new refrigerators in the current year by housing type and Census division, and

is the conit of a second control of the matrice and the

 $EQCUEC_{r,b}$ is the unit energy consumption for refrigerators by housing type and Census

division.

RFRZTEC (Freezing technology choice component)

Freezing is parallel to refrigeration so it is also modeled without reference to the equipment class *eg* which is implicitly 1, and where upright freezers (with *es* instead denoted as *UP*) conceptually take the place of through-the-door refrigerators and receive an assumed market share. The upright freezer market share *UPSHR* is assumed to be 49%. The other characterized freezers are assumed to be of the horizontal or *chest* type. The processing of the market share weights is performed as for similar to refrigeration. The following variables are computed as in the equations indicated:

OPCOST_{y,es,b,r,v} is the operating cost for the equipment type by year, housing type, Census division, and vintage. It is computed as in (B-67) above.
 LFCY_{y,es,b,r,v} is the freezer's life-cycle cost by year, housing type, Census division, and vintage. It is computed as in (B-16) above.
 EQWTN_{y,es,b,r} is the equipment weight for new equipment type by year, housing type, and Census division. It is computed as in (B-20) above.
 EQWTR_{y,es,b,r} is the equipment weight for replacement equipment by year, housing type, and Census division. It is computed as in (B-21) above.
 TOTEWTN_{y,eg,b,r} is the sum of equipment weights for the new purchase equipment class. It is

computed as in (B-22) above.

 $TOTEWTR_{y,eg,b,r}$ is the sum of equipment weights for the replacement purchase equipment class. It is computed as in (B-23) above.

Shares for equipment types, in normalized form, are calculated by a method similar to the method used for other equipment types:

$$NEQTSHR_{y,es,b,r} = UPSHR, if es = upright freezer$$

$$NEQTSHR_{y,es,b,r} = \frac{EQWTN_{es,b,r}}{TOTEWTN_{b,r}} * (1 - UPSHR), otherwise$$
(B-128)

$$REQTSHR_{y,es,b,r} = UPSHR, if es = upright freezer$$

$$REQTSHR_{y,es,b,r} = \frac{EQWTR_{es,b,r}}{TOTEWTR_{b,r}} * (1 - UPSHR), otherwise$$
(B-129)

NEQTSHR_{y,es,b,r} is the new market share for the equipment type in the current year by housing

type and Census division,

 $REQTSHR_{v,es,b,r}$ is the market share for replacement of equipment types in the current year by

housing type and Census division, and

UPSHR is the market share for upright freezers.

The weighted average efficiencies for new and replacement equipment are computed as for other equipment categories:

$$WTEQCEFFN_{y,b,r} = \frac{\sum_{es} \left(NEQTSHR_{y,es,b,r} * RTEQEFF_{es} \right)}{\sum_{es} NEQTSHR_{y,es,b,r}}$$
(B-130)

$$WTEQCEFFR_{y,b,r} = \frac{\sum_{es} \left(REQTSHR_{y,es,b,r} * RTEQEFF_{es}\right)}{\sum_{es} REQTSHR_{y,es,b,r}}$$
(B-131)

where

WTEQCEFFN_{y,b,r} is the market-share-weighted usage of new freezers in the current year

by housing type and Census division,

WTEQCEFFR_{y,b,r} is the market-share-weighted usage of replacement freezers in the

current year by housing type and Census division,

NEQTSHR_{v.b.r} is the new market share in the current year by housing type and Census

division, and

REQTSHR_{v.b.r} is the market share for the replacements n the current year by housing

type and Census division.

RFRZADD (Additions to the freezing stock component)

Calculations of changes in the freezing equipment stock are computed for all vintage categories. For additions after the baseyr+1,

$$EQCADD_{y,b,r} = HSEADD_{y,b,r} * \left(\frac{FRZSAT_{b,r}}{100}\right)$$
(B-132)

where

EQCADD_{V,b,f} is the amount of new (post-base-year-vintage) equipment added in new housing

units in the year by housing type and Census division,

 $HSEADD_{v,b,r}$ is the number of new housing units constructed in the current year by housing

type and Census division, and

 $FRZSAT_{b,r}$ is the market penetration level of freezers by housing type and Census division, from the RSMISC.TXT file, expressed as percentages.

The following variables are computed as in the equations indicated:

EQCSR90_{y,eg,b,r} is the surviving post-base-year vintage equipment in existing housing

units in the current year by housing type and Census division. It is

computed as in (B-36) above.

EQCSUR_{y,eg,b,r} is the surviving new (post-base-year-vintage) equipment in the current

year by housing type and Census division. It is computed as in (B-37)

above.

*EQCREP*_{y,eg,b,r} is the number of replacement units (post-base-year-vintage) equipment

demanded in post-base-year-vintage housing units by housing type and

Census division. It is computed as in (B-29) above.

EQCRP90_{v,ea,b,r} is the number of replacement units demanded in existing housing units

each year by housing type and Census division. It is computed as in (B-

30) above.

EQCRP90RP_{v,eq,b,r} is the number of replacement units for the EQCRP90 units demanded

each year by housing type and Census division. It is computed as in (B-

31) above.

FRZCON (Freezing energy consumption component)

The detailed unit energy consumption variables are computed exactly as for refrigerators:

EQCSUEC_{v,b,r} is the UEC for surviving base-year equipment in each equipment class, by

housing type and Census division, calculated as in equation (B-120),

EQCNUEC_{v,b,r} is the efficiency-weighted unit energy consumption for new freezers in the

current year by housing type and Census division, calculated as in equation (B-

121), and

EQCRUEC_{v,b,r} is the efficiency-weighted unit energy consumption for replacement

refrigerators in the current year by housing type and Census division, calculated

as in equation (B-122).

Weighted average usages are calculated:

$$WTEQCEFFA_{y,b,r} = WTREFFN_{y,b,r}, if \quad y = baseyr + 1$$

$$WTEQCEFFA_{y,b,r} = \frac{\left((EQCREP_{y,b,r} + EQCADD_{y,b,r} + EQCRP90RP_{y,b,r}) \right)}{*WTEQCEFFN_{y,b,r}}$$

$$+ (EQCSR90_{y,b,r} + EQCSUR_{y,b,r}) *WTEQCEFFA_{y-1,b,r}} + EQCRP90_{y,b,r} *WTEQCEFFR_{y,b,r}}$$

$$\frac{\left(EQCREP_{y,b,r} + EQCADD_{y,b,r} + EQCRP90RP_{y,b,r} \right)}{\left(EQCREP_{y,b,r} + EQCADD_{y,b,r} + EQCRP90_{y,b,r} \right)}, otherwise$$

$$+ EQCSR90_{y,b,r} + EQCSUR_{y,b,r} + EQCRP90_{y,b,r}$$

And regional energy consumption is estimated as

$$FRZCON_{y=2006r} = \sum_{b} \left(\frac{EQCESE_{y,b,r} * EQCUEC_{b,r}}{+ EQCADD_{y,b,r} * EQCNUEC_{y,b,r}} + \frac{EQCRP90_{y,b,r} * EQCRUEC_{y,b,r}}{+ EQCRP90RP_{y,b,r} * EQCNUEC_{y,b,r}} \right), \quad \text{if} \quad y = baseyr + 1$$

where

 $WTEQCEFFA_{y,eg,b,r}$

is the market-share-weighted average usage of freezers in the current year by housing type and Census division.

LTCNS (Lighting choice, stock, and energy consumption component)

The lighting end use is separated into distinct applications grouped by usage or lamp characteristics referred to as lighting *applications*: general service lighting, reflector lamps, linear fluorescent lamps, and exterior lighting. General service lighting represents *Edison-type* sockets—the typical screw-base bulbs found on incandescent, compact fluorescent, and LED bulbs. General service lighting is most important in terms of energy consumption for the residential sector; therefore, it also has the most detailed characterization and accounting in the lighting module. The equations below are generalized to represent any of the four applications—the only difference among them is that the general service category is further partitioned into hours-of-use bins, which affects the relationship between operating and capital costs, as documented below. Currently reflector lamps, linear fluorescent lamps, and exterior lighting are characterized with only a single hours-of-use bin; however, this characterization is controlled by the dimensions set in the input file so that additional hours-of-use bins could be characterized, data permitting, up to six bins.

