



# π IN THE SKY<sup>11</sup>

## ANSWER KEY

### MOON MAPPERS

How far does each rover have to drive to survey its portion of the Moon's surface?

- 1 Convert radians to degrees, then use the Pythagorean theorem to find the swath width.

$$(\pi/2) \cdot (180^\circ/\pi) = 90^\circ$$

$$a^2 + b^2 = c^2 \Rightarrow (2 \text{ m})^2 + (2 \text{ m})^2 = c^2 \Rightarrow c = 2\sqrt{2} \text{ m}$$

- 2 Determine the number of swaths the rovers need to drive to map the entire square.

$$20 \text{ m} / 2\sqrt{2} \text{ m} = 5\sqrt{2} \approx 7.07 \text{ swaths, round up to 8 swaths to ensure complete coverage}$$

- 3 Use the Pythagorean theorem to determine the sensor triangle's altitude length.

$$a^2 + b^2 = c^2 \Rightarrow a^2 + (\sqrt{2} \text{ m})^2 = (2 \text{ m})^2 \Rightarrow a = \sqrt{2} \text{ m}$$

- 4 Determine the horizontal drive distance for the first swath.

$$\sqrt{2} \text{ m} + 20 \text{ m} - \sqrt{2} \text{ m} = 20 \text{ m}$$

- 5 Determine the vertical distance the rover must drive to position itself for the second swath. Note that the rover rotating in place does not add drive distance.

$$\sqrt{2} \text{ m} + \sqrt{2} \text{ m} = 2\sqrt{2} \text{ m}$$

- 6 Determine the horizontal drive distance for the second swath, then add it to the vertical distance. The result is the drive distance for each subsequent swath.

$$20 \text{ m} - 2\sqrt{2} \text{ m}$$

$$20 \text{ m} - 2\sqrt{2} \text{ m} + 2\sqrt{2} \text{ m} = 20 \text{ m}$$

- 7 Compute the total distance to be driven by all three rovers, then divide by three.

$$(20 \text{ m})(8) = 160 \text{ m}$$

$$(160 \text{ m}) / 3 \approx 53.3 \text{ m, round up to } \mathbf{54 \text{ m}}$$