Operating costs are developed using the same general framework for each lighting application. Note that operating costs receive a regional dimension due to the regional variation in electricity prices. Capital costs below do not have a regional dimension, though subsidies are available by Census division to represent regional energy efficiency program expenditures.

$$OPCOST_{y,app,bin,e,r} = \\PRICES_{y,r} * BULBWATTS_{app,e,y} * FACTOR * APPBINHOURS_{app,bin} * 365$$
 (B-135)

where

OPCOST_{y,app,bin,e,r} are the annual operating costs for year, application, bin, bulb type, e,

and Census division, r,

PRICES_{y,r} are lighting end-use electricity prices by year and Census division,

BULBWATTS_{app,e,y} are the Watts for application, bulb type, and year,

FACTOR is a value (3.412/10⁶) that converts Watts to Btu per hour,

APPBINHOURS_{app,bin} are the number of hours of use per day for this application and bin, and

365 converts daily hours to annual hours.

Capital costs are merely the cost of the bulb with two potential adjustments. In the case where multiple bulb replacements per year must be made as for high hours-of-use bins (affecting incandescent lights especially), bulb costs are scaled up by the number of annual replacements required, representing the annual purchase costs. Also, for non-incandescent bulbs, an adjustment is made based on the color rendering index (CRI) that normalizes to a CRI-adjusted cost and ultimately reduces the market share in the choice equation below for bulbs with less-desirable light spectra.

$$LTLCAP_{y,app,bin,e} = \frac{[BULBCOST_{app,e,y} / BULBBINLIFE_{app,e,bin,y}] / [BULBCRI_{app,e,y} / 100]^{2}}{[BULBCRI_{app,e,y} / 100]^{2}}$$

where

LTLCAP_{y,app,bin,e} is the total annual bulb costs by year, application bin, bulb type, and

Census division,

 $BULBCOST_{app,e,y}$ is the cost per bulb,

BULBBINLIFE_{app,e,bin,y} is the life in years for a bulb within an hours-of-use bin (if life in years is

greater than one year, the capital cost is not adjusted because the

choice is based on first-year total costs), and

BULBCRI_{app,e,y} is the color rendering index for an application and bin (dividing by 100,

then squaring the result, increases LTLCAP, thus penalizing bulbs with

lower-quality light).

Market shares for purchases of the various types of bulbs available for a particular application are computed separately for each application as follows:

$$LTMSHR_{y,app,bin,e,b,r} = \frac{\exp^{\beta_1*LTLCAP_{y,app,bin,e} + \beta_2*OPCOST_{y,app,bin,e,b,r}}}{\sum_{e} \exp^{\beta_1*LTLCAP_{y,app,bin,e} + \beta_2*OPCOST_{y,app,bin,e,b,r}}}$$
(B-137)

where

LTMSHR_{y,app,bin,e,b,r} is the market share by year, application, bin, bulb type, housing type,

and Census division, and

 β_1 and β_2 are the choice weights for capital and operating costs, respectively.

After computing market shares for each application by bin, bulb type, housing type, and Census division, overall purchases of bulbs, *LTREPTOT* (B-142), are determined. First, bulb purchases needed for each projection year's floorspace additions for new construction, *HSEADD*, plus newly added floorspace in existing homes are developed. The required number of bulb purchases for this element of the residential stock includes floorspace area adjustments for both new construction and added floorspace in the existing stock of households.

$$LTNEEDED_{y,app,bin,e,b,r} = \\ [HSEADD_{y,b,r} * SQRFOOT_{y,b,r} / SQRFOOT_{RECSYR,b,r} \\ + EH_{y,b,r} * (EXSQRFOOT_{y,b,r} / EXSQRFOOT_{y-1,b,r} - 1)] \\ * BULBSPERHH_{app,b} * BULBBINSHARES_{app,bin} * LTMSHR_{y,app,bin,e,b,r}$$
 (B-138)

HSEADD_{y,b,r} is the number of new housing units constructed in the projection year

by housing type and Census division,

SQRFOOT_{v,b,r} is an input table of historical and projected average floorspace areas by

year, housing type, and Census division,

 $EH_{v,b,r}$ is the RECS year housing stock surviving in year y,

EXSQRFOOT_{y,b,r} is the projected average floorspace areas by year, housing type, and

Census division,

BULBSPERHH_{app,b} bulbs per household in the RECS year for each lighting application and

housing type, and

BULBBINSHARES_{app,bin} is the bulb shares by bulb type e within hours-of-use bins for each

application.

The remaining stocks of bulbs for the RECS year housing stock account for the year-to-year decay of the existing housing stock from the RECS year by housing type. Until the remaining stocks become zero, they are calculated as the difference between the bulb stock from the previous year less the number that expire in the remaining (surviving) housing stock this year. Bulbs in this stock existed in the RECS year and, as they expire, get added to *LTREPTOT*, (B-142).

$$LTSTOCKEX_{app,y,e,bin,b,r} = LTSTOCKEX_{app,y-l,e,b,r,bin}$$

$$-LTSTOCKEX_{app,RECSYR,e,b,r,bin} * HDR_b^{(y-RECSYR)} / BULBBINLIFE_{app,e,bin}$$
(B-139)

where

LTSTOCKEX_{app,RECSYR,e,b,r,bin} is the stock of bulbs in the RECS year for each application, bulb

type, housing type, Census division, and hours-of-use bin,

HDR_b is the percentage of the housing stock by housing type that

survives from one year to the next as in (B-2), and

BULBBINLIFE_{app,e,bin} is the life in years by bulb and hours-of-use bin.

Another component of bulb purchases is for the replacement of bulbs in existing homes. *LTREPFUT* represents the stock of bulbs that will need to be replaced each projection year for all bulbs purchased since the RECS year up to, but not including, the current model projection year. It is denoted as *LTREPFUT* because it represents replacements in future years after a bulb is purchased. For any given purchase, future replacements generally decline toward zero as more housing units decay from the stock and as fractions get repurchased every year (and get replaced with a new purchase which again generates its own stream of future replacement requirements). The exception is when purchases are made toward the end of the modeling horizon such that all bulbs would not have yet come up for replacement by the last modeled year of NEMS. Current-year replacements are based on the prior year's lighting stock, adjusted for the decay of the housing stock. For bulbs purchased in a particular year, replacements continue each future year until the number of replacements equals the total in the original purchase, adjusted for the housing stock that has retired:

$$LTREPFUT_{app,y,e,b,r,bin} = P_{app,y-1,e,b,r,bin} / BULBBINLIFE_{e,bin} * HDR_b$$

$$LTREPFUT_{app,y+1,e,b,r,bin} = P_{app,y-1,e,b,r,bin} / BULBBINLIFE_{e,bin} * HDR_b^2$$

$$LTREPFUT_{app,y+2,e,b,r,bin} = P_{app,y-1,e,b,r,bin} / BULBBINLIFE_{e,bin} * HDR_b^3, etc...$$
(B-140)

LTREPSTK represents the remaining purchased bulbs still in the lighting stock which accumulate from year to year as purchases are made.

$$LTREPSTK_{app, y, e, b, r, bin} = LTREPSTK_{app, y-1, e, b, r, bin} - LTREPFUT_{app, y, e, b, r, bin}$$
(B-141)

For each application, all of the required replacement bulbs are aggregated by bulb type, because the purchases will ultimately be reallocated based on purchase market shares, *LTMSHR* (B-137). These consist of replacements that may still be required from the original stock of RECS-year bulbs, replacements for bulbs purchased during the modeling horizon, and bulbs needed for new construction and floorspace additions.

$$LTREPTOT_{app,y,bin,b,r} = \sum_{e} [LTSTOCKEX_{app,y-1,e,b,r,bin} * HDR_b - LTSTOCKEX_{app,y,e,b,r,bin} + LTREPFUT_{app,y,e,b,r,bin} + LTNEEDED_{app,y,e,b,r,bin}]$$
(B-142)

Distributing the replacements to bulb types using LTMSHR,

$$LTREPSTK_{y,app,e,bin,b,r} = LTREPTOT_{app,y,b,r,bin} * LTMSHR_{app,y,e,b,r,bin}$$
 (B-143)

Consumption for the still-existing remaining RECS-year lighting stock is calculated as

$$LTSTOCKEXCONS_{y,app,e,bin,b,r} = \\ LTSTKEX_{app,y,e,b,r,bin} * APPBINHOURS_{app,bin} * 365 * BASEWATTSBULBS_{app,e} \\ * FACTOR$$
 (B-144)

where

APPBINHOURS_{app,bin} are the number of hours of use per day for this application and bin, is the RECS-year Watts for each of the bulb types used for this application, and converts Watts to Btu per hour as in (B-135).

Consumption for replacement bulbs is computed directly from BULBWATTS and stock:

$$LTREPCONS_{y,app,e,bin,b,r} = \\ LREPSTK_{app,y,e,b,r,bin} *APPBINHOURS_{app,bin} *365*BULBWATTS_{app,e,y}$$

$$*FACTOR$$
(B-145)

where

BULBWATTS_{app,e} is the current-year Watts for each of the bulb types used by application.

Total lighting consumption before adjustments for the price elasticity and rebound effects is just the sum of consumption from the surviving bulbs from the RECS year stock, LTSTOCKEXCONS, plus the consumption from all surviving purchases and replacements, LTREPCONS.

WTLEFF represents the average consumption per bulb and is used to calculate the efficiency rebound effect.

$$WTLEFF_{app,y,b,r,bin} = \frac{\sum_{e} \left(LREPSTK_{app,y,e,b,r,bin} * BULBWATTS_{app,e,y} + LTSTKEX_{app,y,e,b,r,bin} * BASEWATTSBULBS_{app,e} \right)}{\sum_{e} \left(LREPSTK_{app,y,e,b,r,bin} + LTSTKEX_{app,y,e,b,r,bin} \right)}$$
(B-146)

LTNUEC is the efficiency- and rebound-adjusted energy consumption by application, year, housing type, and Census division.

$$LTNUEC_{app,y,b,r} = \sum_{bin} LTBINSHARE_{app,bin} * LTUEC_{app,r,b} *$$

$$(WTLEFF_{app,y,b,r,bin} / BASEWATTSBINS_{app,bin})^{(1+\alpha)}$$
(B-147)

where

LTUEC_{app,r,b} is RECS-year unit energy consumption by application, Census division,

and housing type,

BASEWATTSBINS_{app,bin} is computed directly from lighting inputs for the RECS year and defined

below, and

α is the short-run price elasticity of demand.

$$BASEWATTBINS_{app,bin} = \sum_{e} BULBBINSHARES_{app,e,bin} * BASEWATTSBULBS_{app,e}$$
(B-148)

LTEQCN makes the adjustment for leap year and price elasticity and aggregates over bulb types and lighting bins:

$$LTEQCN_{y,app,b,r} = LEAPYR * \sum_{e,bin} (LREPSTK_{app,y,e,b,r,bin} + LTSTKEX_{app,y,e,b,r,bin}) *$$

$$LTNUEC_{app,y,b,r} * RSELAST$$
(B-149)

where

LTSTOCK_{v,b,r} is the number of general service bulbs in the current year by housing type and

Census division,

LTNUEC_{v,r,b} is the unit energy consumption for general service lighting by year, Census

division, and housing type, and

RSELAST is the short-term price elasticity function applied to electricity prices with

distributed lag weights EF1, EF2, and EF3, and the total short-term price

elasticity, α , as described in (B-39).

Finally, $LTCON_{y,r}$ is the reporting variable for NEMS and is merely the aggregation of $LTEQCN_{y,app,b,r}$ over all applications and all housing types.

APCNS (Miscellaneous Electric Loads/appliance consumption component)

For these miscellaneous electric loads (MELs), two input arrays, based on metrics from contracted report data and other sources, provide a penetration rate (number of units per household) and usage trend (kilowatthours per unit per year).

Throughout this section, the end use will be generalized as *MEL*. In the code, those three letters are replaced with three letters associated with each end use, such as *TVS* for televisions, *STB* for set-top boxes, *LPC* for laptop personal computers, and so on. The abbreviations associated with each end use are described in the RSMELS.TXT description in Appendix A.

To form the projection of usage, the usage index is multiplied by the base-year UEC. Specifically,

$$MELNUEC_{y,r,b} = MELUEC_{r,b} * MELEFF_{y,}$$
(B-150)

where

MELNUEC_{y,r,b} is the unit energy consumption for a MEL by year, Census division, and housing

type,

MELUEC_{r,b} is base-year unit energy consumption for a MEL by Census division and housing

type,

 $MELEFF_y$ is the usage index for a MEL in year y.

In some cases, this array is also multiplied by an income index, as certain uses are more likely to be adopted when households have higher disposable income:

$$MELNUEC_{y,r,b} = MELUEC_{r,b} * MELEFF_{y} * \left(\frac{MC_YPDR_{r,y}}{MC_YPDR_{r,baseyr}}\right)^{0.05}$$
(B-151)

MC_YPDR_{cy} is the personal disposable income variable from the Macroeconomic Activity

Module, and

0.05 is an exponent that estimates the correlation between changes in disposable

income and changes in adoption of certain MELs.

The income effect described above is applied to the following MELs: TVS, STB, HTS, VGC, DPC, LPC, MON, NET, BAT, DEH, PHP, SEC, and SPA.

Similarly, the projection of stock is formed by multiplying the equipment stock index by base-year stock:

$$MELEQP_{y,r,b} = \left(\frac{MELEQP_{r,b}}{EH_{y=baseyr,r,b}}\right) * MELPEN_y * \left(EH_{y,b,r} + NH_{y,b,r}\right)$$
(B-152)

where

MELEQP_{y,r,b} is the number of each MEL in the housing stock by year, Census division, and

housing type,

 $MELEQP_{r,b}$ is the base-year equipment stock for each MEL $MELPEN_y$ is the estimated penetration of each MEL for year y,

EH_{y,r,b} is the existing housing stock by year, Census division, and housing type, and

*NH*_{v.r.b} is the new housing stock by year, Census division, and housing type.

The final step of this component is to calculate consumption for each MEL:

$$MELCON_{y,r} = \sum_{b} \left(\frac{\left(MELEQP_{y,b,r} * MELNUEC_{y,b,r}\right) *}{RSELAST(f,r,\alpha,EF1,EF2,EF3,baseyr)} \right)$$
(B-153)

where

MELCON_{y,r} is the energy consumption of each MEL by year and Census division, and is the short-term price elasticity function with distributed lag weights EF1, EF2, and EF3, and the total short-term price elasticity, α , described in (B-39).

The remaining electricity consumption is captured in a catch-all category that includes small kitchen appliances, small consumer electronics, and small motor devices that are used in homes but do not fall into any of the other categories of equipment that have their own consumption components described above. The component computes the UEC on a per-housing-unit basis, by housing type and Census division. Based on historical data, a growth rate is estimated and applied to the UEC to project future energy consumption.

Electric appliance energy consumption is computed as follows:

$$APCON_{y,r} = \sum_{b} \frac{\left(EAUEC_{y,r} * EAPEN_{y,r}\right) * \left(EH_{y,r,b} + NH_{y,r,b}\right)}{*RSELAST(f,r,\alpha,EF1,EF2,EF3,baseyr)}$$
(B-154)

APCON $_{y,r}$ is other electric appliance energy consumption,EAUEC $_{y,r}$ is other electric unit energy consumption,EAPEN $_{y,r}$ is the growth rate in other electric unit energy consumption,RSELASTis the short-term price elasticity function with distributed lag weights EF1, EF2,and EF3, and the total short-term price elasticity, α , described in (B-39),EH $_{y,r,b}$ is the existing housing stock by year, Census division, and housing type, andNH $_{y,r,b}$ is the new housing stock by year, Census division, and housing type.

SHTCNS (Secondary heating energy consumption component)

Energy consumption by secondary heaters is calculated directly from shares by fuel read into the model from a user file:

$$SHTCON_{y,f,r} = \sum_{b} \left(SHTSHR_{r,f} * (NH_{y,b,r} + EH_{y,b,r}) * SHTUEC_{r,f,b} \right)$$

$$*AHSHELL_{y,f,r,b}$$

$$*RSELAST(f,r,\alpha,EF1,EF2,EF3,baseyr)$$
(B-155)

where

is the consumption of energy by secondary space heating equipment by year, SHTCON_{v,f,r} fuel, and Census division, $SHTSHR_{r,f}$ are shares of seven fuels for secondary space heating by Census division, is the number of old (existing) housing units in the current year by housing type $EH_{y,b,r}$ and Census division, $NH_{v,b,r}$ is the number of new (post-base-year) housing units in the current year by housing type and Census division, $SHTUEC_{r,f,b}$ is base-year unit energy consumption for secondary heating by Census division, fuel, and housing type, is the average post-base-year heating shell index by year, fuel, Census division, AHSHELL_{y,f,r,b} and building type, and is the short-term price elasticity function with distributed lag weights EF1, EF2, RSELAST and EF3, and the total short-term price elasticity, α , described in (B-39).

APPCNS (Non-electric miscellaneous appliance energy consumption component)
Other appliances refers to small appliances not covered in the other categories that do not use electricity as their primary fuel. Consumption alone is calculated.

The formula is a simple calculation from housing stock and unit energy consumption:

$$APLCON_{y,f,r} = \sum_{b} \left(\frac{\left(\left(EH_{y,b,r} + NH_{y,b,r} \right) * APPUEC_{y,b,r} \right)}{* RSELAST(f,r,\alpha,EF1,EF2,EF3,baseyr)} \right)$$
(B-156)

 $APLCON_{v,f,r}$ is the energy consumption by other appliances by year, fuel, and Census

division,

EH_{v,b,r} is the number of old (existing base-year) housing units in the current year by

housing type and Census division,

NH_{y,b,r} is the number of new (post-base-year) housing units in the current year by

housing type and Census division,

APPUEC_{r,f,b} are unit energy consumption estimates from the RSUEC.TXT file, by year,

housing type, and Census division, and

RSELAST is the short-term price elasticity function with distributed lag weights EF1, EF2,

and EF3, and the total short-term price elasticity, α , described in (B-39).

RDISTGEN (Distributed Generation Subroutine)

The Residential Demand Module includes a subroutine that develops penetration estimates for distributed electric generation technologies based on explicit cost and performance assumptions. The model is structured to allow for three technologies and can be readily expanded to include more if needed. The three technologies characterized are solar photovoltaics, fuel cells, and small distributed wind turbines.

The technology input file contains the following general categories of input data:

- Cost and performance of specific technologies (system capacity, cost per kW, efficiencies, etc.).
- Tax credits and regional subsidies, if any apply to a particular technology (this allows tax credit policies and subsidies to be included in the economic considerations).
- Technology window of availability, assumed to be a fixed interval of time after which a new
 technology characterization becomes operable. The interval length is flexible in the number of
 years it represents, and new technologies do not necessarily have to be different from the
 previous versions. The present practice is to characterize a *vintage* for each projection year in
 order to readily model proposed legislation; for extended NEMS time frames, however, multiyear time intervals beyond the projection horizon can be added for simplicity.
- Economic assumptions including tax rates, inflation rates for projecting results in the cash flow model, and financing assumptions such as down payment percentages and loan terms.
- Program-driven penetrations of technologies by Census division. These are viewed as noneconomic, supplemental to any economic penetrations.
- Market niche variables developed from RECS data and solar and wind resource maps produced by the National Renewable Energy Laboratory (NREL). Each Census division includes from two to four solar insolation niches. Niches are further subdivided, based on the level of electricity prices relative to the Census division average electricity price, into three cases: high, average, and low prices. In addition to solar insolation and relative electricity prices, the market niche variables also include average wind speed, the Census division share of housing units within a niche,

- average annual energy use (in kWh) per single-family housing unit, average roof area per single-family housing unit and the percentage of housing units considered rural (for wind turbine modeling). The solar niches are cross-classified by three levels of electricity prices, yielding a total of 63 market niche categories that are modeled separately.
- Utility interconnection limitations for each Census division. These limitations are intended to reflect state-level laws, regulations, and policies that encourage or limit distributed generation integration. State-level scores on a scale of zero (closed to interconnection) to one (open to interconnection) are aggregated to the Census division level by population. The scores are based on information from the Database of State Incentives for Renewables & Efficiency (DSIRE) and on updates on state legislative and public utility commission websites. Components include state-level renewable portfolio standards or goals, public benefit funds that support renewable resources, the existence of net-metering and interconnection standards and rules, whether fuel cells or CHP are eligible RPS technologies, and the existence of solar or wind access laws.

Distributed generation penetration is based on a cash flow simulation model. For each year in a NEMS run, a complete 30-year cash flow analysis is done for each of the three distributed generation technologies. For solar photovoltaic, an alternate penetration hurdle model using ZIP code-level input data is discussed later in this section. Cash flow analysis simulations are carried out by market niche for single-family homes. System characteristics, financial variables, solar insolation, and program-driven systems (e.g., the California solar program) are supplied to the subroutine via the RSGENTK.TXT input file.

The *payback* concept used in the residential Distributed Generation Subroutine is the number of years required for an investment to achieve a cumulative positive cash flow. This approach is related to, but different from, calculating what is commonly referred to as the *simple payback*. Simple paybacks are merely the investment cost divided by estimated annual savings and do not consider the timing of savings or costs that occur irregularly. The cumulative positive cash flow approach incorporates the time distribution of costs and returns including loan financing terms, tax credits, production credits (as under renewable portfolio standards), intermittent maintenance costs (e.g., inverter replacement for solar PV systems), inflationary increases in electricity rates, degradation in system output with age, and other factors that change over time. The current financing assumption is that, for new construction, investments in distributed generation technologies are rolled in with the home mortgage. The financing terms other than the mortgage rate are controlled through the distributed generation input file. The residential mortgage rates are supplied by the NEMS Macroeconomic Activity Module. Because tax credits are included in the input file, modeling alternative tax policies can usually be accomplished without changes to the model code.

Investments begin with a negative cumulative cash flow representing the down payment costs, assumed to be paid up front. In any subsequent year, the net of costs and returns can either be positive or negative. If the return is positive, then the cumulative net cash flow increases, and vice versa. For all technologies during the first full year of operation, electricity savings are realized, and loan payments and maintenance costs are paid. For fuel cells, natural gas costs are paid, but hot water savings are also realized via the capture and utilization of waste heat. Loan interest is separately tracked and leads to a tax savings (in the year following the payment) based on home mortgage deductibility. In the second full

year of operation, tax credits, if any, are also received. Based on current legislation, solar PV receives a 30% credit on installed capital costs through 2019, dropping to 26% in 2020, 22% in 2021, and discontinuing after 2021. These are modeled as one-time payments back to the consumer and, given the time value of money, such payments can have a major effect on increasing the cumulative net cash flow, because they are received near the front end of the cash flow.

Technology penetration rates for distributed generating technologies installed in new construction are determined by how quickly an investment in a technology is estimated to recoup its flow of costs. This penetration rate is allowed to be as high as 75% for distributed technologies if the investment *pays back* in less than one year, 30% if the investment pays back in one year, and correspondingly less for longer paybacks. The penetration function is assumed to follow a logistic functional form, as shown in equation (B-183), and a chart of the shape under different paybacks is provided in Figure 3. For retrofitting distributed generation into existing construction, penetration is capped by assumption at the lesser of 0.5% and the penetration rate into new construction divided by 40. The cap is in effect if penetration into new construction exceeds 20%.

In any given NEMS projection year, the total number of cash flow simulations performed equals the number of distributed technologies modeled (t=3), times the number of Census division niches (n=21), times the number of electricity price niches (*l*=3). An uppercase Y is used to denote years internal to the cash flow analysis in order to distinguish cash flow simulation years from NEMS model years (which are denoted with a lowercase y). The annual technology vintages will also be denoted with lowercase y because technology vintages currently *align* with NEMS projection years. Many of the concepts do not vary by solar or rate-level niches (subscripted by n and *l*, respectively). In cases where a concept varies by niche for only a subset of technologies, separate equations will be given for the relevant subsets, and in downstream equations the subscript will be placed in brackets to denote that it applies to only the relevant subset of technologies.

Even though the cash flow model is run by niche for each distributed generation technology and for each NEMS model year, many of the cash flow variables are only dimensioned by Y, the simulation year of the cash flow model itself, and are reused for other niches or technologies for a particular NEMS year. Such variables will be notated in the equations with the appropriate dimensions (indicating loops in the program), even if they are overwritten when the computer code is executed.

Technology capital cost is adjusted for learning effects on equipment cost for emerging technologies:

$$AdjCost_{t,y} = MIN \langle CapCost_{t,y}, C_{0,t} \cdot CumShip_{t,y}^{-\beta_t} \rangle$$
 (B-157)

where $CapCost_{t,y}$ is the tentative maximum cost from the distributed generation input file, and $C_{0,t}$ and β_t are technology-specific (hence subscript t) learning cost parameters, and $CumShip_{t,y}$ represents cumulative shipments (in MW) for NEMS model year y, for residential and commercial buildings and utility installations combined (supplied via the global interface). Learning effects are modeled for photovoltaic, fuel cell technologies and wind turbines.

Calculated Maximum kW for Photovoltaic Systems:

The calculated maximum capacity (in kW) for photovoltaic systems, xCalcKW_{t=1,n,l,v} is allowed to vary from the menu capacity in the RSGENTK.TXT input file. The capacity is niche-dependent with the target maximum size being enough to serve the residence's annual electricity requirements, subject to maximum and minimum size constraints for the technology being evaluated. In the case of solar photovoltaics, only 90% of the properly oriented half of roof area is considered to be suitable for solar PV installation. Available roof area per house is developed from floor space and number of floors estimated from RECS and provided as part of the niche inputs in RSGENTK.TXT. The modules are also assumed to be placed at *latitude tilt* which requires roughly twice the roof area for minimum rack spacing when installed on flat roofs. On sloped roofs, solar modules are assumed to be close enough to being *flush-mounted* so that a one-square-foot module requires one square foot of roof area. An estimated 75% of residential roofs are sloped; so, on average, for a given amount of available residential roof area, 75%*1.0 + 25%*2.0 (or 1.25) square feet of roof area are required to mount a one-square-foot module. Based on these constraints, the kW capacity of the maximum module area is calculated as

$$xCalcKW_{t=1,n,l,y} = RoofAreaPerHH_{n,l}/1.25 \cdot 90\% \cdot 50\% / xSqftperkW_{y}$$
(B-158)

Note: see equation (B-167) below for the calculation of $xSqftperKW_y$ which is recalculated each year based on module conversion efficiency for the appropriate year vintage.

Installed Equipment Cost:

Installed equipment cost, $EqCost_{t,y}$, is the learning-adjusted cost from above plus the installation cost which is an input from the distributed generation input file times the system capacity:

$$EqCost_{t,y} = (AdjCost_{t,y} + InstCost_{t,y}) \cdot kW_{t,y}$$
(B-159)

For solar photovoltaics, $kW_{t,y}$ is replaced by $xCalcKW_{t,n,l,y}$ from (B-158).

Initial Outlay Cost:

$$DownPay_{t,y} = EqCost_{t,y} \cdot DownPayPct$$
(B-160)

Annual Levelized Payment Calculation:

$$Payment_{t,y} = \left[EqCost_{t,y} - DownPay_{t,y} \right] \cdot \frac{IntRate}{1 - (1 + IntRate)^{-Term}}$$
(B-161)

where the term in brackets is the amount financed,

IntRate is the interest rate for the loan and

Term is the number of years over which the loan payments are amortized.

Outlays for Capital Relating to Down Payments and Borrowing Costs:

$$Outlay_{t,y,Y=I} = DownPay_{t,y}$$

$$Outlay_{t,y,I < Y \le Term} = Payment_{t,y}$$

$$Outlay_{t,y,Y > Term} = 0$$
(B-162)

Calculations of Loan Interest Paid and the Value of Tax Credits:

$$\begin{aligned} Prin_{t,y,Y} &= Payment_{t,y} - IntAmt_{t,y,Y} \\ where &\quad IntAmt_{t,y,Y} &= IntRate \cdot LoanBal_{t,y,Y-1}, \ and \\ &\quad 1 < Y \leq Term \end{aligned} \tag{B-163}$$

 $Prin_{t,y,Y}$ is the amount of principal paid on the loan in each year Y of the cash flow analysis and is also used to determine the loan balance for the next year of the analysis. It is computed as the difference between the levelized payment and the interest paid: $IntAmt_{t,y,Y}$ is the interest paid for the loan in each year of the analysis. This variable is a component of the tax deduction calculation. It is computed as last year's ending principal balance, $LoanBal_{t,y,Y-1}$, times the interest rate on the loan. $LoanBal_{t,y,Y}$ is the principal balance of the loan for each year of the analysis. The loan balance reduces over time according to the formula:

$$LoanBal_{t,y,Y} = LoanBal_{t,y,Y-I} - Prin_{t,y,Y}$$
(B-164)

 $TaxCredit_{t,y,Y}$ is the allowed tax credit and can vary both by technology and vintage for distributed generation investments favored by the tax code. The credit is assumed to be collected in Year 3 of the cash flow analysis.

$$\begin{split} TaxCredit_{t,y,Y} &\equiv MIN \Big\langle EqCost_{t,y} \cdot TaxCreditPct_{t,y}, TxCreditMax_{t,y} \Big\rangle, \\ & if \ Y = 3, \\ 0, \quad if \ Y \neq 3 \end{split} \tag{B-165}$$

Annual kWh Generated by Technology:

AnnualKWH $_{t,n,y}$ represents the base level of annual system kWh generation for a new system for the specific technology and vintage being analyzed.

For photovoltaics (technology, t=1) annual generation is determined by system size, efficiency and solar availability as follows:

$$AnnualKWH_{t,n,y} = \begin{pmatrix} ElEff_{t,y} \cdot SolarIns_n \cdot 365.25 \cdot \\ xSqftperKW_y / 10.8 \cdot LossFac_{t,y} \end{pmatrix} \cdot xCalcKW_{t,n,y}$$
 (B-166)

The parenthetical expression represents the kWh generated by a 1-kW system, so this amount is then multiplied by system kW to yield the annual generation amount. Solar insolation, *SolarIns_n* varies within a Census division by niche, and is expressed in average daily kWh falling on a square meter area and annualized in equation (B-168). The insolation value is then adjusted for module square footage (10.8 square feet per square meter) and the electrical efficiency of a prototypical photovoltaic technology. Finally a loss factor (the percentage of the generation reaching the outlet) allows further adjustment of annual kWh available to the building by accounting for downstream electrical losses. The subroutine assumes that a typical solar PV module in 2009 has a system efficiency of 14% and requires an area of 77 square feet for a 1-kW system. The variable for the estimated photovoltaic array square footage for a 1-kw system, *xSqftperKW_v*, depends inversely on the electrical efficiency of the system, *ElEff_{1,v}* as follows:

$$xSqftperKW_{y} = 77 \cdot \frac{0.14}{ElEff_{I,y}}$$
 (B-167)

The higher the efficiency, the smaller the square footage that will be required for a given system capacity. As system size is allowed to vary, higher-efficiency modules lead to higher-capacity systems being potentially selected.

For fuel cells (t=2), annual system generation for a 1-kW unit is determined by hours-of-use multiplied by an availability factor and a loss factor. Annual generation is determined by multiplying the amount for a 1-kW system by system capacity:

$$AnnualKWH_{t,y} = (OperHours_t \cdot Avail_{t,y} \cdot LossFac_{t,y}) \cdot kW_{t,y}$$
(B-168)

For distributed wind turbines (t=3), annual system generation is determined by turbine capacity ($kW_{3,y}$), efficiency and average wind speeds as follows:

$$AnnualKWH_{t,n,y} = \left(\frac{ElEff_{t,y}}{ElEff_{t,l}} \cdot (.0645 - .0670 \cdot xMpS_n + .0210 \cdot xMpS_n^2 - \\ 0.0011 \cdot xMpS_n^3)\right)$$

$$\cdot LossFac_{t,y} \cdot kW_{t,y}$$
(B-169)

 $xMpS_n$ denotes average wind speed in meters per second for niche n. Distributed wind turbine penetration is also assumed appropriate and suitable for only rural residences (developed from RECS and input in RSGENTK.TXT due to permitting issues and site limitations.

 $KWH_{t,y,Y}$ is the actual kWh generated in each of the years of the cash flow analysis. The actual generation is the ideal generation adjusted for degradation as the system ages. Currently, only photovoltaic generation has a non-zero degradation factor. Its value of 0.01 assumes a 1%-per-year loss in output as the modules age. Degradation begins in the year after the system is fully in use, which, in the cash flow model assumptions, is year 3.

$$KWH_{t,y,Y} = AnnualKWH_{t,[n],y} \cdot \left(1 - Degradation_{t,y}\right)^{(Y-2)}$$
(B-170)

Fuel Consumption for Fuel-using Distributed Generation Technologies:

Fuel consumption for fuel cells (t=2) is denoted by the variable $FuelInput_{t,y}$ and is calculated in MMBtu of the input fuel used by the technology:

$$FuelInput_{t,y} = \frac{0.003412 \cdot OperHours_{t} \cdot Avail_{t,y}}{ElEff_{t,y}} \cdot kW_{t,y}$$
(B-171)

Calculation of Waste Heat Available for Water Heating Use:

 $BTUWasteHeat_{t,y}$ represents the amount of waste heat potentially available for providing an offset to home water heating. It is also computed in MMBtu and is the difference between the fuel input and the energy expended on electricity generation, multiplied by the waste heat recovery efficiency specific to this technology and vintage.

$$BTUWasteHeat_{t,y} = \\ \left(FuelInput_{t,y} - 0.003412 \cdot AnnualKWH_{t,y}\right) \cdot WhRecoveryEff_{t,y} \tag{B-172}$$

The amount of available waste heat is used to offset water heating end use service demand up to the average housing unit consumption from RECS:

$$WaterHeatingMMBtu_{t,y}$$

$$= MIN \langle BTUWasteHeat_{t,y}, AvgWaterHtgMMBtu \rangle$$
(B-173)

Any amount of waste heat generated beyond the average water heating requirements is not assumed to offset end-use fuel requirements.

Net Fuel Cost:

 $BaseYrFuelCost_{t,y}$ is the initial fuel costs for operating the generation technology net of savings stemming from displaced water heating. It is calculated from the current fuel price and fuel input and converted to the same year constant/ real dollars as the technology capital costs.

$$BaseYrFuelCost_{t,y} = \\ \left(FuelInput_{t,y} - WaterHtgMMBtu_{t,y}\right) \cdot FuelPrice_{r,y}$$
(B-174)

 $FuelCost_{t,y,Y}$ is the nominal-dollar value fuel cost for the technology net of any water heating cost savings from using waste heat:

$$FuelCost_{t,y,Y} = BaseYrFuelCost_{t,y} \cdot (I + inflation)^{(Y-2)}$$
(B-175)

Value of Electricity Savings Calculations:

 $ValElecSaveBase_{t,n,l,y}$ represents the calculated value of generated electricity for the initial year of the cash flow simulation for a particular solar and price level niche (n,l). This value is further adjusted to account for inflation and generation efficiency degradation in a later calculation described below.

Case 1: Photovoltaics

If generation is less than average electricity usage (i.e., $AnnualKWH_{t,y} \le AvgKWH$), then savings are valued at the air conditioning price, $PELRSOUT_{r,y,AC}$ (because photovoltaic generation tends to correlate with the need for air conditioning):

$$ValElecSaveBase_{t=1,n,l,y} = \begin{bmatrix} PELRSOUT_{r,y,AC} \cdot xRateScala\,r_{n,l} \cdot 0.003412 + \\ EPRPSPR_{y} / 1000 \cdot xScaleRPS_{t} \\ \cdot AnnualKWH_{t[n],y} \end{bmatrix} \tag{B-176}$$

The factor 0.003412 converts prices in dollars per million Btu to dollars per kWh. The potential to model renewable portfolio standard credits is incorporated in NEMS. The credit is received if it applies; however, in current reference case runs, RPS credits are not received. The credit amount, *EPRPSPR_y*, is provided by the NEMS Electricity Market Module and must be divided by 1,000 because it is provided in mills per kWh⁴. If the credit is received, the scalar is set to a value greater than zero (e.g., for triple credits, the scalar is 3). Because RPS credits often have a last year or *sunset* year, the cash flow simulation also tracks the calendar year of each of the simulated years and zeroes out the credit if the calendar year exceeds the sunset year. If generation exceeds average usage, then the excess kWh are sold to the grid at the marginal price for utility purchases (*PELME_{t,y}*) and the value is:

$$\begin{aligned} \textit{ValElecSaveBase}_{t,n,l,y} &= 0.003412 \cdot \begin{bmatrix} \textit{PELRSOUT}_{r,y,AC} \cdot \textit{xRateScala} \ r_{n,l} \cdot \textit{AvgKwh} \\ + \textit{PELME}_{r,y} \cdot \left(\textit{AnnualKWH}_{t,y} - \textit{AvgKwh} \right) \end{bmatrix} \\ &+ \textit{EPRPSPR}_{y} / 1000 \cdot \textit{xScaleRPS}_{t} \cdot \textit{AnnualKWH}_{t,y} \end{aligned} \tag{B-177}$$

Case 2: All other technologies

The air conditioning price, $PELRSOUT_{r,y,AC}$, is replaced by $PELRS_{r,y}$, the average residential electricity price. RPS credits are generally not available for the non-renewable technologies. Therefore, when RPS credits are modeled, scalars for non-renewable technologies are set to zero.

⁴ A mill is equal to 1/1000 of a U.S. dollar, or 1/10 of one cent. Mills per kilowatthour (kWh) equals dollars per megawatthour (mWh). To convert mills per kWh to cents per kWh, divide mills per kWh by 10.

 $ValElecSave_{t,n,l,y,Y}$ is the nominal dollar (inflated) value of $ValElecSaveBase_{t,n,l,y}$ with adjustment for output degradation:

$$\begin{aligned} ValElecSav\,e_{t,n,l,y,Y} &= \\ &ValElecSav\,eBas\,e_{t,n,l,y} \cdot \left(l + inflation\,\right)^{(Y-2)} \\ &\cdot \left(l - Degredation_{t,y}\right)^{(Y-2)} \end{aligned} \tag{B-178}$$

Maintenance Cost Calculations:

 $MaintCost_{t,y,Y}$ is the calculated nominal dollar cost of maintenance for the specific technology and vintage being analyzed. $MaintCostBase_{t,y}$ is the annual maintenance cost per kW and $xIntervalCst_{t=1,y}$ is the interval maintenance cost for inverter replacement per kW if the technology being evaluated is a photovoltaic system (i.e., technology index 1). $xIntervalCst_{t=1,y}$ is non-zero only if the cash flow model year, Y, is an inverter replacement year based on the replacement interval for solar photovoltaic system vintage, y.

$$MaintCost_{t,y,Y} = kW_{t,y} \cdot \left(MaintCostBase_{t,y} + xIntervalCst_{t=1,y}\right) \cdot \left(1 + inflation\right)^{(Y-2)}$$
(B-179)

Deductible Expenses for Personal Income Taxes:

$$TaxDeduct_{t,y,Y} = \begin{pmatrix} IntAmt_{t,y,Y-1} - MaintCost_{t,y,Y-1} + \\ FuelCost_{t,y,Y-1} - ValElecSave_{t,y,Y-1} \end{pmatrix} * TaxRate + TaxCredit_{t,y,Y}$$
 (B-180)

Cash Flow and Investment Payback Years:

NetCashFlow_{t,n,l,y,Y} and CumCashFlow_{t,n,l,y,Y}:

$$\begin{aligned} Net Cash Flow_{t,n,l,y,Y} &= \\ Val Elec Save_{t,n,l,y,Y} &+ Tax Deduct_{t,y,Y} - Out Lay_{t,y,Y} - \\ &Fuel Cost_{t,y,Y} - Maint Cost_{t,y,Y} \end{aligned} \tag{B-181}$$

 $\textit{CumCashFlow}_{t,n,l,y,Y}$ is defined as the accumulated sum of all prior $\textit{NetCashFlow}_{t,n,l,y,Y}$ amounts.

Simple Payback Years:

 $SimplePayback_{t,n,l,y}$ is defined as the first year in the cash flow stream for which an investment has a positive $CumCashFlow_{t,n,l,y,Y}$ (i.e., the Y if and when $CumCashFlow_{t,n,l,y,Y}$ first becomes greater than or equal to 0). Note that $SimplePayback_{t,n,l,y}$ is stored as a real (floating point) number and not rounded off to whole years – this will affect the calculated maximum penetration of the technology, as described below.

Real-valued Simple Payback Calculation:

Let Y' be the integer-valued year in the 30-year cash flow simulation for which $CumCashFlow_{t,y,Y'}$ achieves a non-negative value. Call this value $IntSimplePayback_{t,n,l,y}$ to represent the integer-valued payback. The real-valued $SimplePayback_{t,n,l,y}$ for this technology is interpolated as follows:

$$SimplePayback_{t,n,l,y} = IntSimplePayback_{t,n,l,y} - \\ \frac{CumCashFlow_{t,n,l,y,Y'-I} + NetCashFlow_{t,n,l,y,Y'}}{NetCashFlow_{t,n,l,y,Y'}}$$
 (B-182)

Because Y' is the first year for which $CumCashFlow_{t,n,l,y,Y}$ is greater than or equal to zero, its prior-year value (in year Y'-1) was less than zero. If $CumCashFlow_{t,n,l,y,Y'-1}$ is small in absolute value relative to $NetCashFlow_{t,n,l,y,Y'}$, the right-hand term is near unity, indicating that the payback was achieved close to the beginning of Y.

Maximum Penetration into New Construction:

$$MaxPen_{t,n,l,y} = \frac{PenParm_{t}}{SimplePayback_{t,n,l,y}}$$
(B-183)

 $PenParm_t$ is set to 0.3 for all technologies. Thus the asymptotically approached $MaxPen_{t,n,l,y}$ for these technologies with a 1-year payback will be 30%. Because $SimplePayback_{t,n,l,y}$ is a real-valued number, it can potentially achieve values of less than one. For a $SimplePayback_{t,n,l,y}$ of 0.5 years, $MaxPen_{t,n,l,y}$ is 60%.

Easing of Interconnection Limitations:

$$Inxdecay_{r,y} = MIN \left\langle 1.0, Inx_r + (1.0 - Inx_r) \cdot \frac{y - Inxfy}{Inxly - Inxfy} \right\rangle$$
 (B-184)

Inxfy and Inxly define the interval (in calendar years) over which interconnection limitations decrease to 0 and Inxdecay_{r,y} approaches 1. Inx_r values range between 0 and 1 and are aggregated from state to Census division level by population. State scores are based on the presence of rules, regulations, and policies that affect utility grid interconnection of distributed generation and are determined by EIA analyst judgment.

Penetration Function Formula for New Construction:

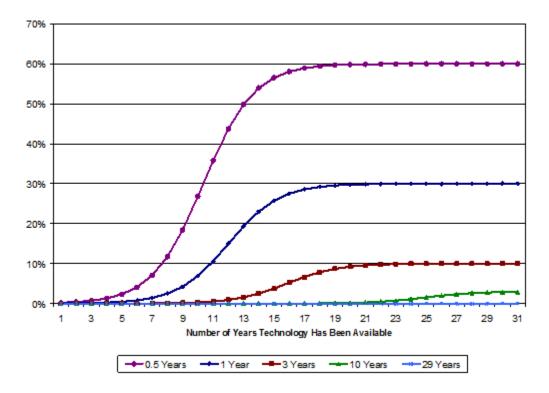
For a given value of $SimplePayBack_{t,n,l,y}$, penetration in NEMS model year y is an increasing function of y.

$$Pen_{t,n,l,y} = Inxdecay_{r,y} \cdot \left[MaxPen_{t,n,l,y} - \frac{1}{\frac{1}{MaxPen_{t,n,l,y}} + e^{\left[\alpha_{t} \cdot \left(y - RECSYear + 1 - SimplePayBack_{[t]\downarrow y]}\right)\right]}} \right]$$
(B-185)

For new construction, $Pen_{t,n,l,y}$ is constrained to a maximum penetration of 75%.

Figure 3 below shows the logistic-shaped penetration function for a variety of years to achieve positive cumulative net cash flow:

Figure 3. Penetration rate of distributed generation into new construction for selected years to positive cumulative net cash flow



Penetration Function Formula for Existing Construction:

Penetration of distributed generation into the existing housing stock is limited to a maximum of 0.5% or one-fortieth of the penetration into new construction, whichever is less. It is denoted by $DeltaPen_{t,n,l,y}$.

Outputs to the Residential Demand Module and NEMS:

Explicit recognition of the Census-division dimension commences here. Refer to the variable descriptions in the Residential Distributed Generation Equipment File section of Appendix A for variables not explicitly defined here. *Units_{y,r,t}* denotes the accumulated total number of units in NEMS model year y employing the relevant type of generation technology by Census division and is the sum of *Units_{y-1,r,t}* plus penetration into new construction (*HSEADD*) plus penetration into existing housing units (EH) for the current NEMS model year plus additional exogenous penetration (*ExogPen*) representing programdriven amounts. The subscripts denoting Census division are restored for this section of the documentation, to explicitly describe the interface with NEMS.

*Units*_{y,r,t} accumulates the number of projected distributed generation units based on penetration rates into new (*HSEADD*) and existing housing units (*EH*) for the share of households in each niche (*xHHShare*):

$$Units_{y,r,t} = Units_{y-l,r,t}$$

$$+ \sum_{n,l \in r} \left[\frac{\left(ExogPen_{y,r,t} - ExogPen_{y-l,r,t}\right) + \left(Pen_{t,n,l,y} \cdot HSEADD_{r,y} + DeltaPen_{t,n,l,y} \cdot EH_{r,y}\right) \right] \cdot xHHShare_{n,l}$$
(B-186)

Trills_{y,r,t} accumulates total generation (own use plus grid sales) and converts it to trillions of Btu:

$$Trills_{y,r,t} = Trills_{y-1,r,t}$$

$$+ \sum_{n,l \in r} \left[\frac{\left(ExogPen_{y,r,t} - ExogPen_{y-1,r,t}\right) + \left(Pen_{t,n,l,y} \cdot HSEADD_{r,y} + DeltaPen_{t,n,l,y} \cdot EH_{r,y}\right) \right] \cdot xHHShare_{n,l} \cdot AnnualKWH_{t,n,l,y} \cdot 3412 \cdot 10^{12}$$
(B-187)

 $TrillsOwnUse_{y,r,t}$ accumulates total electricity generation for on-site consumption (own use) and converts it to trillions of Btu. It is the minimum of 1) the average electric consumption from RECS, and 2) the annual generation.

$$TrillsOwnUse_{y,r,t} = TrillsOwnUse_{y-1,r,t} + \\ \begin{bmatrix} \left(ExogPen_{y,r,t} - ExogPen_{y-1,r,t} \right) + \\ \left(Pen_{t,n,l,y} \cdot HSEADD_{r,y} + DeltaPen_{t,n,l,y} \right) \\ \cdot EH_{r,y} \\ \cdot xHHShare_{n,l} \\ \cdot MIN \left\langle AnnualKWH_{t,n,l,y}, RECSAvgKwh_{n,l} \right\rangle \\ \cdot 3412 \cdot 10^{12} \end{bmatrix}$$
(B-188)

FuelUsage_{y,r,t} accumulates FuelInput_{r,t,y} and converts from MMBtu to trillions of Btu:

$$FuelUsage_{y,r,t} = FuelUsage_{y-1,r,t} + \\ \sum_{n,l \in r} \left[\frac{\left(ExogPen_{y,r,t} - ExogPen_{y-1,r,t} \right) + \left(Pen_{t,n,l,y} \cdot HSEADD_{r,y} + DeltaPen_{t,n,l,y} \cdot EH_{r,y} \right) \right] \\ \cdot xHHShare_{n,l} \cdot FuelInput_{r,t,y} \cdot 10^{6}$$
(B-189)

 $HWBtu_{y,r,t}$ accumulates $WaterHtgMMBtu_{r,t,y}$ and converts it to trillions of Btu:

$$\begin{aligned} HWBtu_{t,r,y} &= HWBtu_{t,r,y-1} + \\ &\sum_{n,l \in r} \left[\frac{\left(ExogPen_{y,r,t} - ExogPen_{y-1,r,t}\right) + \left(Pen_{t,n,l,y} \cdot HSEADD_{r,y} + DeltaPen_{t,n,l,y} \cdot EH_{r,y}\right) \right] \\ &\cdot xHHShare_{n,l} \cdot WaterHtgMMBtu_{r,t,y} \cdot 10^6 \end{aligned} \tag{B-190}$$

 $Invest_{y,r,t}$ is the current-year investment in distributed generation resources in millions of constant/ real dollars:

$$Invest_{y,r,t} = Invest_{y-1,r,t} + \sum_{n,l \in r} \left[\frac{\left(ExogPen_{y,r,t} - ExogPen_{y-1,r,t}\right)}{\left(Pen_{t,n,l,y} \cdot HSEADD_{r,y} + DeltaPen_{t,n,l,y} \cdot EH_{r,y}\right)} \right]$$

$$\cdot xHHShare_{n,l} \cdot EqCost_{t,y} \cdot kW_{t} \cdot 10^{6}$$
(B-191)

Beginning with AEO2017, the cash flow analysis for residential solar photovoltaic penetration has been superseded by an econometric hurdle model using ZIP code-level input data. The *UseNewModel* variable in the RGENTK.TXT input file is used to switch between the new ZIP code model and the old cash flow model for PV; the cash flow model continues to be used for non-PV distributed generation technologies. Detailed information on how the econometric model was developed, the data it incorporates, and its functional forms can be found in *Using Hurdle Models for Long-term Projections of Residential Solar Photovoltaic Systems Installations*.

The hurdle model uses ZIP code level data from solar PV project databases, NREL, the U.S. Census Bureau's American Community Survey (ACS), and other sources. The model estimates the number of residential solar PV systems to be installed for each of the ZIP codes characterized in the RGENTK.TXT input file, starting in *EstYear* as determined by ACS data availability. From the base year through *EstYear*, an additive factor, *ExogPVMistier*,, is used as in (B-192) to calibrate total capacity by Census division to historical exogenous PV capacity, *xexogpent*, *ExogPVMistier*, capacity is held constant from *EstYear* onward. The number of PV systems associated with *ExogPVMistier*, is added to *Unitsy*, and generation associated with *ExogPVMistier*, is shared out to *Trillsy*, and *TrillsOwnUsey*, t.

$$ExogPVMistie_{r,v} = ExogPen_{r,v} - Capacity_{r,v}$$
 (B-192)

ExogPVMistier,y is the adjustment factor used to calibrate solar PV capacity,

ExogPen represents program-driven or historical capacity from RSGENTK.TXT, and

Capacity is the calculated capacity from the hurdle model.

$$Capacity_{r,y} = Capacity_{r,y} + ExogPVMistie_{r,y}$$
 (B-193)

$$Units_{y,r,t} = Units_{y,r,t} + \left(\frac{ExogPVMistie_{r,r}}{kW_{t,y}}\right)$$
(B-194)

where

 $kW_{t,y}$ is the average solar PV system capacity from RSGENTK.TXT.

$$Trills_{y,r,t} = Trills_{y,r,t} + \left(\frac{ExogPVMistie_{r,y}}{kW_{t,y}}\right) \cdot AnnualKWH_{t,z,l,y} \cdot 3412 \cdot 10^{12}$$
 (B-195)

$$TrillsOwnUse_{y,r,t} = TrillsOwnUse_{y,r,t} + \left(\frac{TrillsOwnUse_{y,r,t}}{Trills_{y,r,t}}\right) \cdot \left(\frac{ExogPVMistie_{r,y}}{kW_{t,y}}\right) \cdot AnnualKWH_{t,z,l,y} \cdot 3412 \cdot 10^{12}$$
(B-196)

FUELCN (Fuel consumption totals component)

The total residential energy consumption for the nation is computed by summing end-use service consumption by fuel for each Census division. Division by 1,000,000 converts units from million Btu per year to trillion Btu per year. The factor *LEAPYR* in each equation takes on the value of 366/365 in near-term years (i.e., history and years up through the STEO benchmarking period); otherwise it has the value of 1.

Natural Gas (ng)

$$RSFLCN_{y,ng,r} = \frac{\left(HTRCON_{y,ng,r} + H2OCON_{y,ng,r} + CKCON_{y,ng,b,r} + GASINPUT_{y,r} + CKCON_{y,ng,r} + CKCON_{y,ng,r} + SHTCON_{y,ng,r} + APLCON_{y,ng,r} + APLCON_{$$

Electricity (el)

$$RSFLCN_{y,el,r} = \\ \left(HTRCON_{y,el,r} + H2OCON_{y,el,r} + CKCON_{y,el,b,r} + REFCON_{y,r} + DRYCON_{y,el,r} + COOLCN_{y,el,r} + SHTCON_{y,el,r} + APCCON_{y,r} + FRZCON_{y,r} + CSWCON_{y,r} + DSWCON_{y,r} + LTCON_{y,r} + SPACON_{y,r} + CFCON_{y,r} + CMCON_{y,r} + MOCON_{y,r} + RCCON_{y,r} + HACON_{y,r} + SSCON_{y,r} + FANCON_{y,r} + COON_{y,r} + TVCON_{y,r} - ANNUALKWH_{y} + ANNUALKWH_{y} + COON_{y,r} + TVCON_{y,r} - ANNUALKWH_{y} + COON_{y,r} + COON_{y,r} + TVCON_{y,r} + ANNUALKWH_{y} + COON_{y,r} + COON_$$

* LEAPYR

* LEAPYR

Distillate Fuel Oil (ds)

$$\frac{RSFLCN_{y,ds,r}}{\left(HTRCON_{y,ds,r} + H2OCON_{y,ds,r} + SHTCON_{y,ds,r} + APLCON_{y,ds,r}\right)}{1,000,000} * (B-199)$$

LEAPYR

LPG (lpg)

$$RSFLCN_{y,lpg,r} = \frac{\left(HTRCON_{y,lpg,r} + H2OCON_{y,lpg,r} + CKCON_{y,lpg,b,r} + \right)}{SHTCON_{y,lpg,r} + APLCON_{y,lpg,r}} * LEAPYR$$

$$1,000,000$$
(B-200)

Kerosene (ks)

$$RSFLCN_{y,ks,r} = \frac{\left(HTRCON_{y,ks,r} + SHTCON_{y,ks,r}\right)}{1,000,000} * LEAPYR$$
(B-201)

Coal (cl)

$$RSFLCN_{y,cl,r} = \frac{SHTCON_{y,cl,r}}{1,000,000} * LEAPYR$$
(B-202)

Wood (wd)

$$RSFLCN_{y,wd,r} = \frac{\left(HTRCON_{y,wd,r} + SHTCON_{y,wd,r}\right)}{1.000.000} * LEAPYR$$
(B-203)

Geothermal (geo)

$$RSFLCN_{y,geo,r} = \frac{\left(HTRCON_{y,geo,r} + COOLCN_{y,geo,r}\right)}{1,000,000} * LEAPYR$$
(B-204)

National Total (us)

$$RSFLCN_{y,US} = \sum_{r,f} \left(RSFLCN_{y,f,r} \right)$$
 (B-205)

RSBENCH (Benchmarking fuel consumption totals)

For historical years, the present year, and near-term future (through the current *Short-Term Energy Outlook* [STEO] horizon), fuel consumption totals are benchmarked to maintain consistency across EIA products. These products include the State Energy Data System (SEDS), which provides state totals (then aggregated to the Census division level), and the *Monthly Energy Review* (MER), which provides national totals distributed to the Census division levels based on the previous year's SEDS distribution. Fuel consumption levels in the Residential Demand Module are benchmarked to the specific values in these historical publications.

For near-term future years, national fuel consumption totals are intended to be within a reasonable percentage of the STEO values. Currently, 2% is considered reasonable, but occasionally a larger difference may be accepted for a specific fuel if warranted by inherent differences in modeling structures. Beyond the benchmarked period (i.e., beyond the STEO horizon), there is an option to maintain these benchmark factors throughout the projection. Benchmark factors may be additive, meaning the difference between the modeled fuel total and benchmarked fuel total is maintained throughout, or multiplicative, meaning the ratio is maintained throughout. Fuels with more consumption such as electricity, natural gas, distillate fuel oil, and LPG use additive benchmarking, while kerosene uses multiplicative benchmarking.

Because benchmarking factors must be attributed to certain end uses, the benchmark factors for natural gas, distillate fuel oil, LPG, and kerosene are attributed to space heating. For electricity, the benchmark is applied to miscellaneous uses not specifically modeled, also known as *electric other*.

Appendix C: Bibliography

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Appendix D: Data Quality

This Appendix discusses the quality of the Residential Energy Consumption Survey (RECS), which forms the basis of the historical housing stock, appliance stock, and technology information that drives the NEMS Residential Demand Module. Data quality information pertinent to additional sources used in the module development is not available for this report.

The RECS data collection procedure relies on two instruments: the housing unit survey and the energy supplier survey. Data are collected from a representative sample of housing units through personal interviews. Billing data are then collected through mail questionnaires from the companies supplying energy to the participating housing units, provided that authorization is obtained from the housing units. The results of the housing unit and energy supplier surveys are presented in the U.S. Department of Energy documentation of the RECS.

Stage I of RECS consists of personal interviews. The sample for the interviews is drawn from the population of housing units occupied as primary residences in the 50 states and the District of Columbia. The sample design process is composed of five steps that disaggregate the geographic scope into housing clusters of approximately five housing units to be surveyed.

The interview responses provide information on housing characteristics, fuels used, housing unit measurements, fuel bills, kitchen appliances, home appliance and electronics, space heating, air conditioning, water heating, miscellaneous uses, residential transportation, household characteristics, and energy expenditure assistance. Housing unit respondents are also asked to sign authorization forms to allow access to their billing records with energy suppliers.

Stage II of the survey design consists of a mail questionnaire for energy suppliers of the housing units interviewed in Stage I. Suppliers of residential electricity, natural gas, distillate fuel oil, kerosene, and liquefied propane gas (LPG) are contacted in Stage II. For the RECS, each supplier was asked to supply billed quantities and expenditures for the housing units interviewed in Stage I.

Quality assurance begins with a manual verification of the interview data from Stage I. The questionnaires are checked for completeness and consistency. Interview responses are compared to energy supplier data, and respondents are contacted in the event that an inconsistency persists. These data collection and verification procedures ensure the quality of the survey data.